

Some applications for Spatial Network Analysis: transport, accessibility,
health, communities, economics and classification of regions

Crispin Cooper

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Mohammed, Anwar Hossein, Richard Price, Chinmoy Sarkar,
Brian Webb, Neil Harris, Adrian Healey*

Office for National Statistics
November 2019

Today's talk

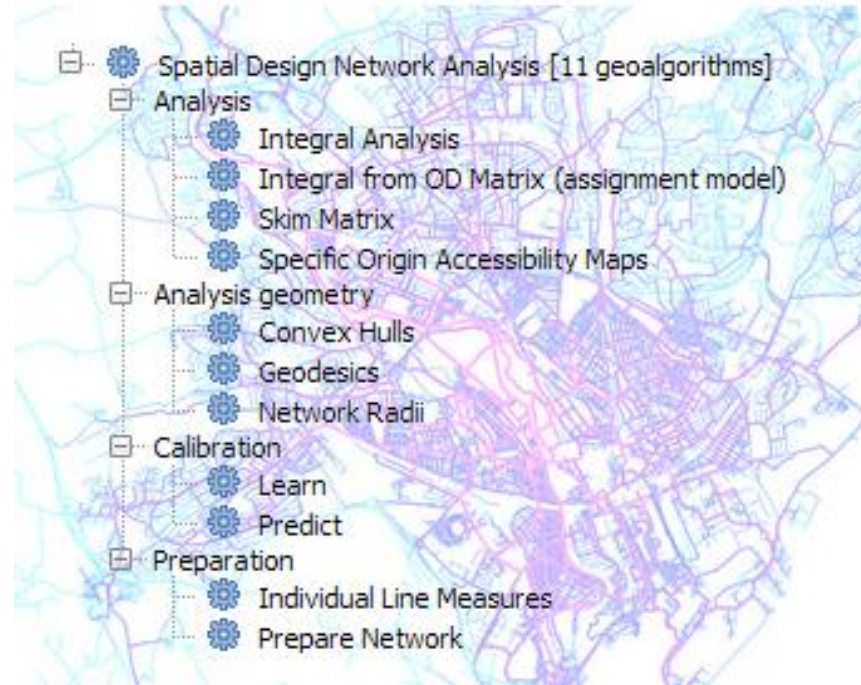
- Theory
 - Networks vs Spatial Networks
 - Distance, Reach, Closeness, Betweenness, Directness, Eigenvalue Centrality
 - What is accessibility?
- Applications
 - Transport
 - Cycling
 - Walking and accessibility
 - Community cohesion & health
 - Economics: house price, business rates & productivity (local, national)
 - Defining regions



About the sDNA software



- Software we've produced since 2011
 - Plugin for ArcGIS, QGIS, Autocad
 - Command line tools
 - Python API
 - Standard version = free and open source
 - C++/OpenMP backend, Python frontend

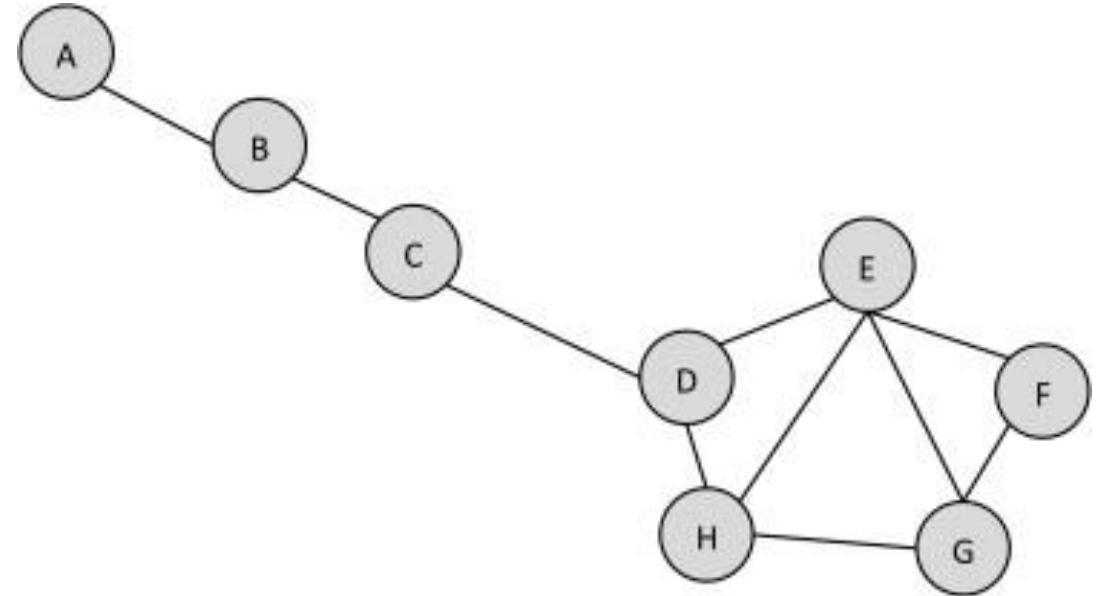


- All examples you are about to see use sDNA

A screenshot of the sDNA software settings panel. The panel is titled 'Input polyline features' and contains several configuration options. At the top, there is a dropdown menu for 'Input polyline features' and a green refresh button. Below this, there are four checked checkboxes: 'Compute betweenness', 'Betweenness is bidirectional', 'Compute junction counts', and 'Compute convex hull statistics'. There are two dropdown menus for 'Start grade separation [optional]' and 'End grade separation [optional]'. The 'Routing and analysis metric' is set to 'CYCLE_ROUNDTRIP'. The 'Radii (in units of radial metric or source data projection)' is set to '400,800,2000,n'. There are two checked checkboxes: 'Banded radius' and 'Continuous Space'. The 'Radial metric' is set to 'MATCH_ANALYTICAL'. The 'Weighting' is set to 'Link'. There are two dropdown menus for 'Origin weight [optional]' and 'Destination weight [optional]'. At the bottom, there is a dropdown menu for 'Origin Destination Matrix input file [optional]'.

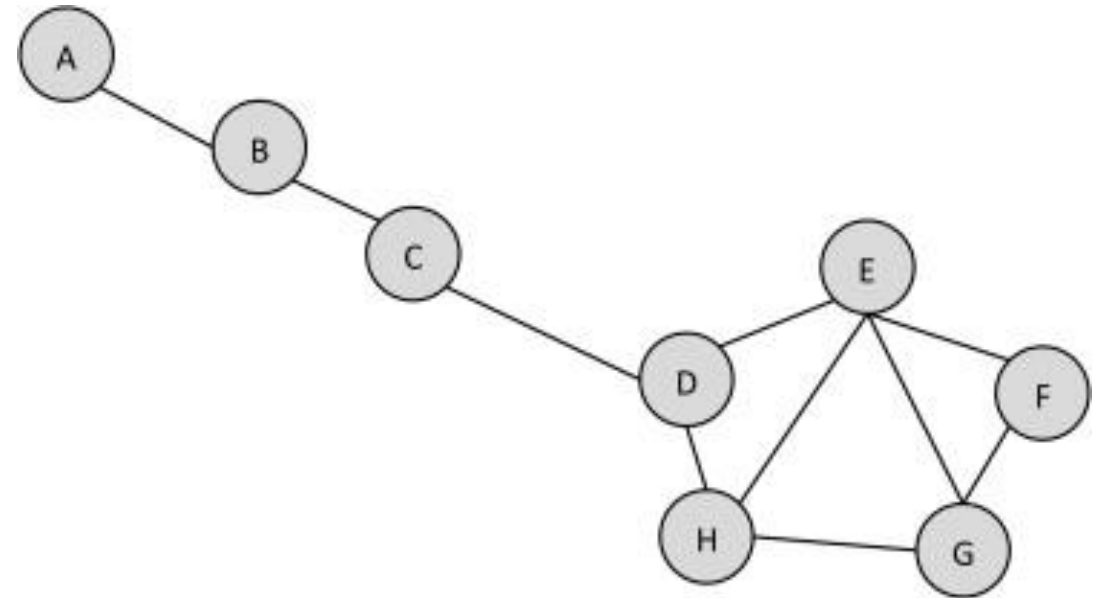
Networks

- Networks
 - Nodes connected by links
 - Measuring distance through network



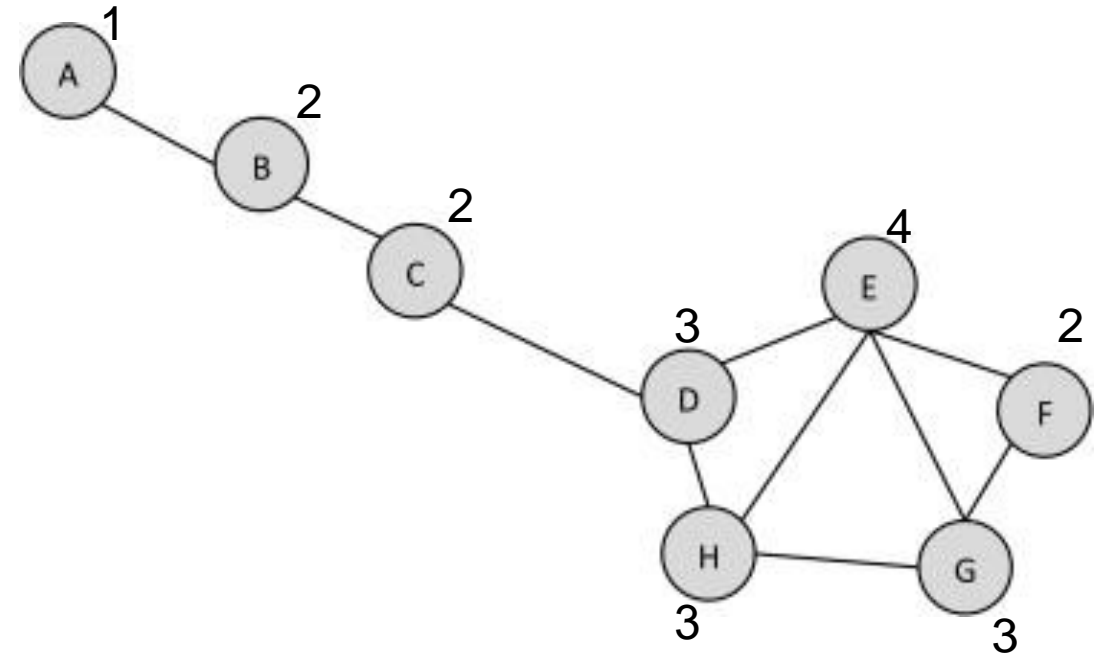
Networks

- Networks
 - Nodes connected by links
 - Centrality measures
 - Degree centrality: number of links from a node
 - Mean distance: mean number of hops from a given node to the others
 - Closeness: $1/\text{mean distance}$
 - Betweenness: number of shortest paths (everywhere to everywhere) that pass through a given node
 - Reach: number of nodes within given distance



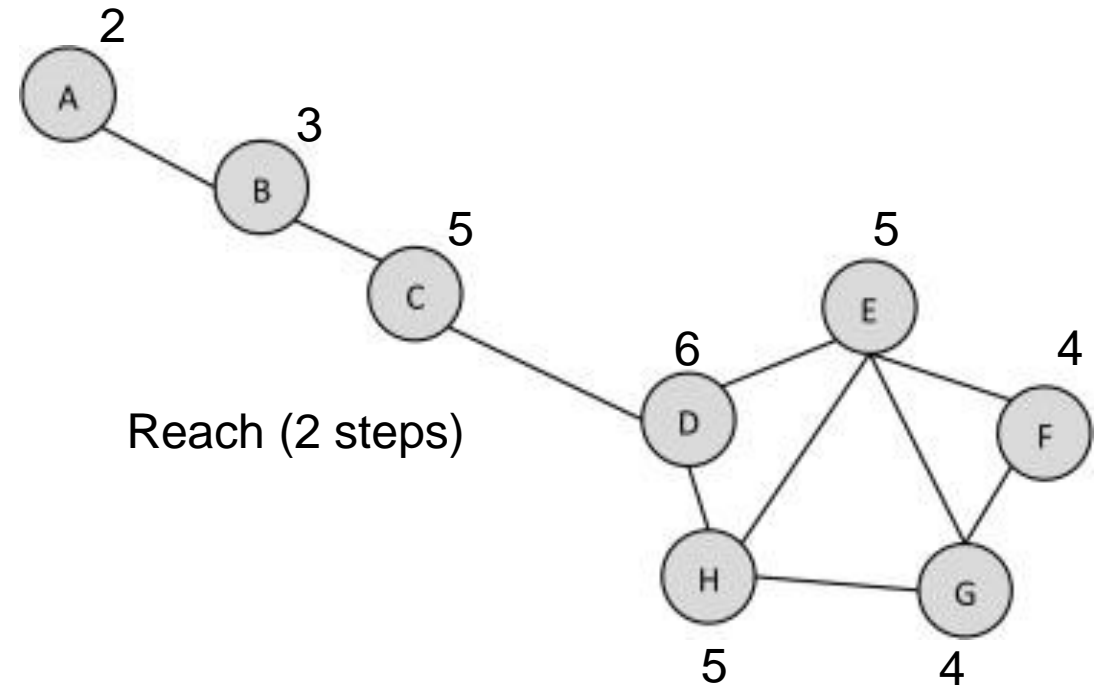
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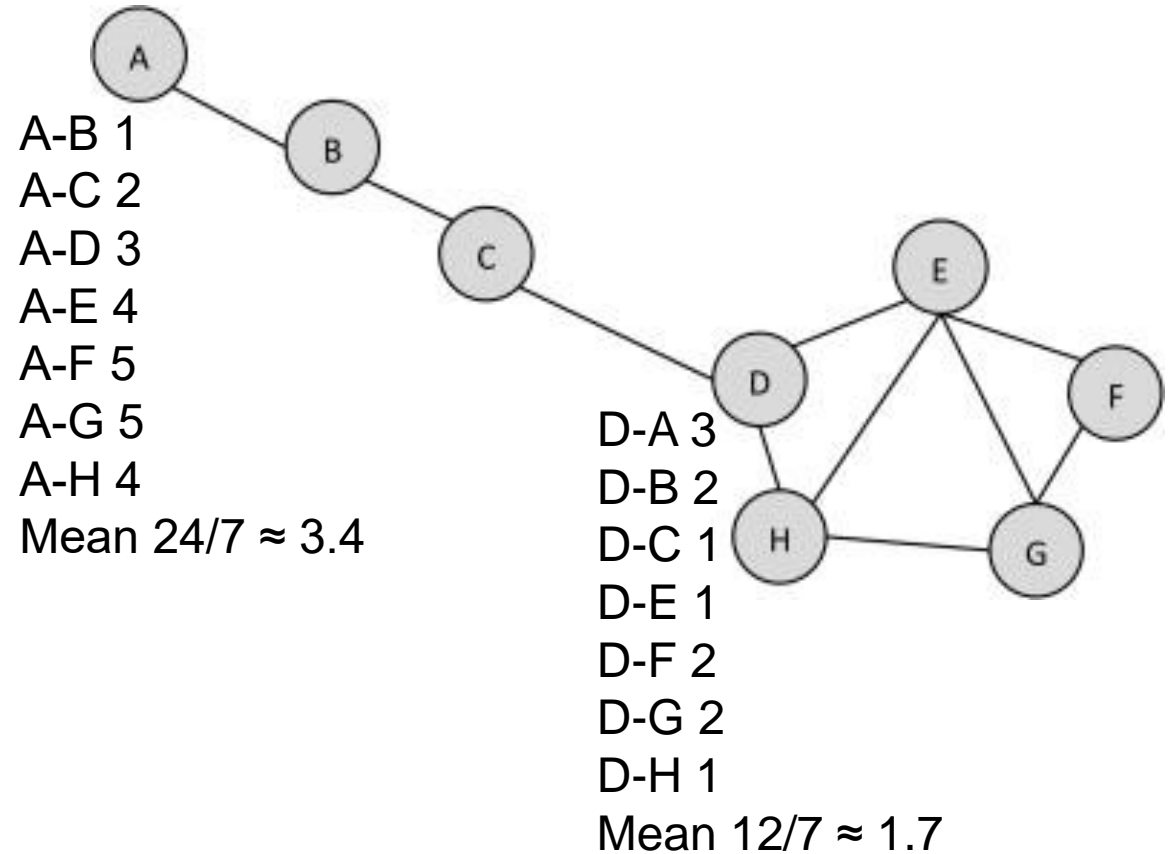
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Networks

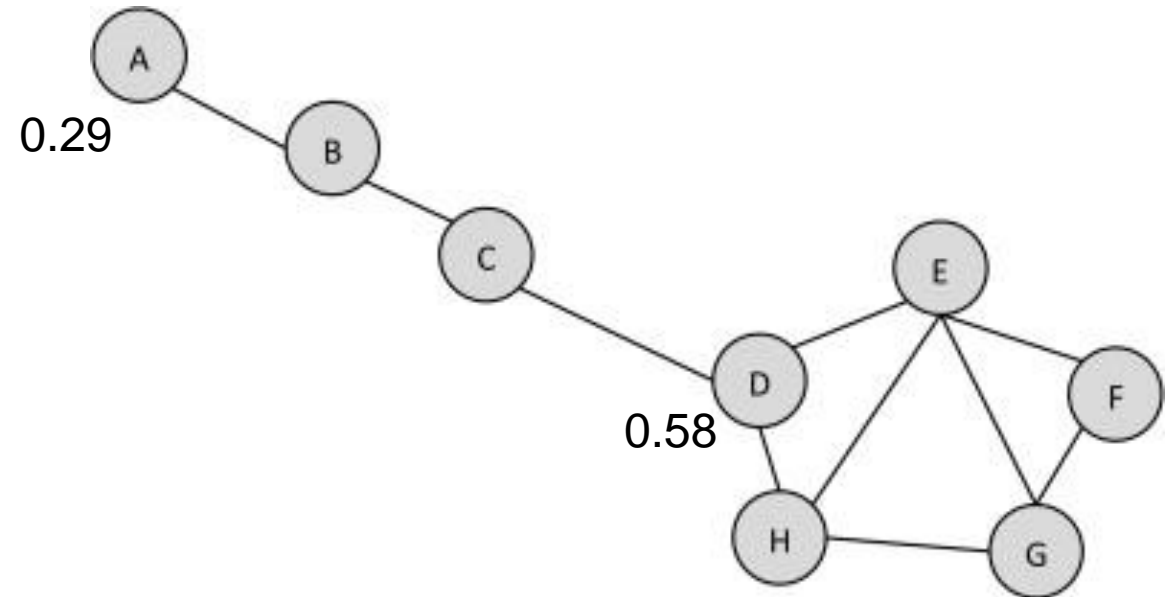
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Networks

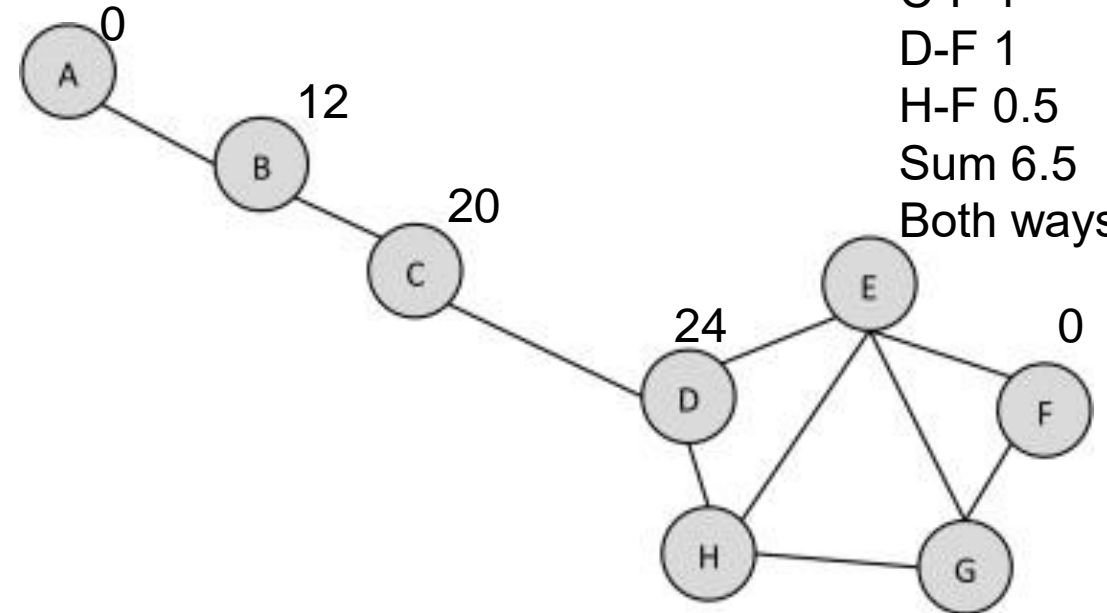
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Networks

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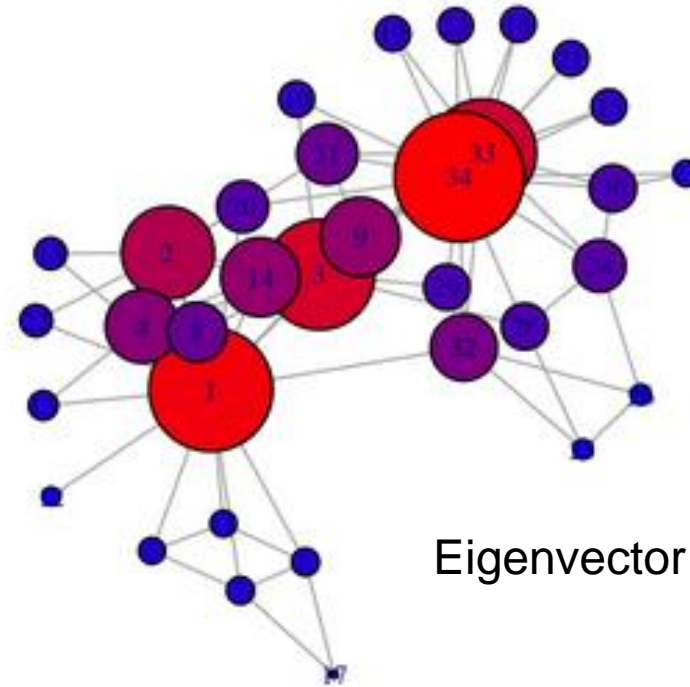
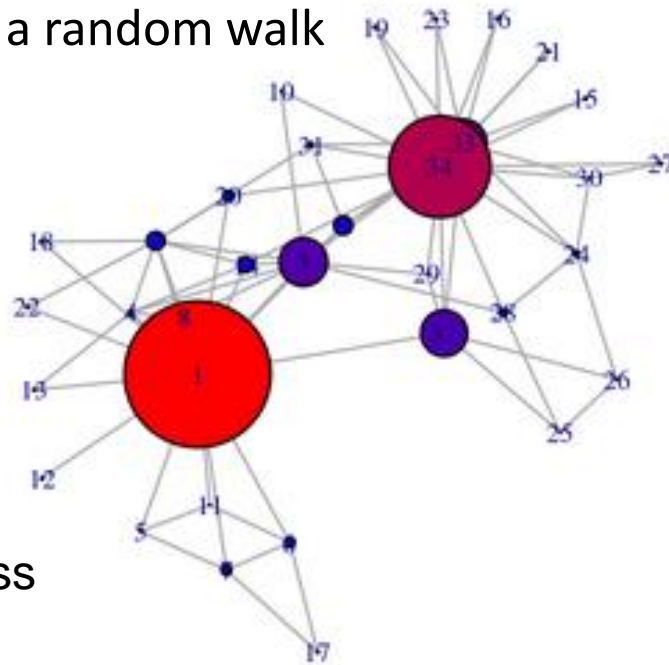
A-G 0.5
B-G 0.5
C-G 0.5
D-G 0.5
A-F 1
B-F 1
C-F 1
D-F 1
H-F 0.5
Sum 6.5
Both ways 13

A-G 0.5
B-G 0.5
C-G 0.5
D-G 0.5
Sum 2
Both ways 4
H-F 0.5
Both ways 1

Networks

- Eigenvector centrality
 - Principal eigenvector of connectivity matrix
 - Google PageRank
 - Betweenness of a random walk

Betweenness



Eigenvector

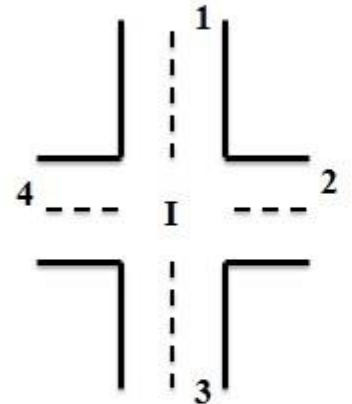
http://www.rpubs.com/shestakoff/sna_lab4

What's different about Spatial Networks?

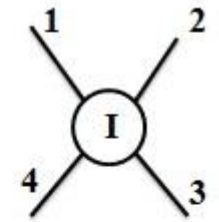
- Ontological
 - Nodes have positions in space
 - Links have shape: they may not be straight lines
- Analytical
 - We care more about links than nodes => dual representation
 - We can use spatial characteristics to define weightings and distance
 - We can restrict measures to spatial locality
 - We can use spatially explicit measures (more on this later)

Dual representation

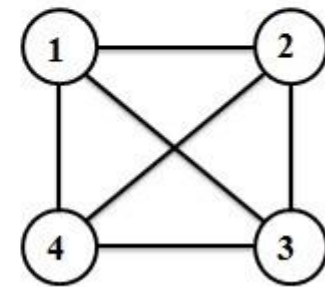
- Links become nodes, nodes become links (Añez 1996)
- Nodes (e.g. roads) now have spatial extent
 - Self closeness
 - Self betweenness (SoftwareX? 2019)



Road Network with an intersection



Primal Graph

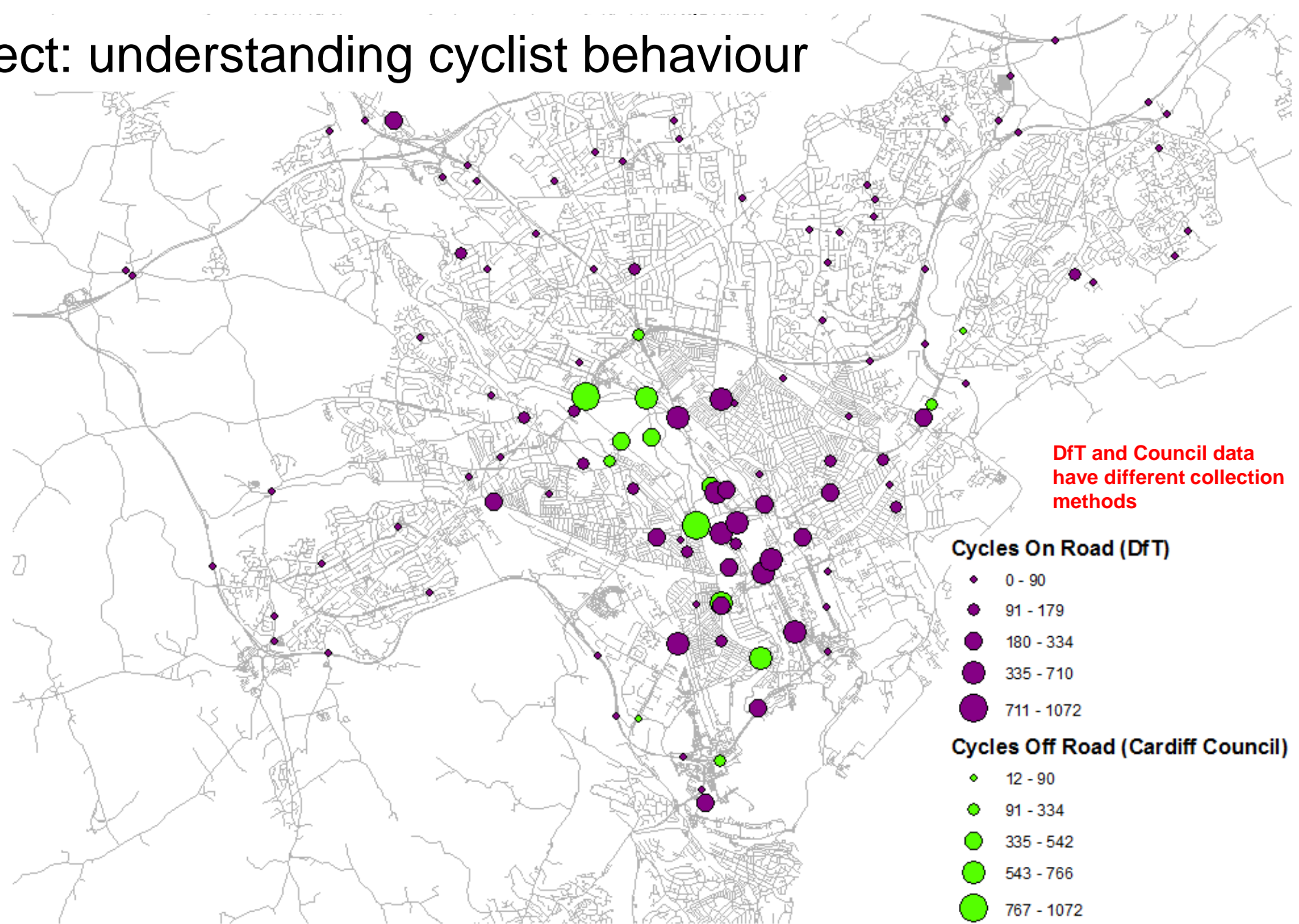


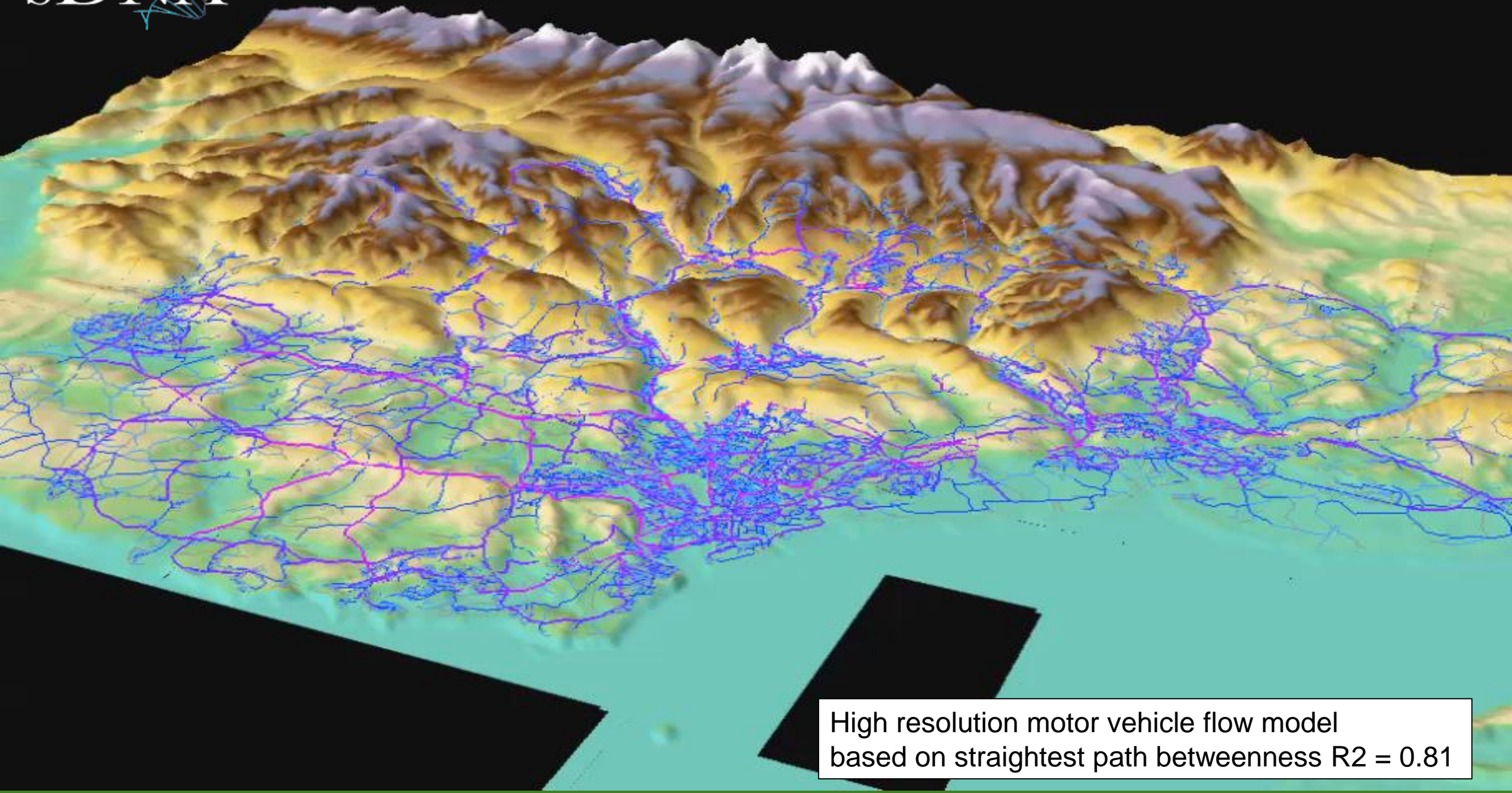
Dual Graph

Using space and localizing measures

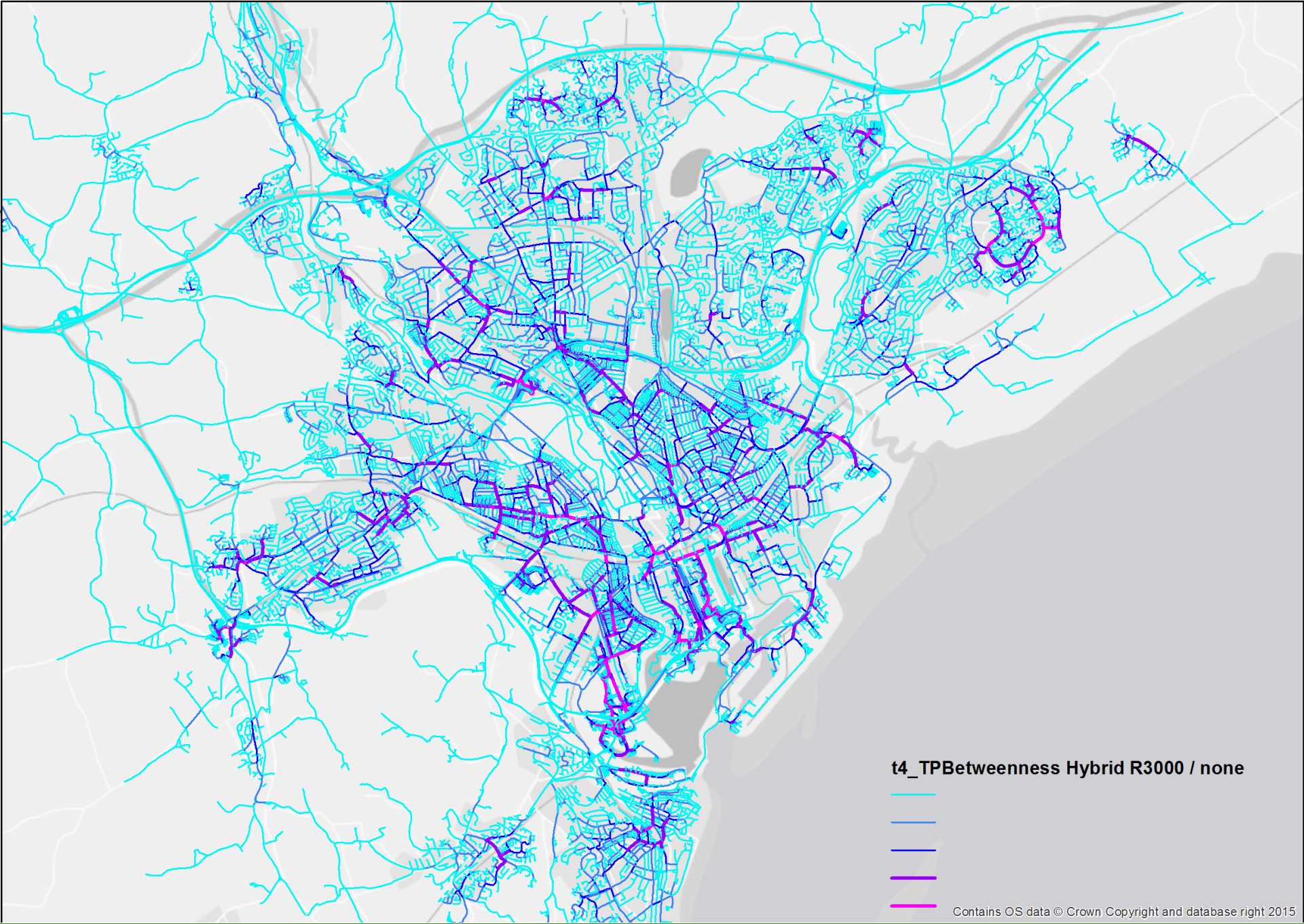
- Distance metrics
 - Length along network: network-Euclidean i.e. shortest distance
 - Angular: least turning, most direct
 - Topological: fewest junctions
 - Travel time
 - Cyclist distance: negative utility including aversion to hills and traffic
 - Pedestrian distance: blend of shortest plus straightest with randomization
- Localizing
 - “Cut out” the network surrounding each link within e.g. a 5km network-Euclidean buffer
 - Compute network statistics for the locality
 - Details
 - Only remove origins/destinations or also remove links for routing? How to handle paths that exceed size of the locality? Does it matter – compute time, desired results? (IJGIS 2015)

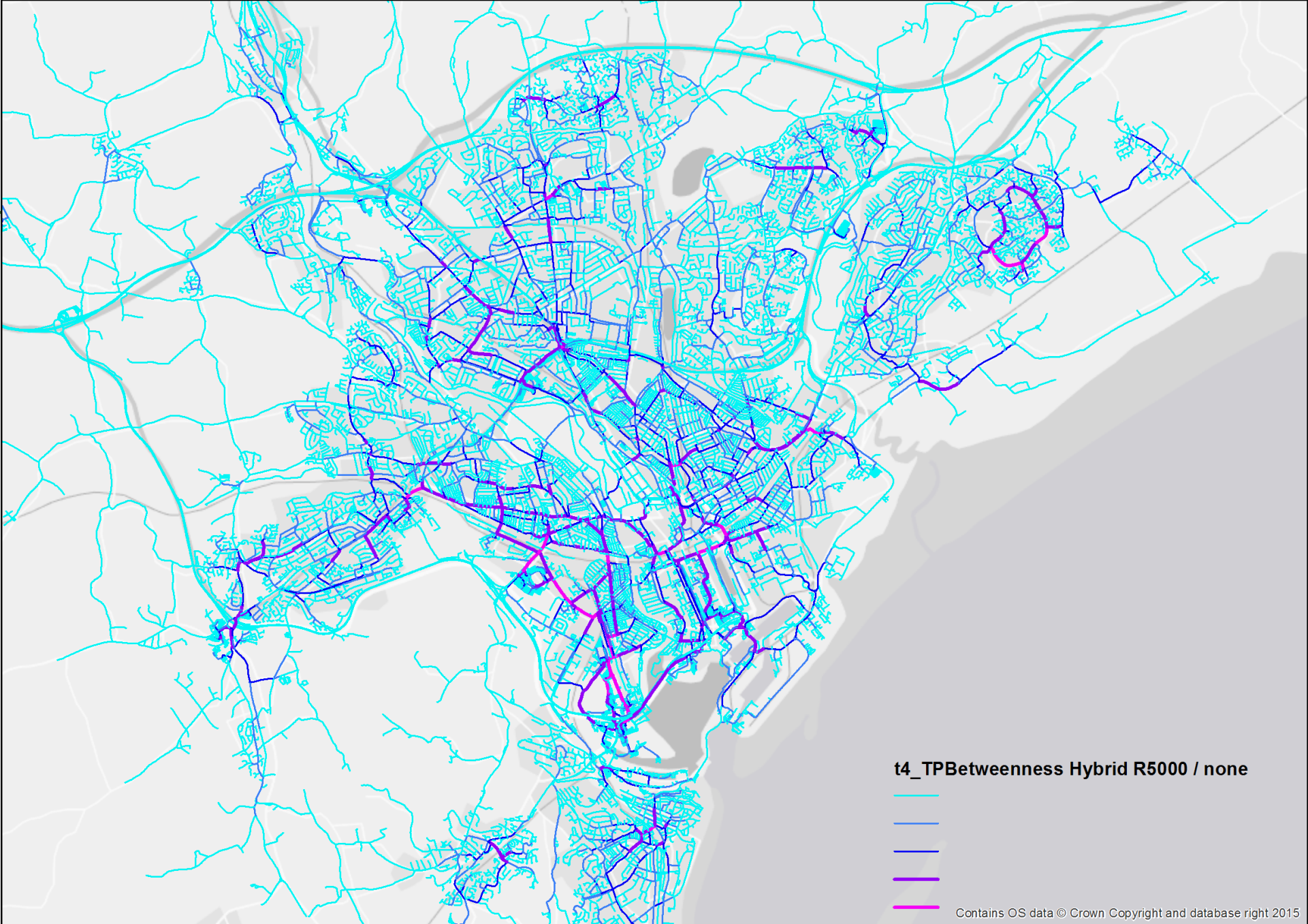
Project: understanding cyclist behaviour

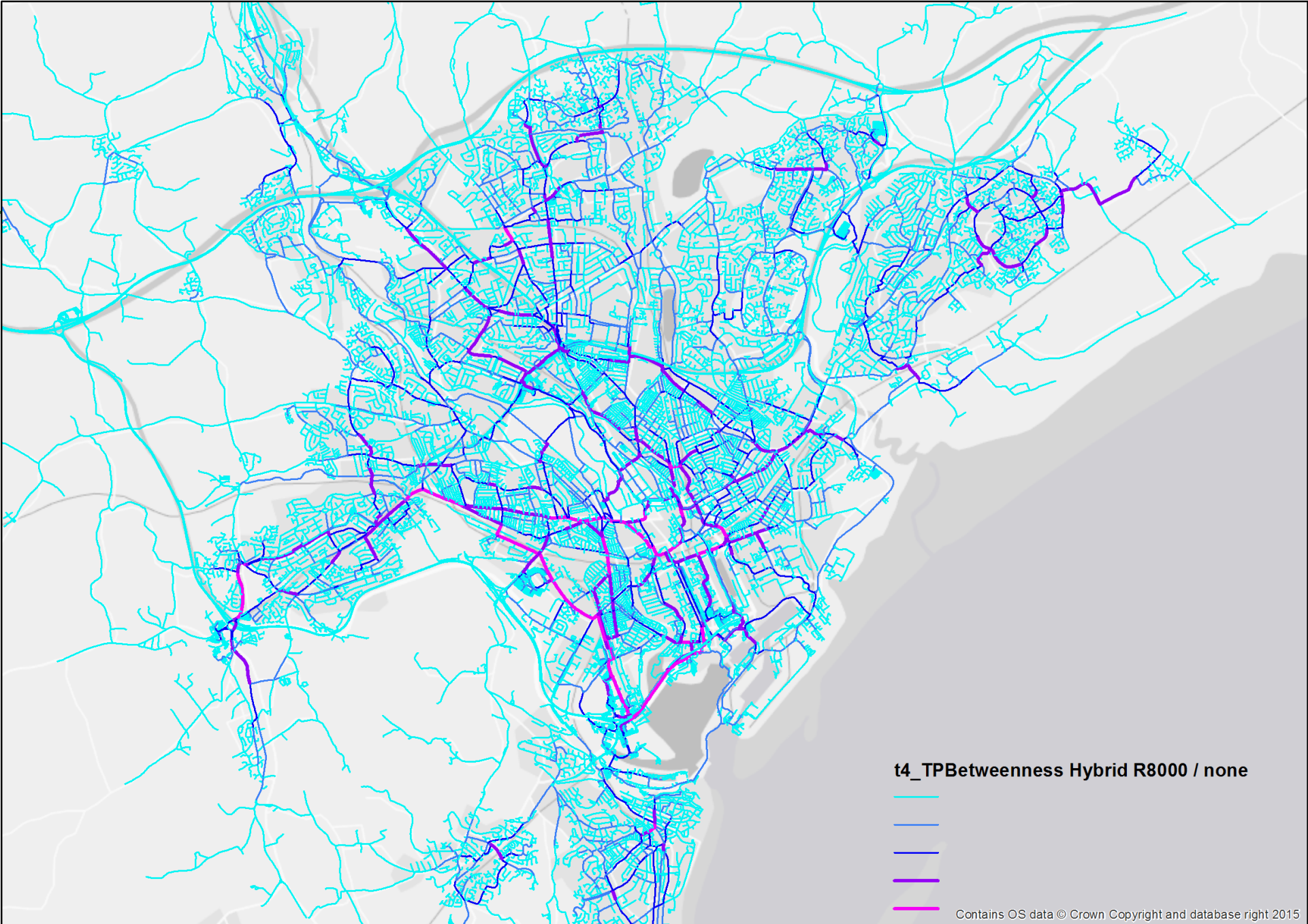


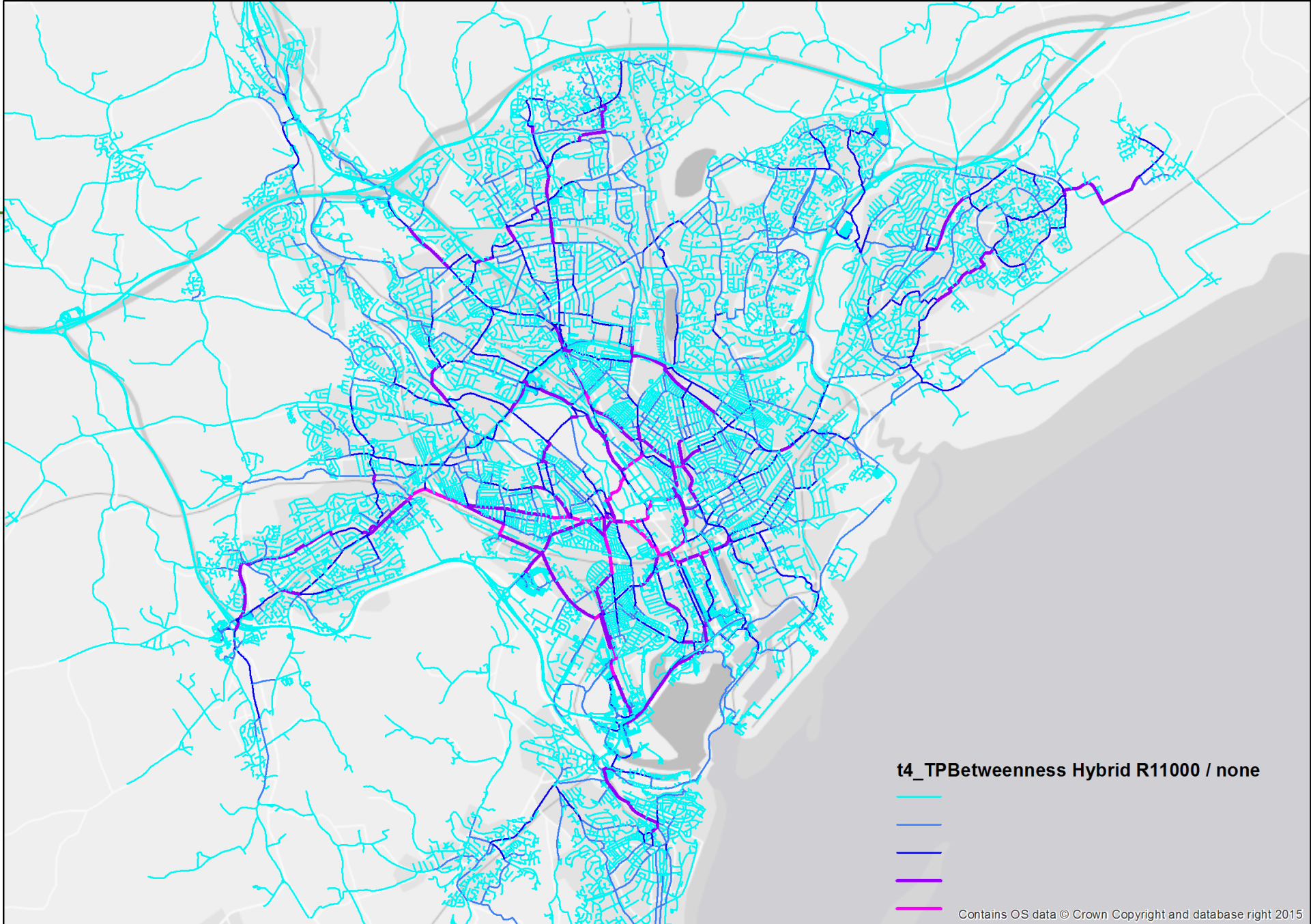


High resolution motor vehicle flow model
based on straightest path betweenness $R^2 = 0.81$

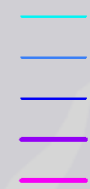




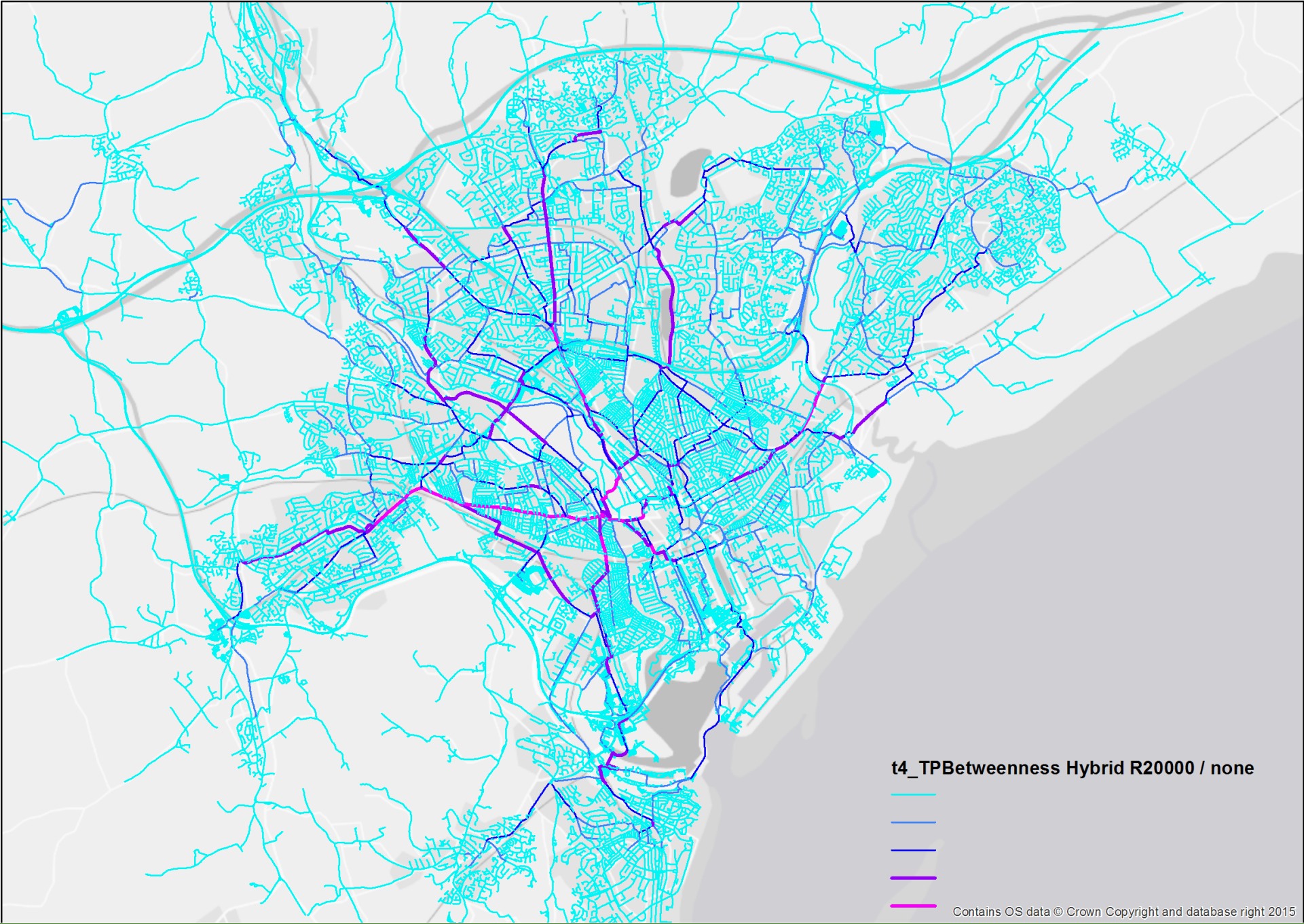




t4_TPBetweenness Hybrid R11000 / none



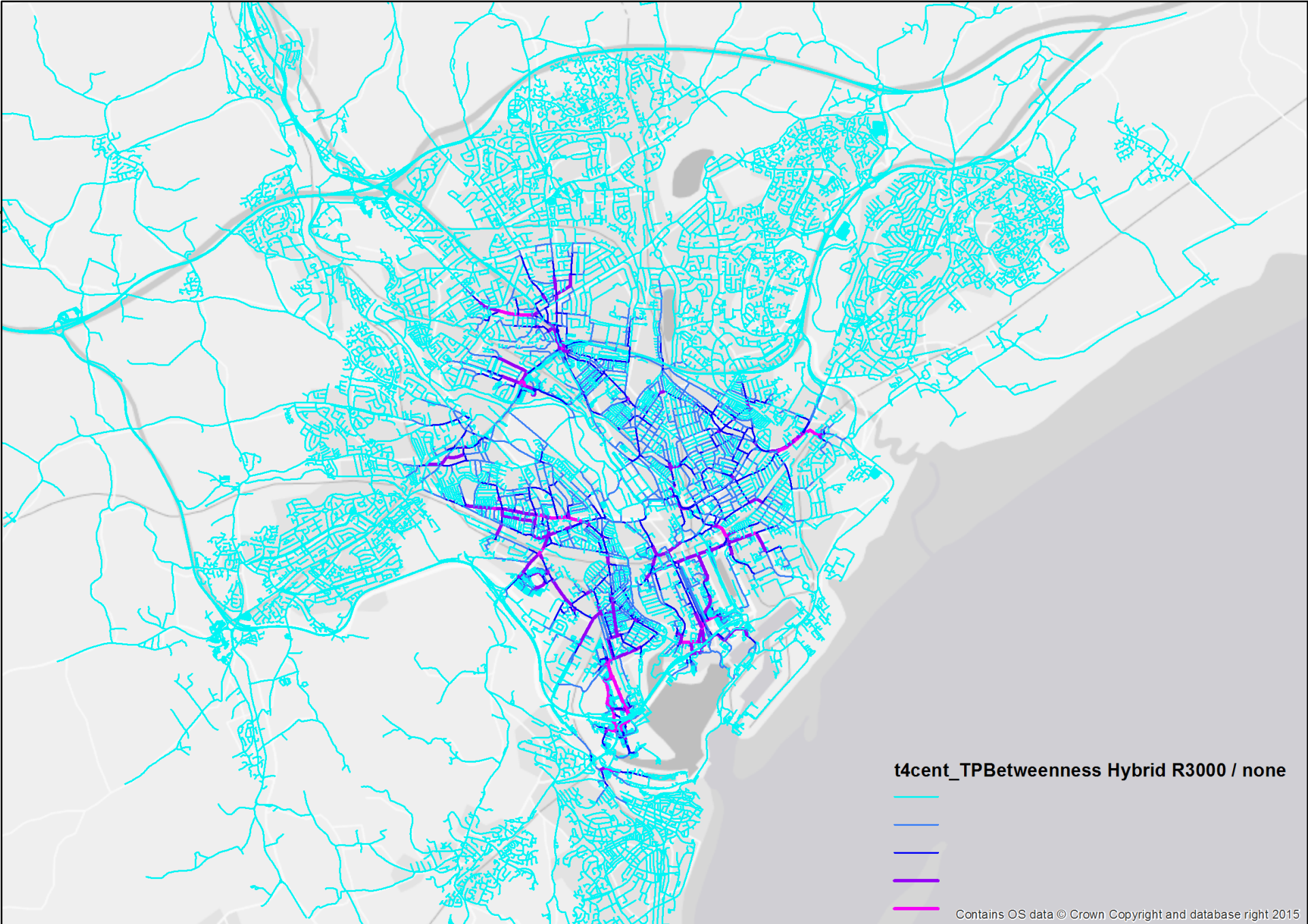
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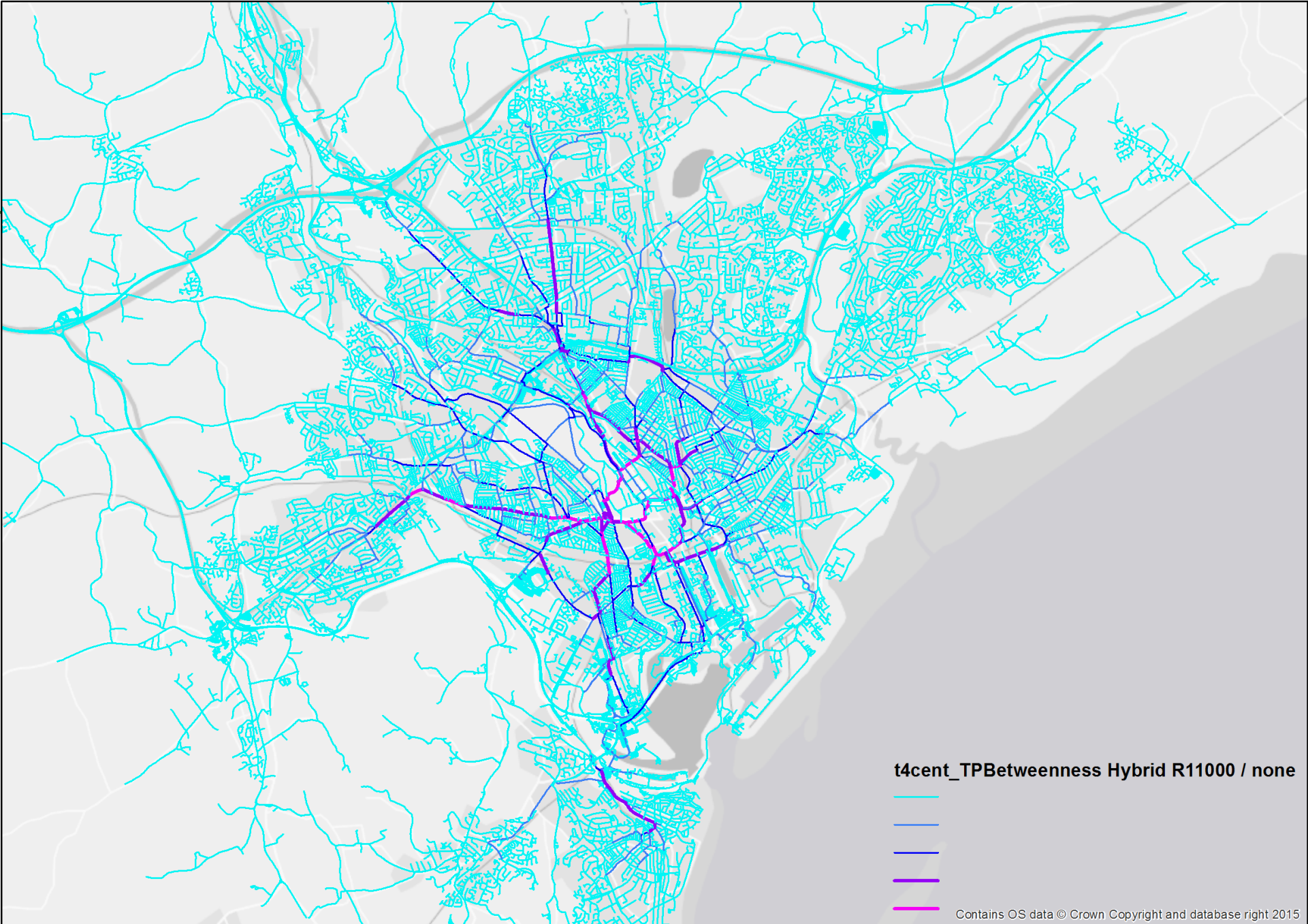


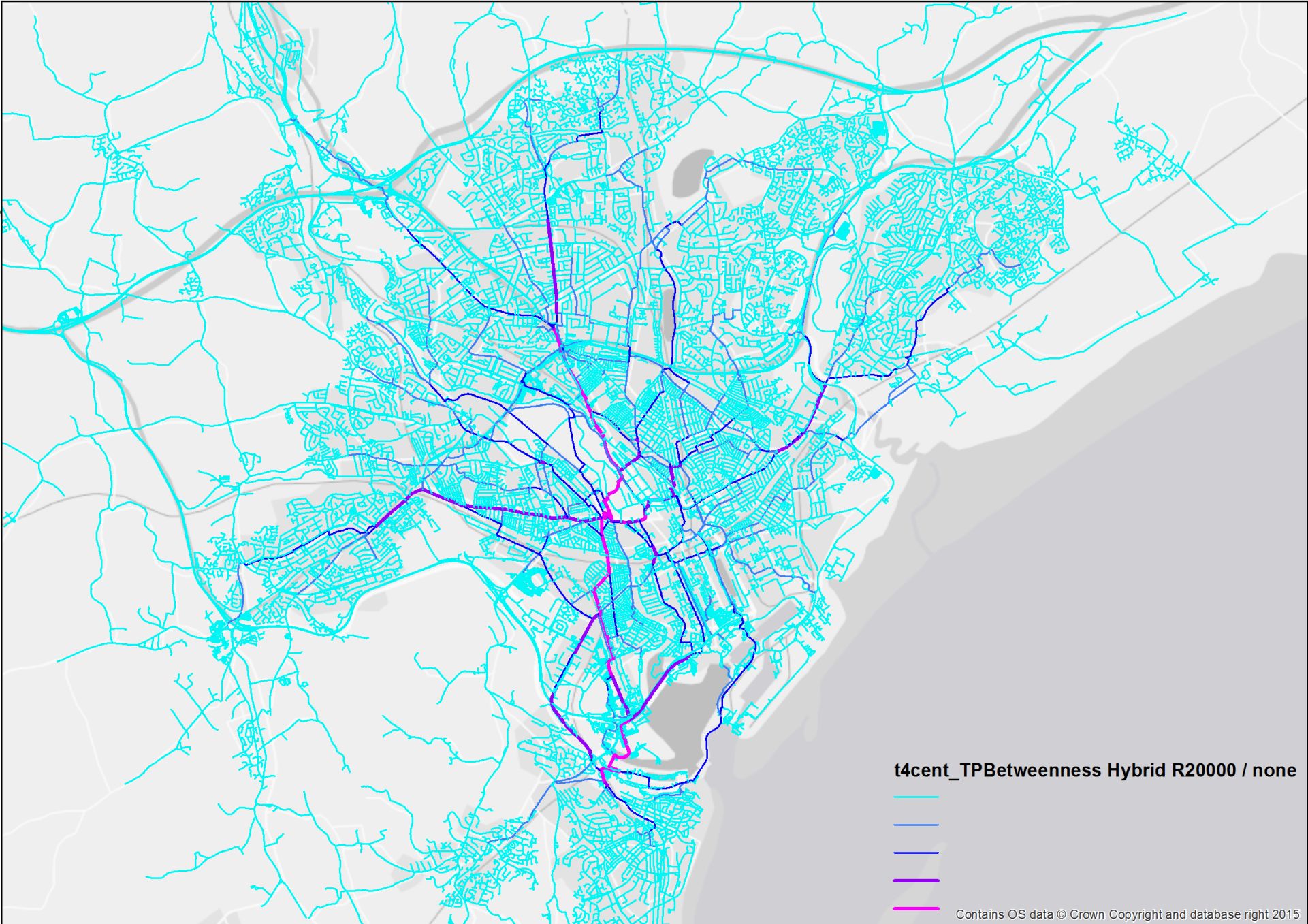
t4_TPBetweenness Hybrid R20000 / none

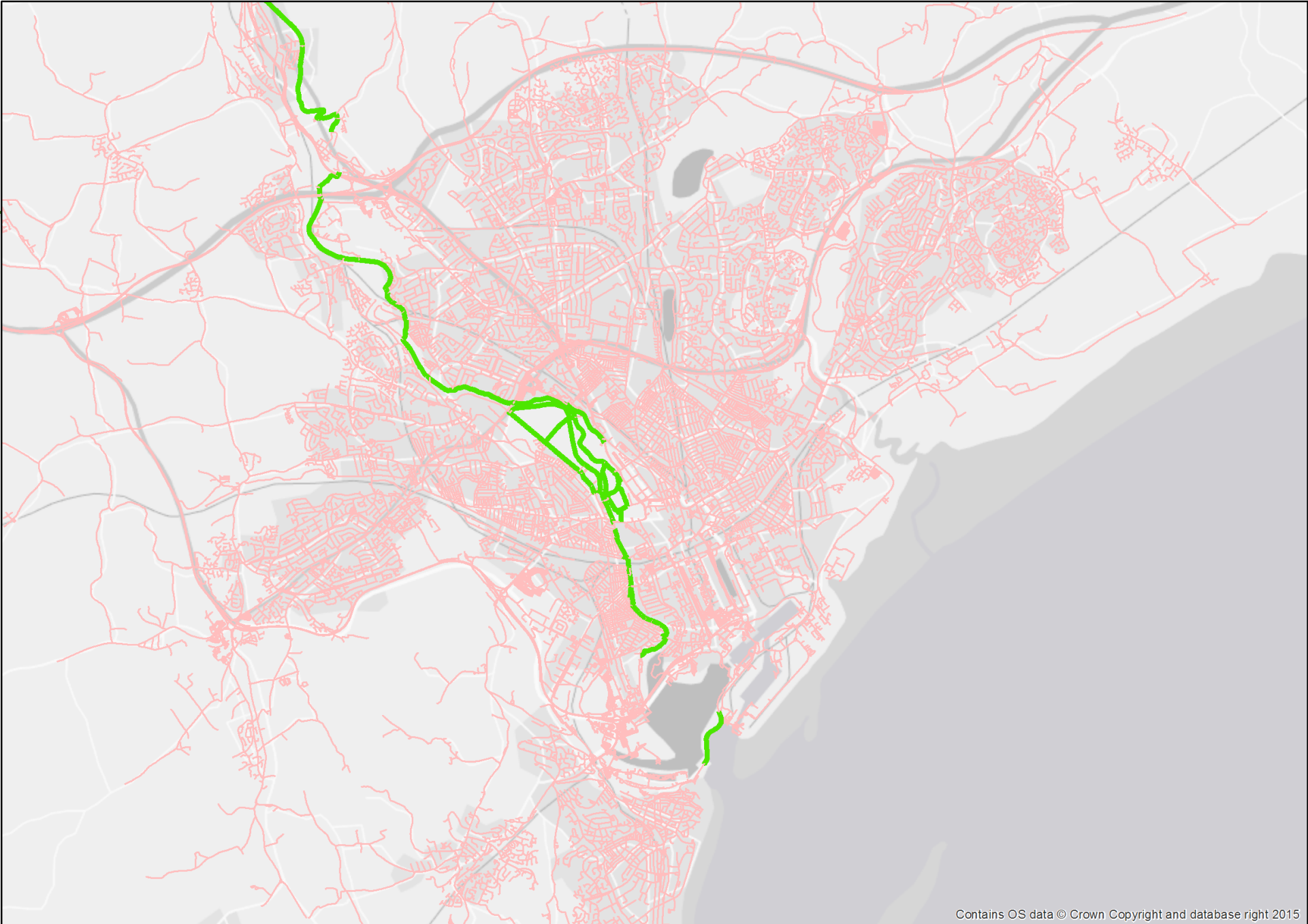


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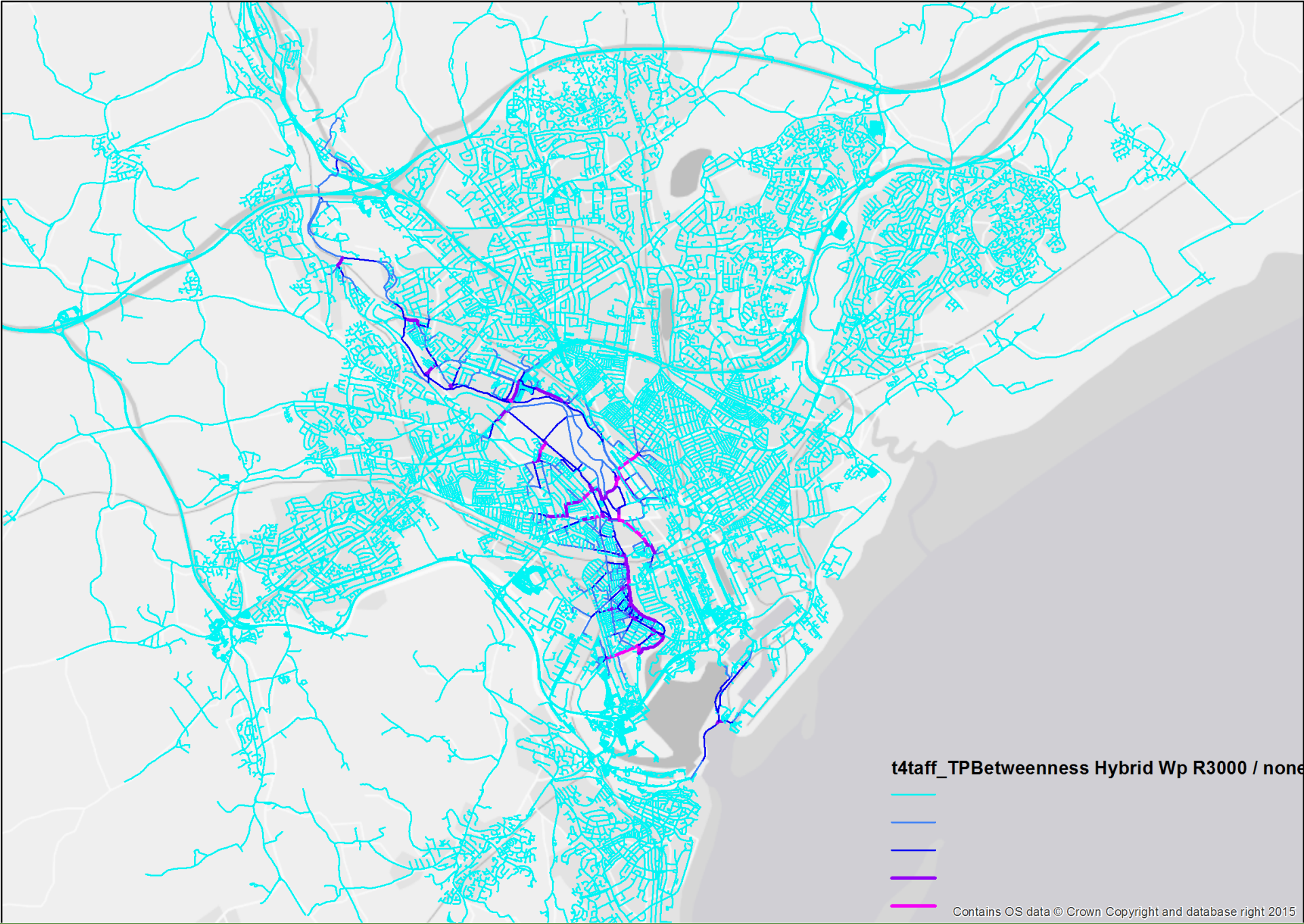








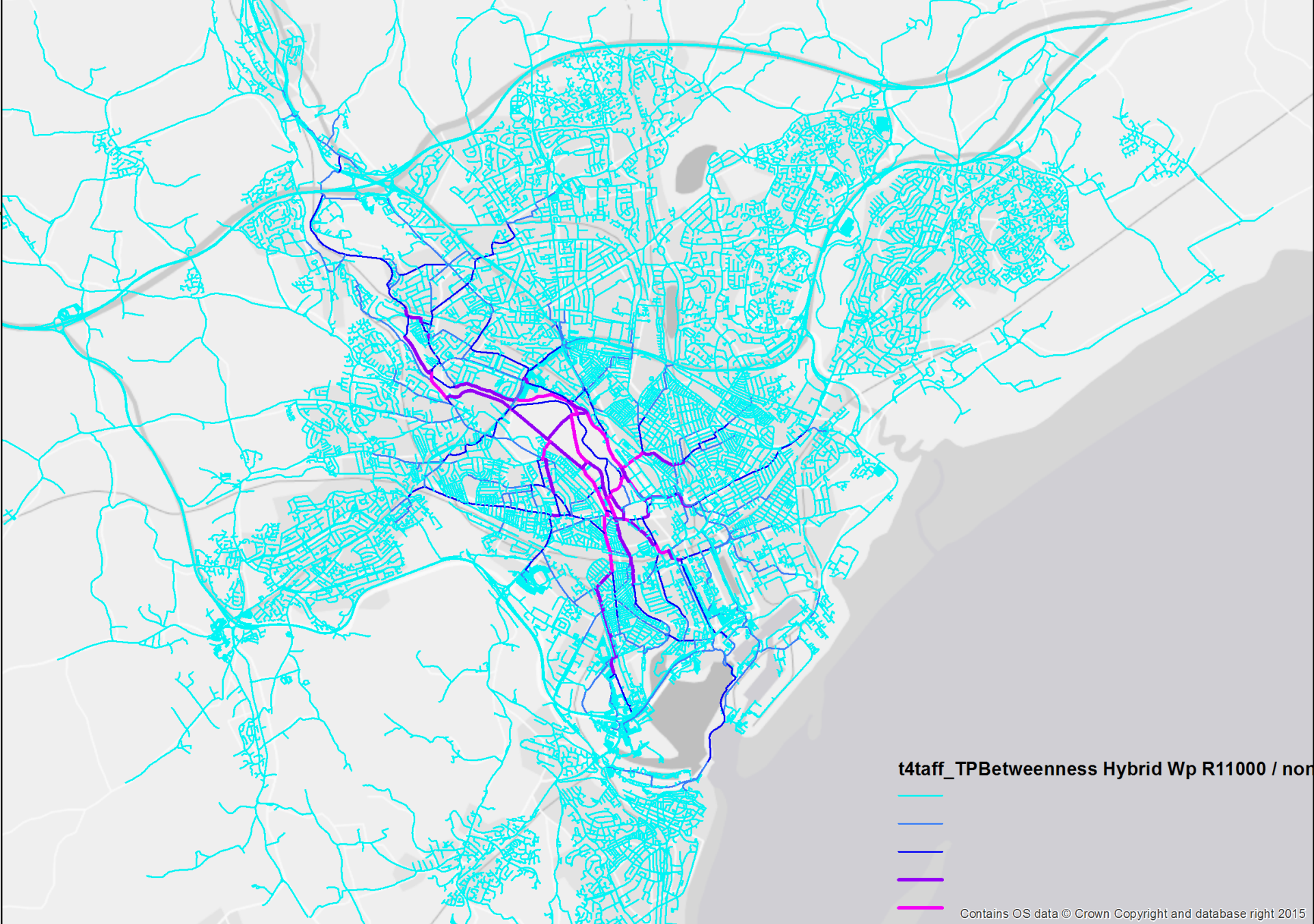
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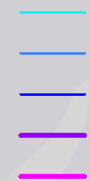
t4taff_TPBetweenness Hybrid Wp R3000 / none



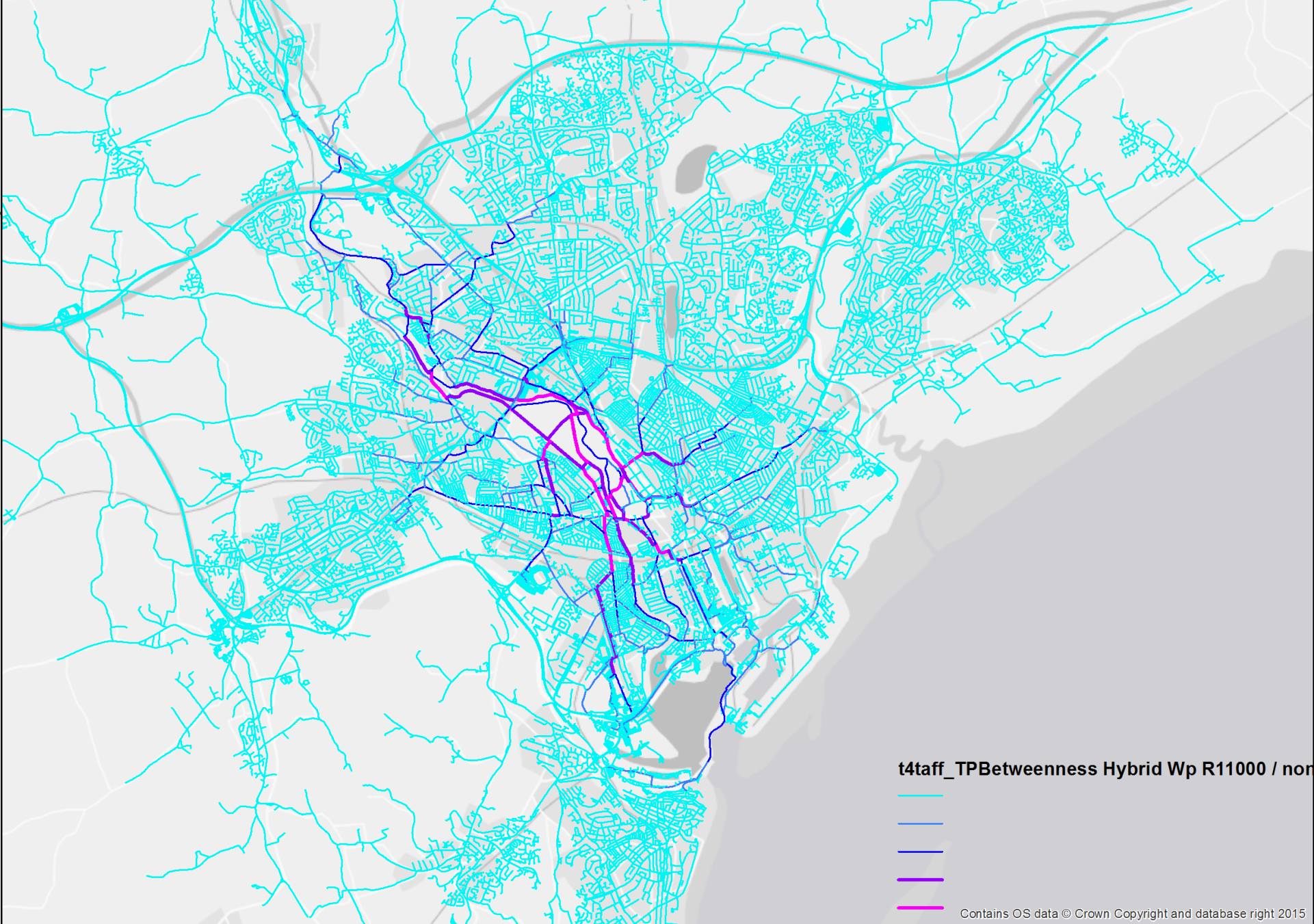
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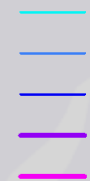
t4taff_TPBetweenness Hybrid Wp R11000 / nor



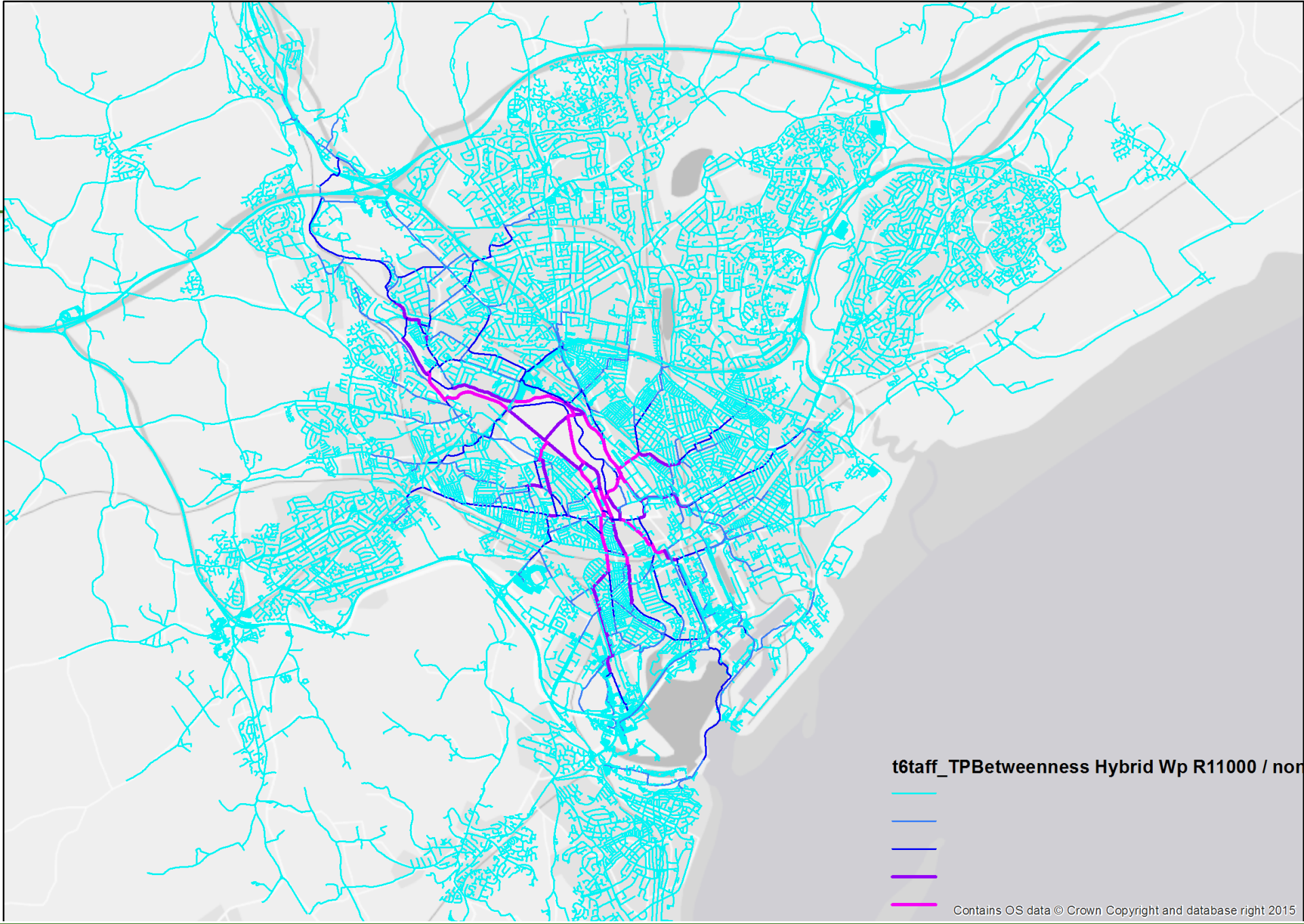
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t4taff_TPBetweenness Hybrid Wp R11000 / nor

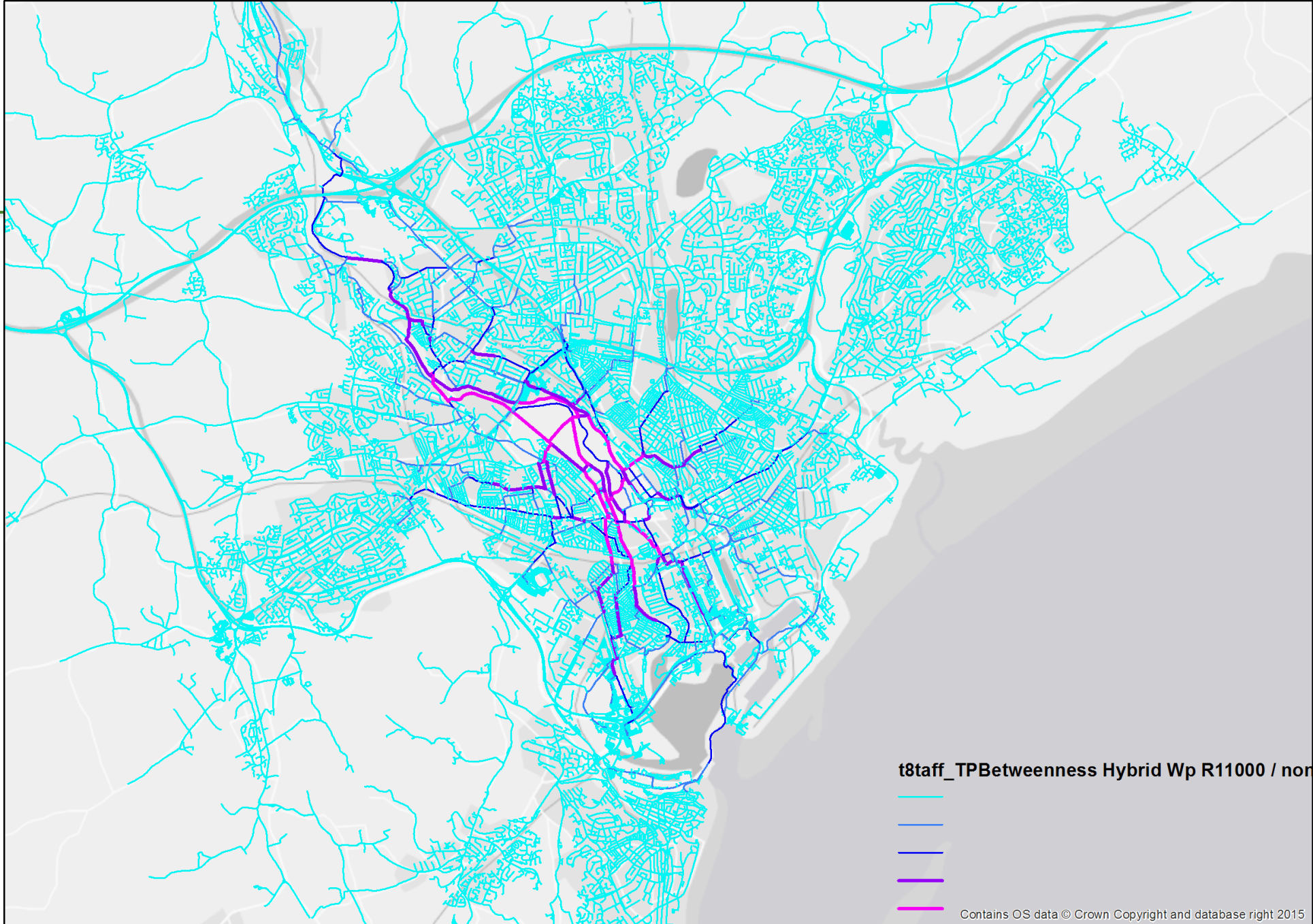


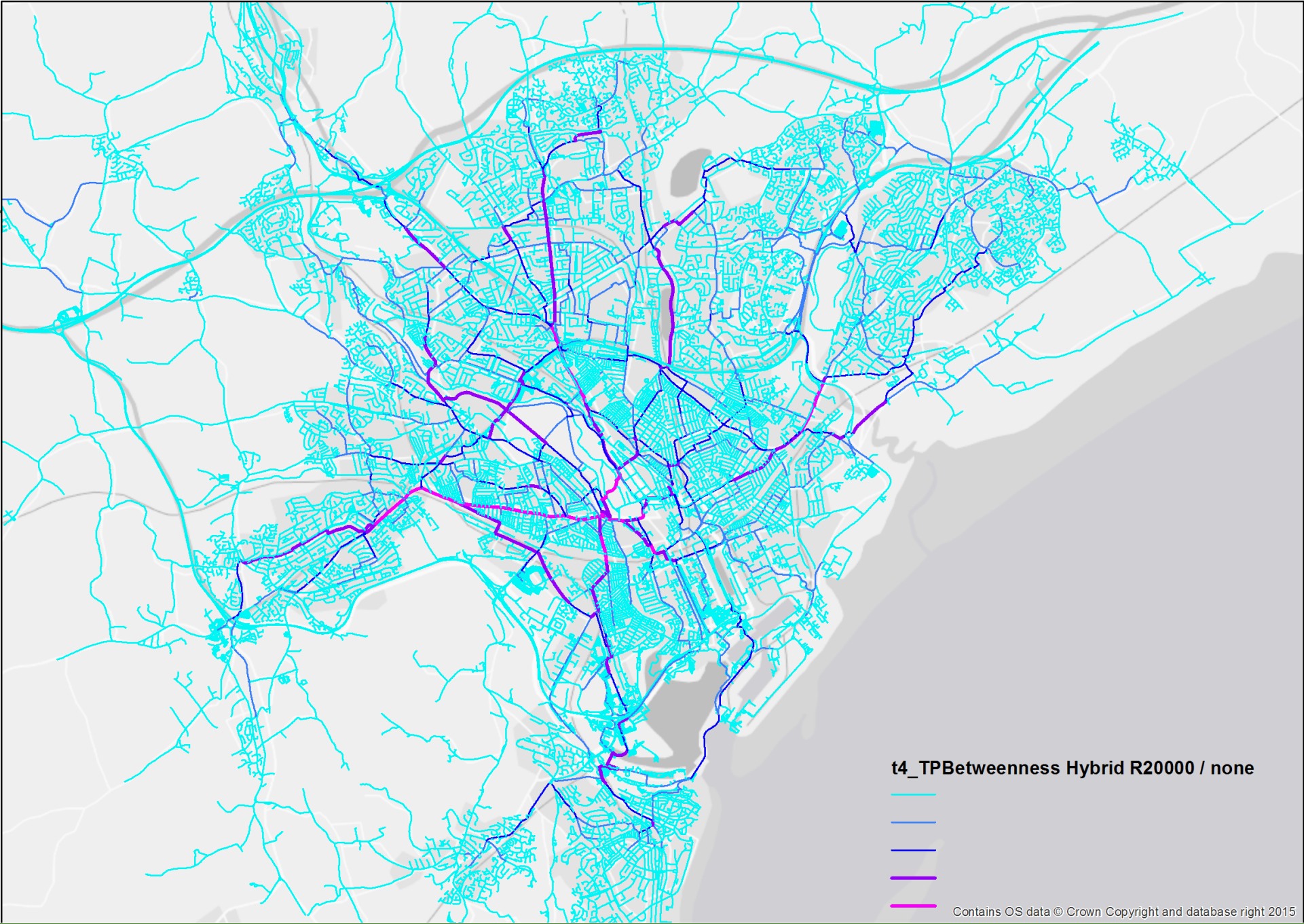
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t6taff_TPBetweenness Hybrid Wp R11000 / nor

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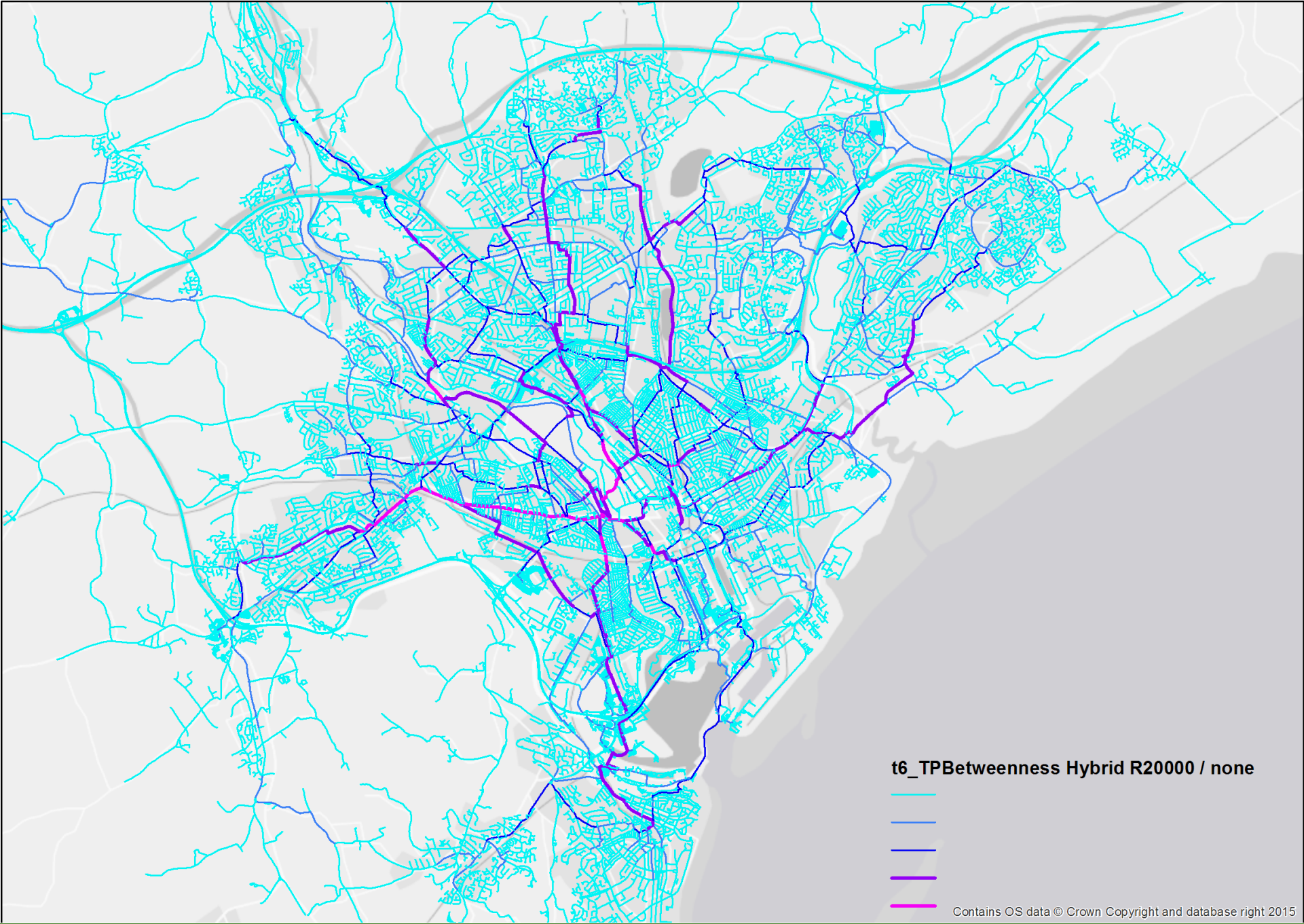




t4_TPBetweenness Hybrid R20000 / none



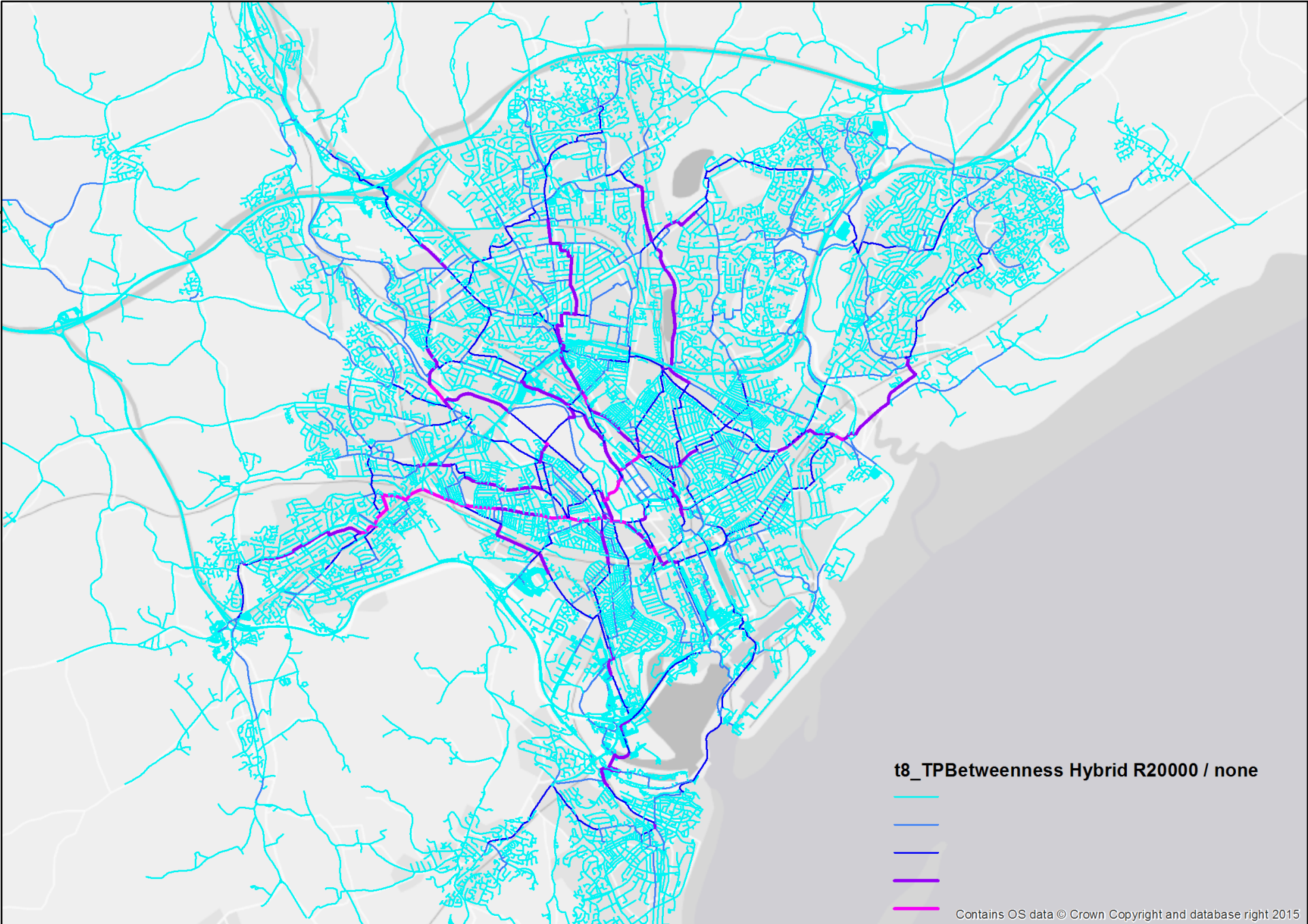
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t6_TPBetweenness Hybrid R20000 / none

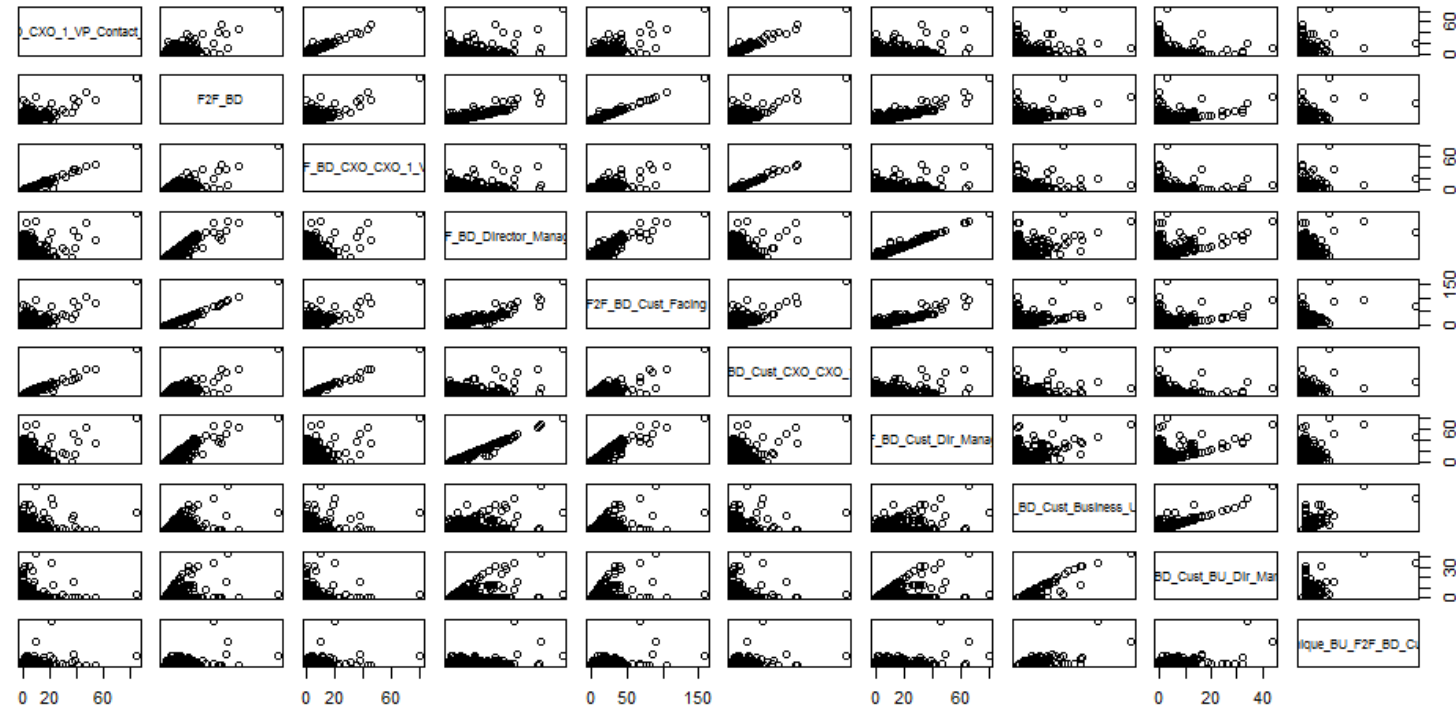


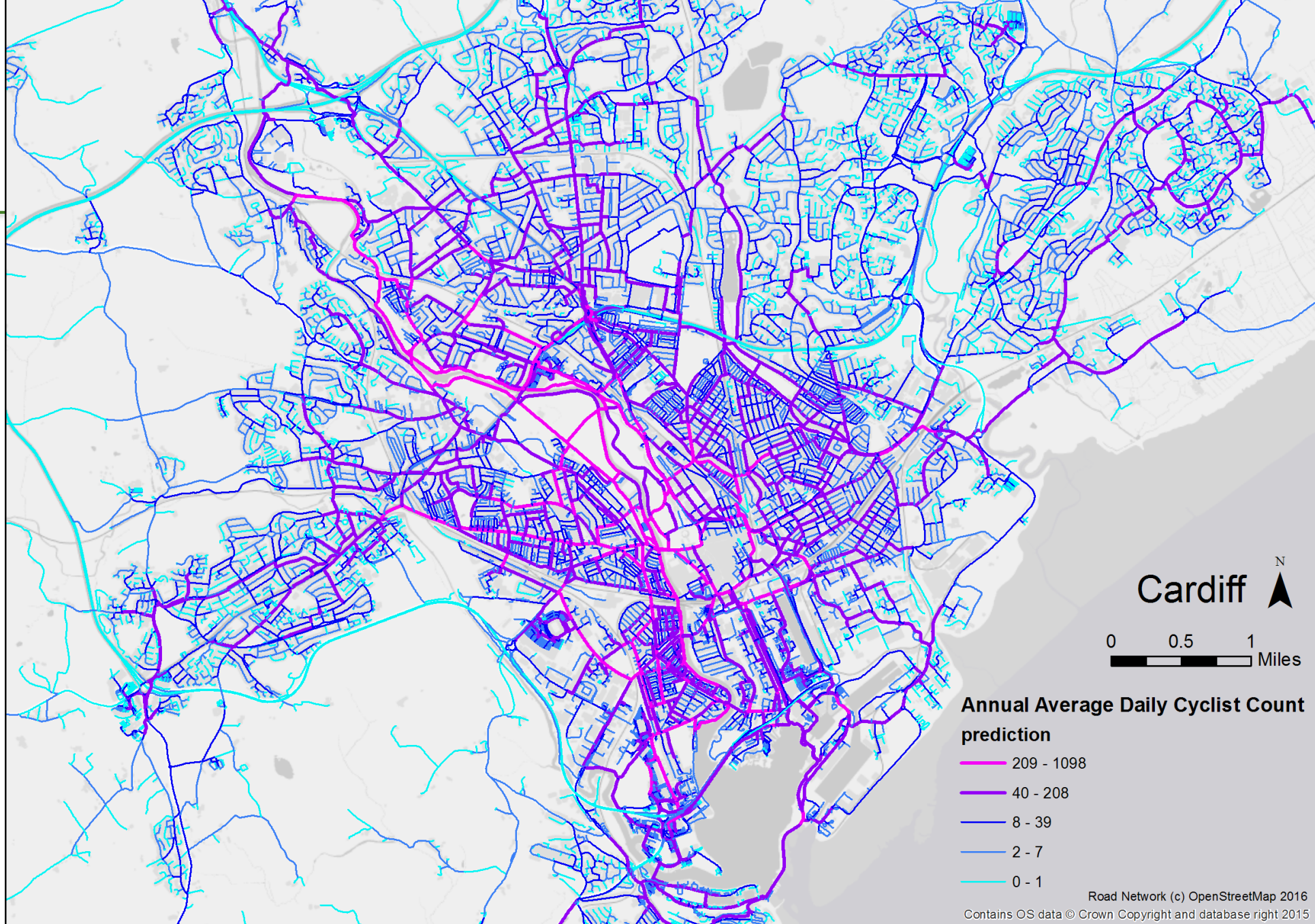
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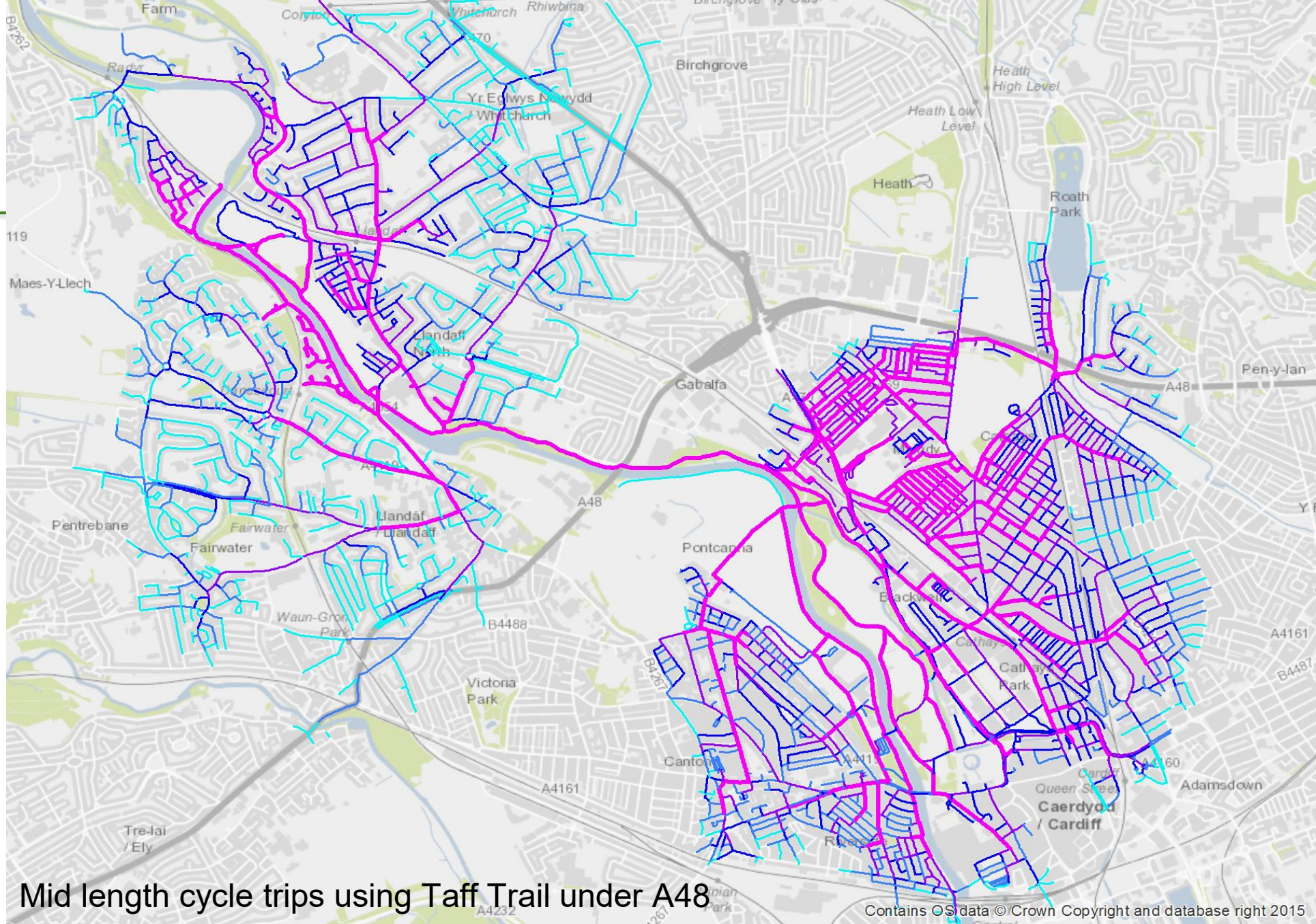


Predicting flows

- Each betweenness calculation can be seen as a potential cyclist behaviour / independent variable
- Fit linear model to flow data to see what combination of behaviours best explains observations
- High collinearity between variables leads to overfitting on noise generated by differences between similar variables
- Use regularized regression
 - OLS minimizes $\sum(y - \beta X)^2$
 - ridge minimizes $\sum(y - \beta X)^2 + \lambda \sum \beta^2$
 - lasso minimizes $\sum(y - \beta X)^2 + \lambda \sum |\beta|$
- Cross-validation to select optimal λ and prevent overfit
- R^2 (weighted to reduce effect of large flows) = 0.78

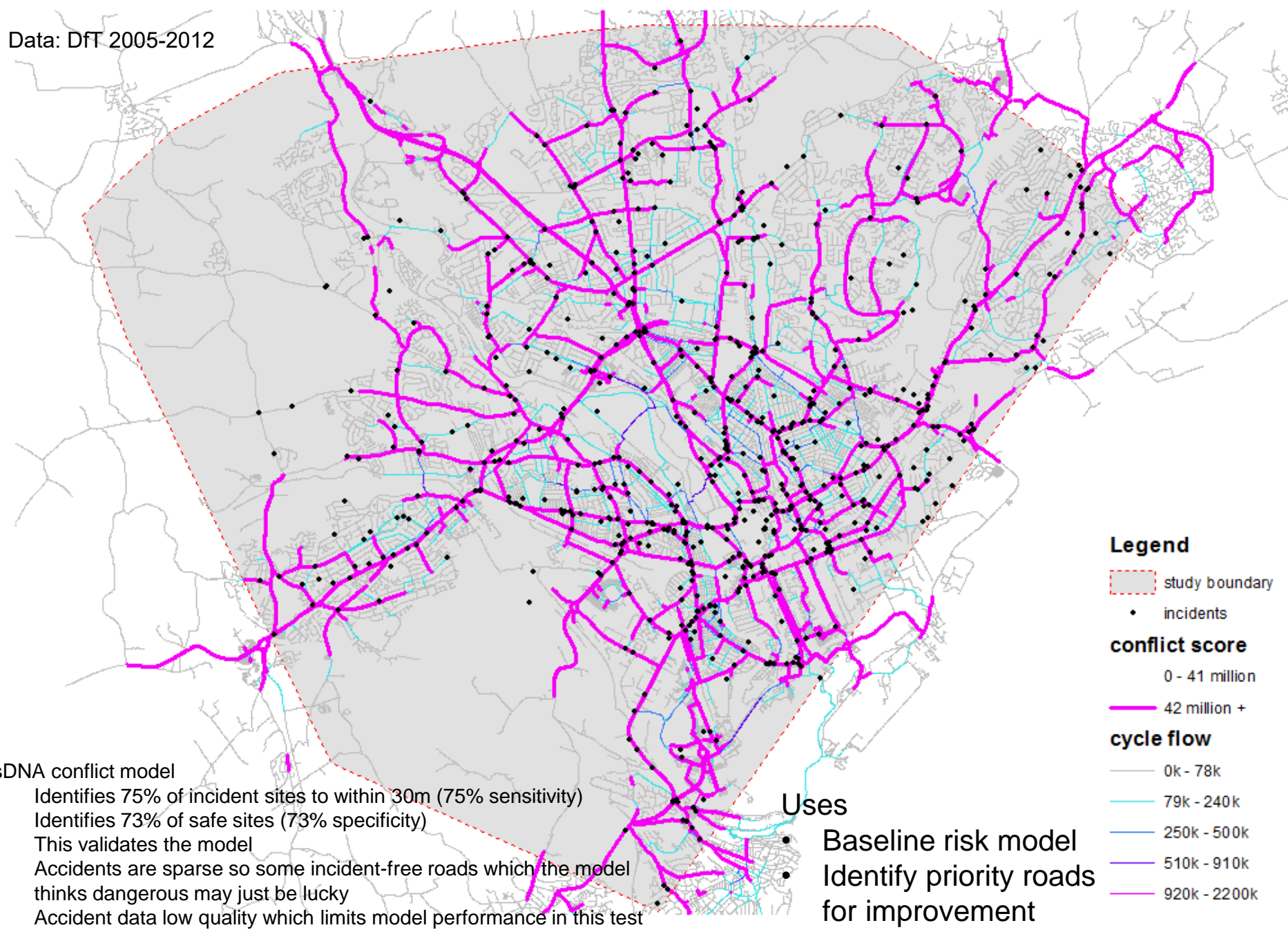






Mid length cycle trips using Taff Trail under A48

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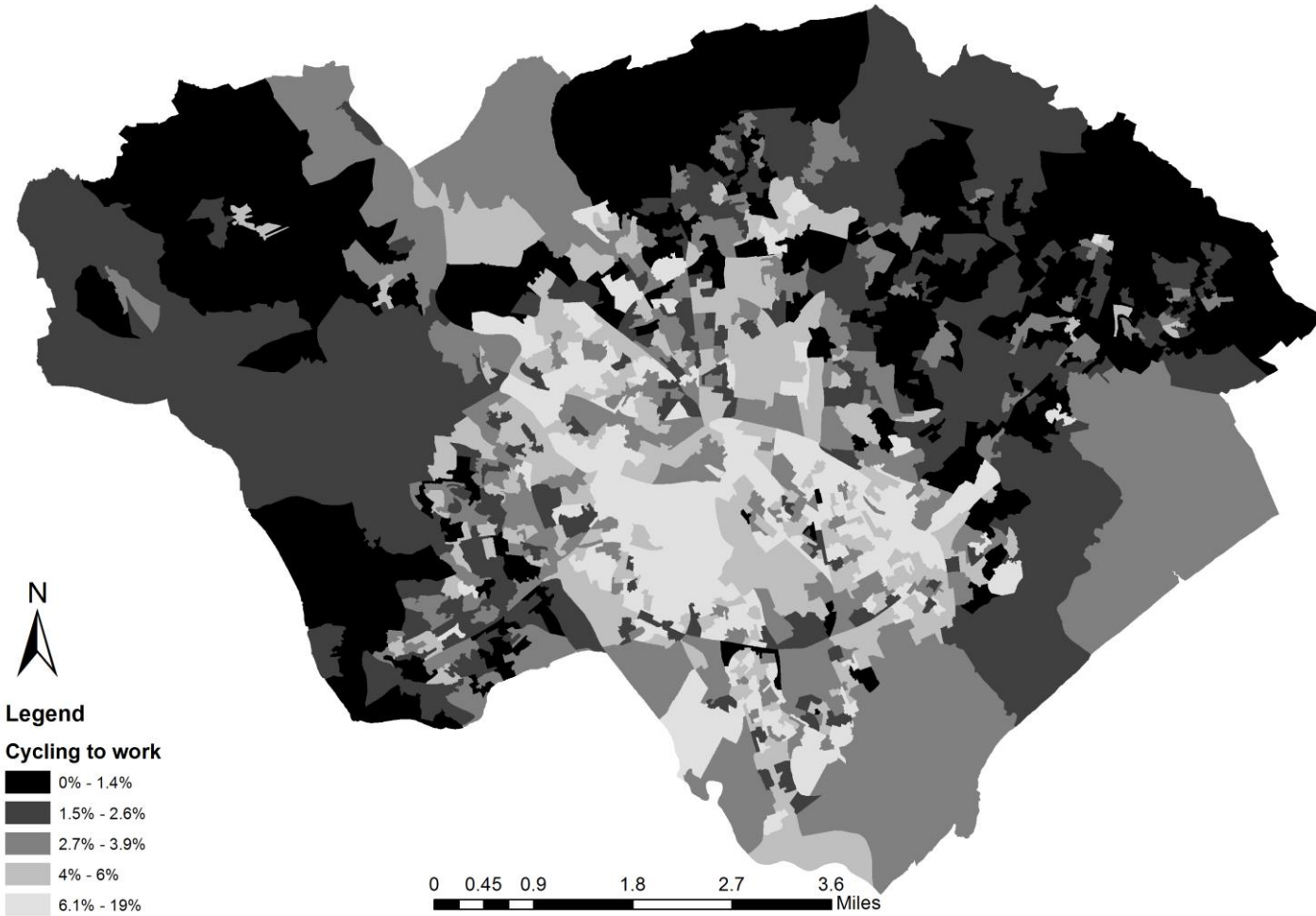


sDNA conflict model

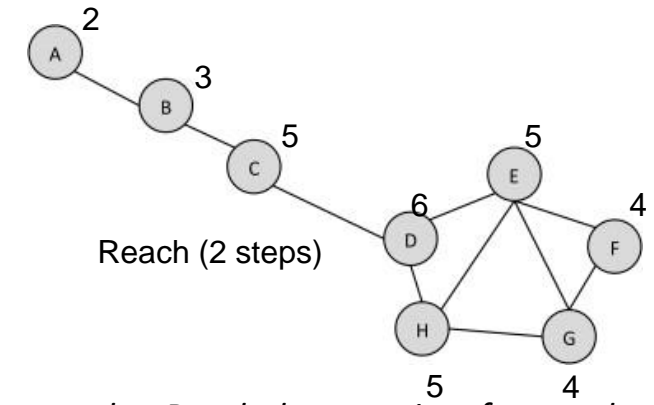
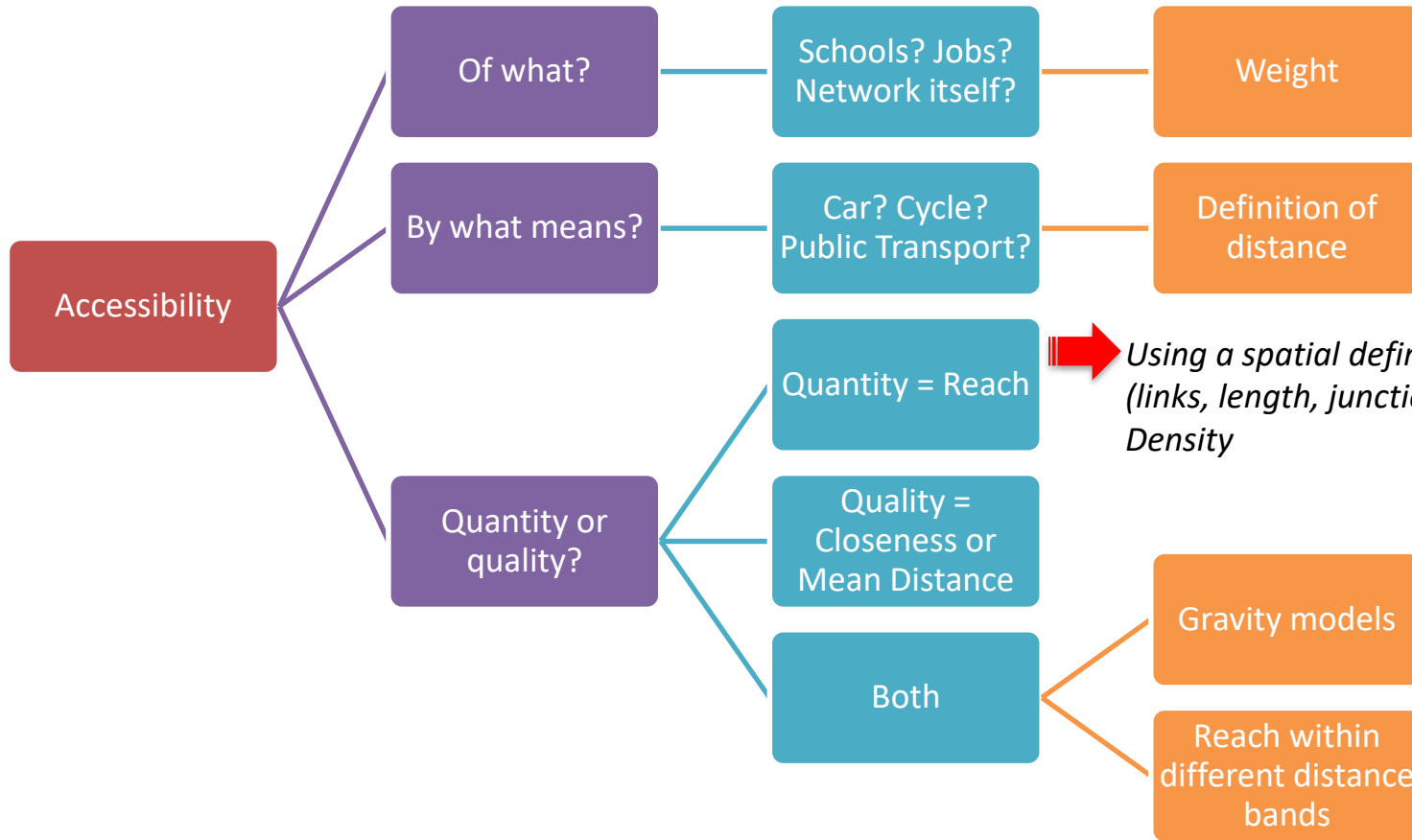
- Identifies 75% of incident sites to within 30m (75% sensitivity)
- Identifies 73% of safe sites (73% specificity)
- This validates the model
- Accidents are sparse so some incident-free roads which the model thinks dangerous may just be lucky
- Accident data low quality which limits model performance in this test

Uses

- Baseline risk model
- Identify priority roads for improvement



Measuring Accessibility

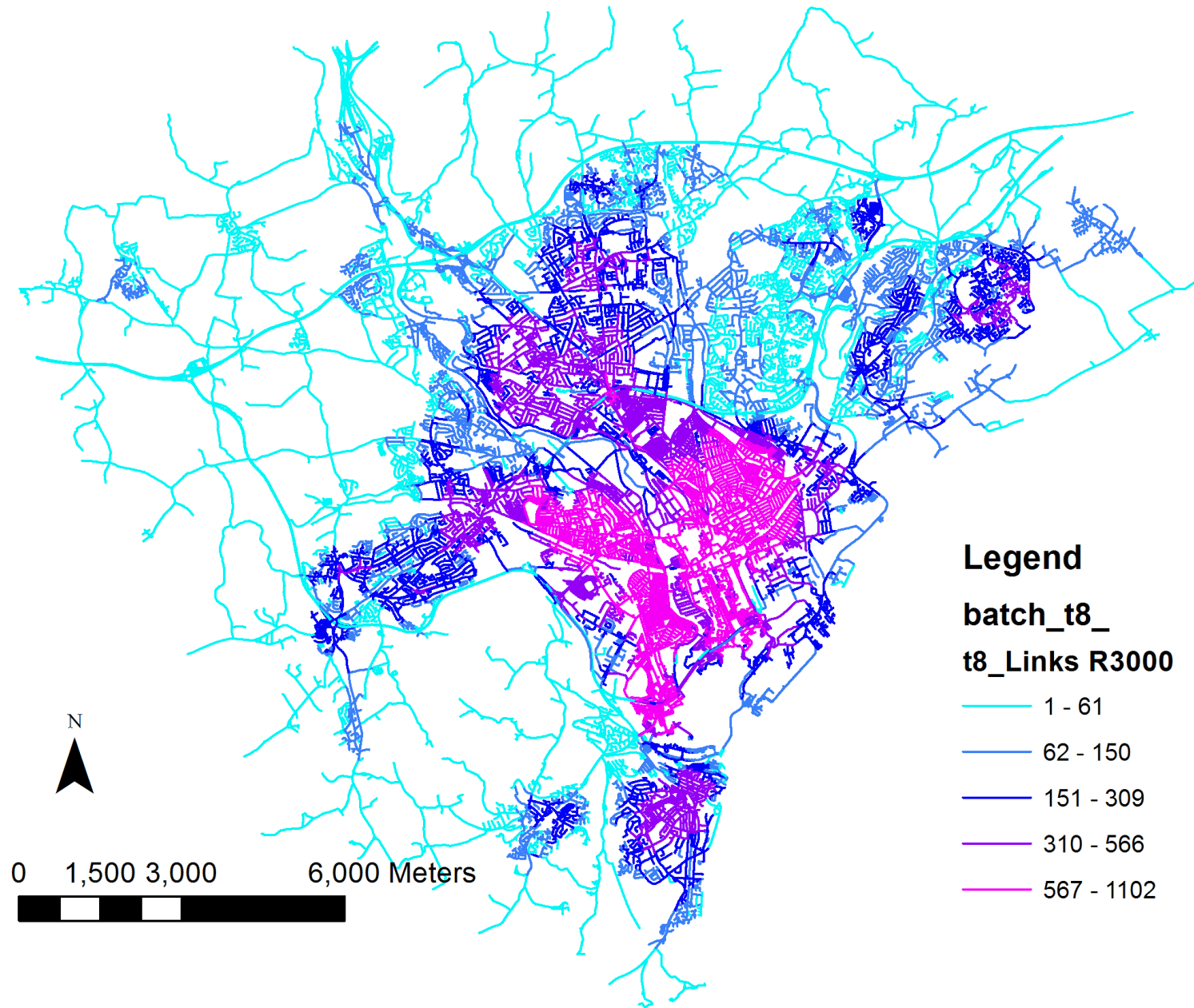


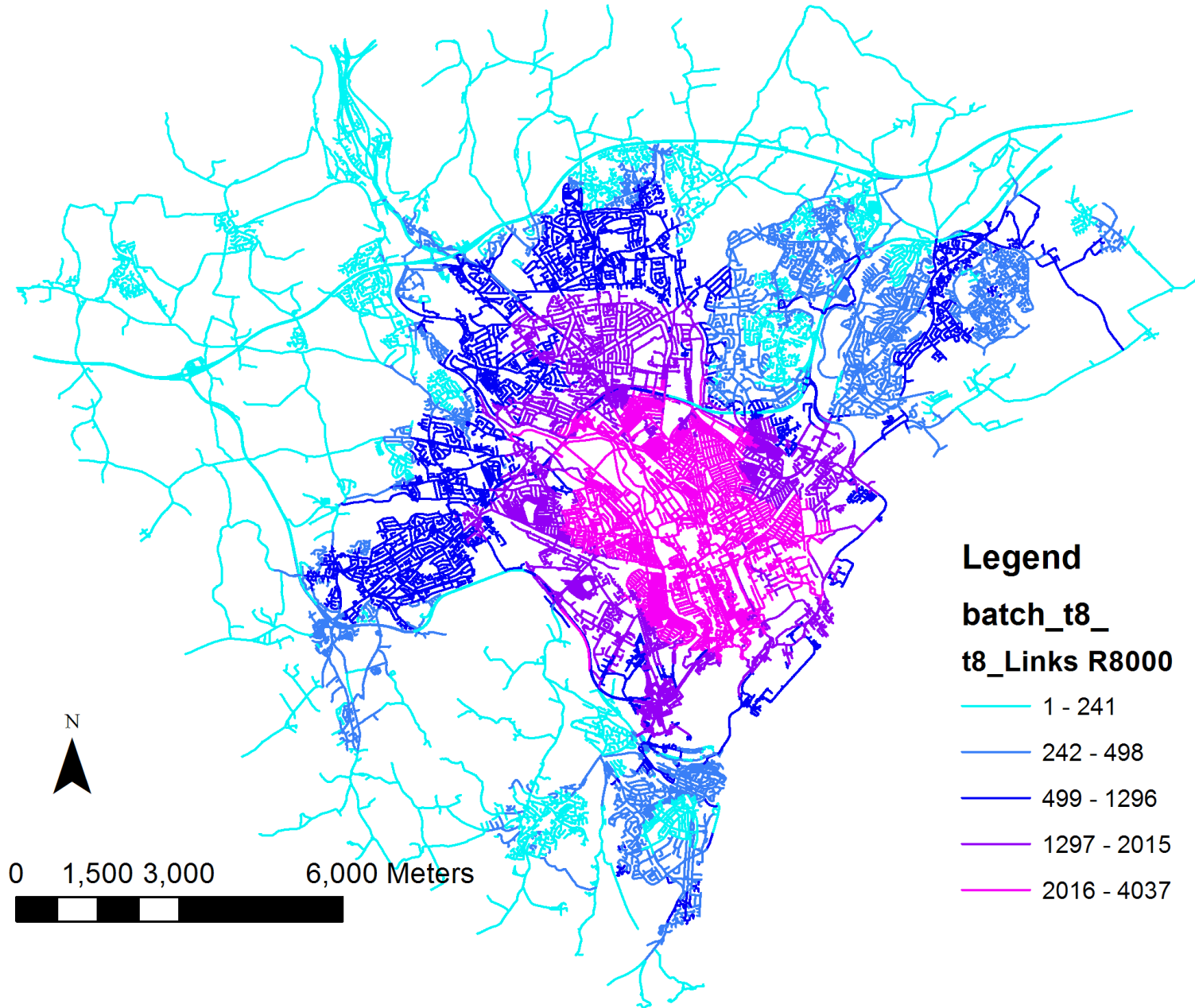
Using a spatial definition of distance makes Reach the quantity of network (links, length, junctions, custom weight) within spatial locality - aka Density

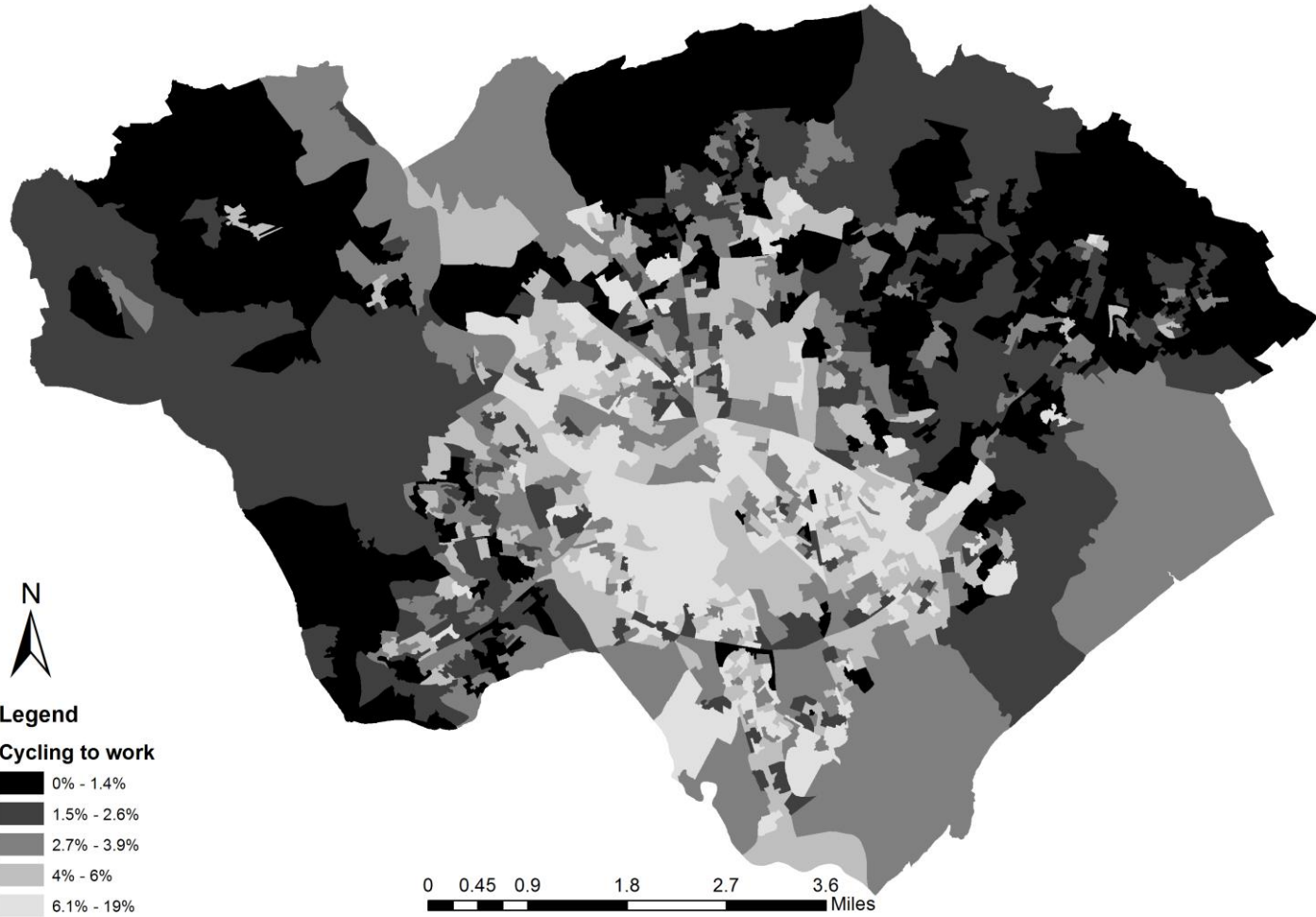
$$\frac{reach^a}{f(\text{mean distance})}, \text{ typically } \frac{reach^a}{\text{mean distance}^b}$$

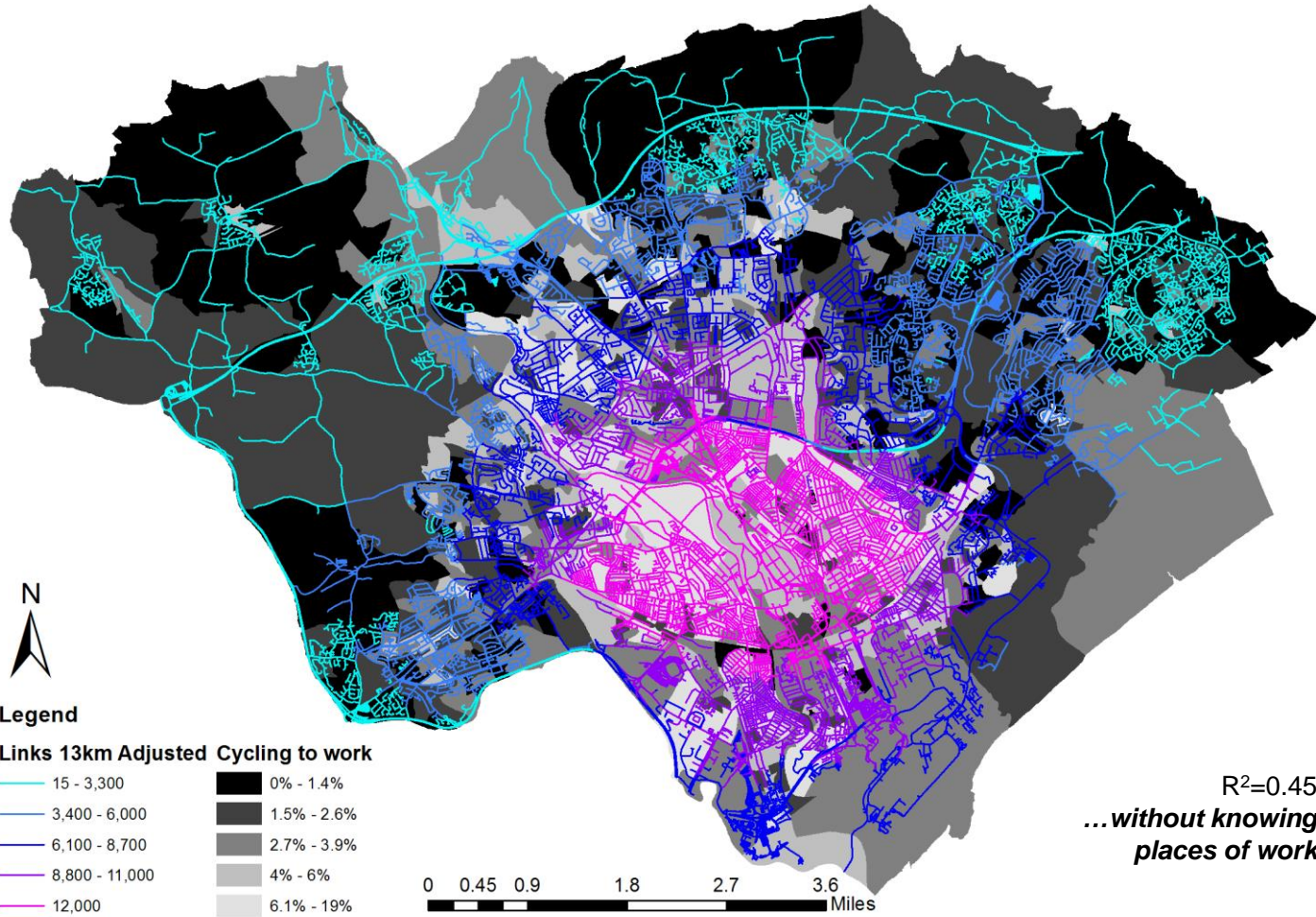
$$\beta_0 reach_{\{0-2km\}} + \beta_1 reach_{\{2-4km\}} + \dots$$

(parametric calibration of gravity curve)



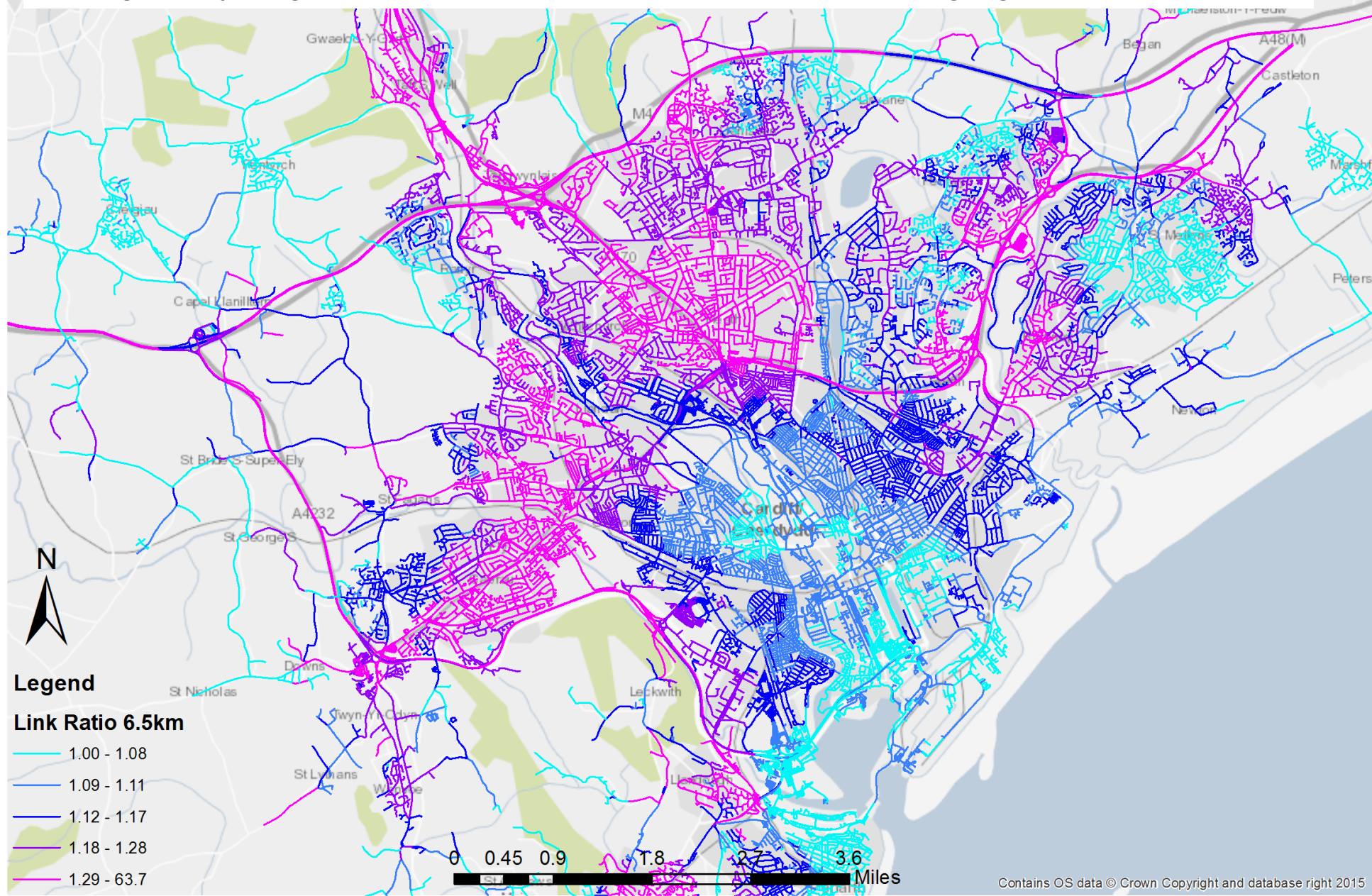




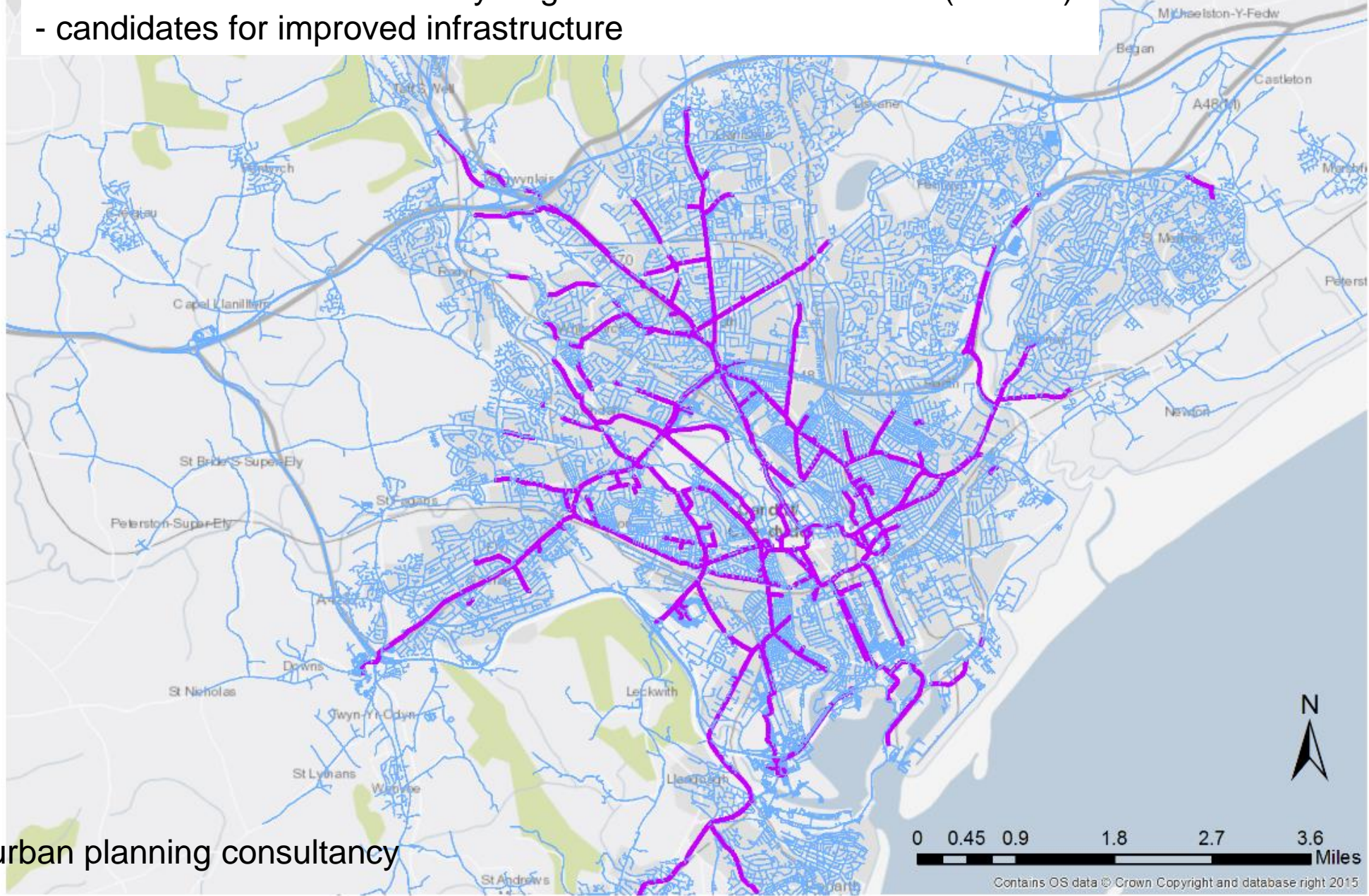


$R^2=0.45$
*...without knowing
 places of work*

Change in cycling to work if we remove vehicles / provide segregated infrastructure



Roads that would see more cycling under no-traffic scenario (outliers)
- candidates for improved infrastructure



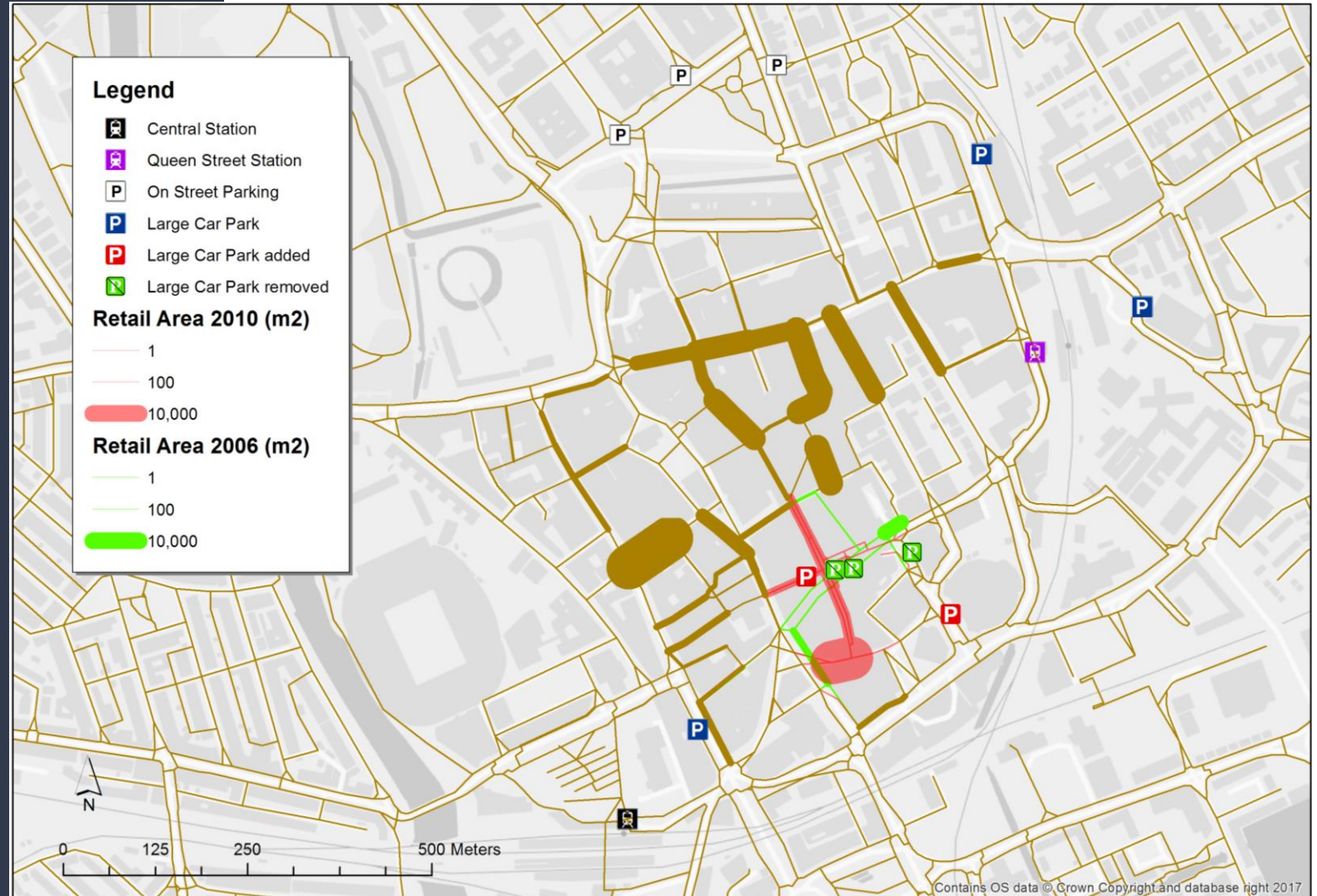
Uses: Arup urban planning consultancy

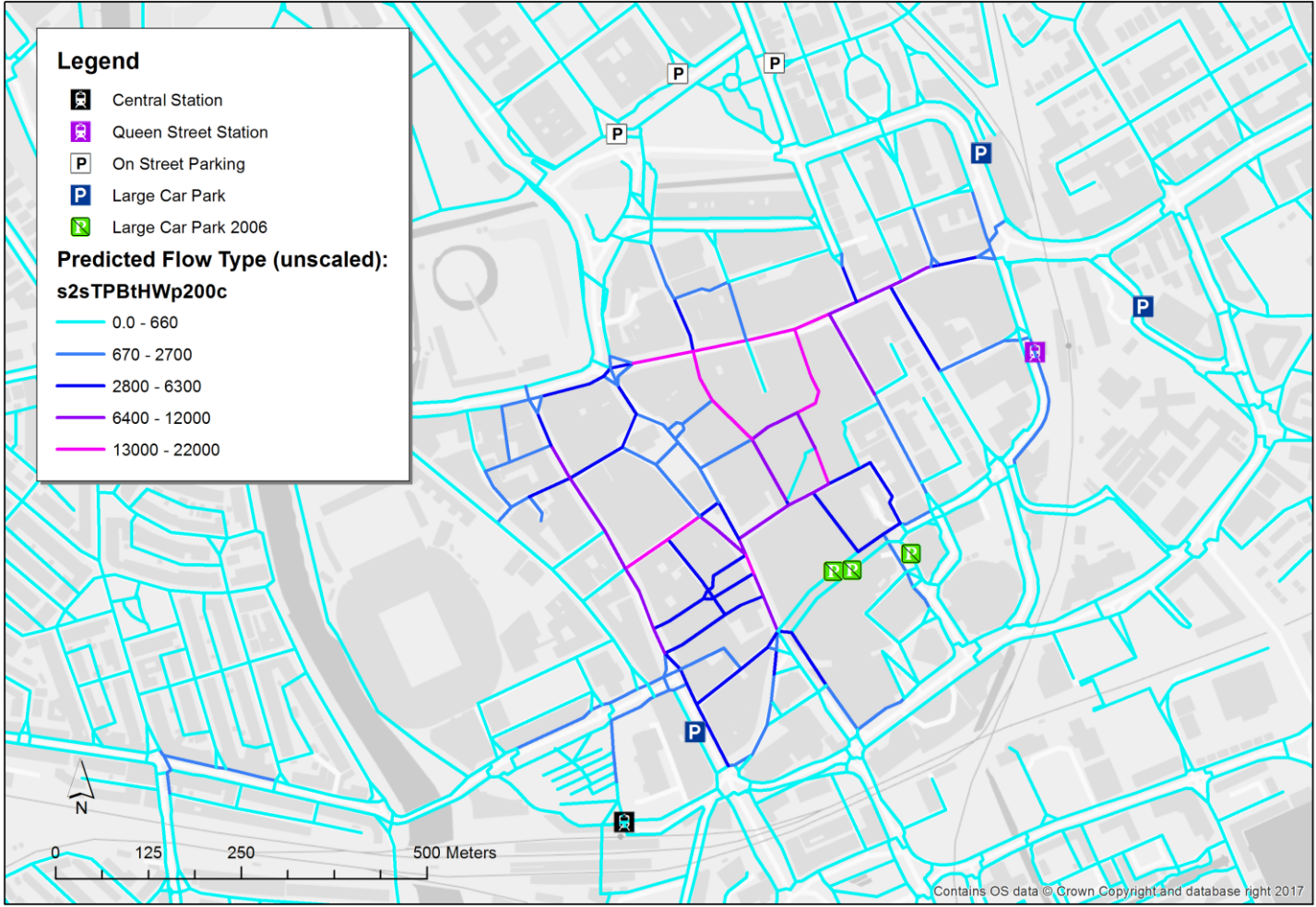
Cardiff model of walking

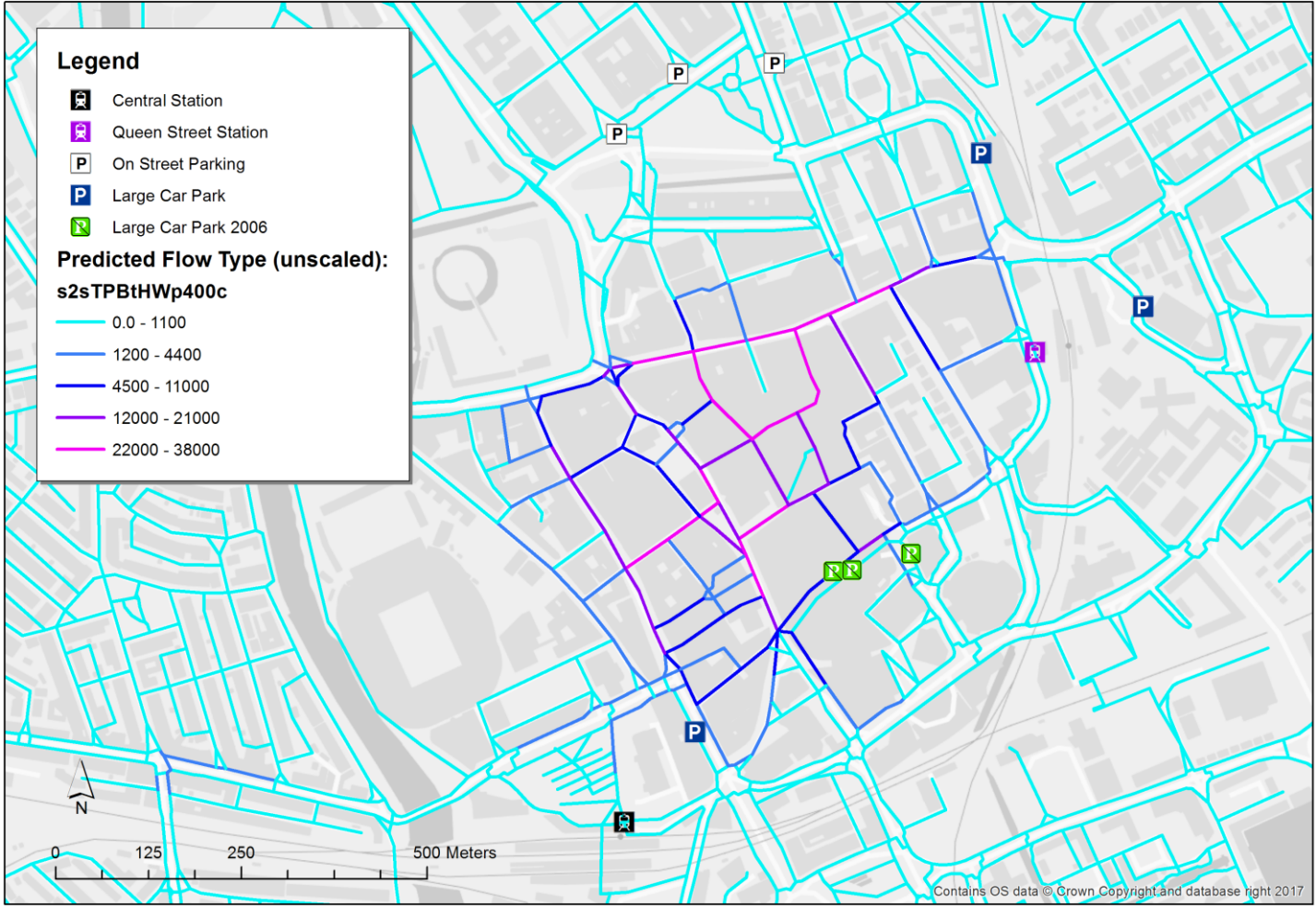
Longitudinal test against Cardiff data

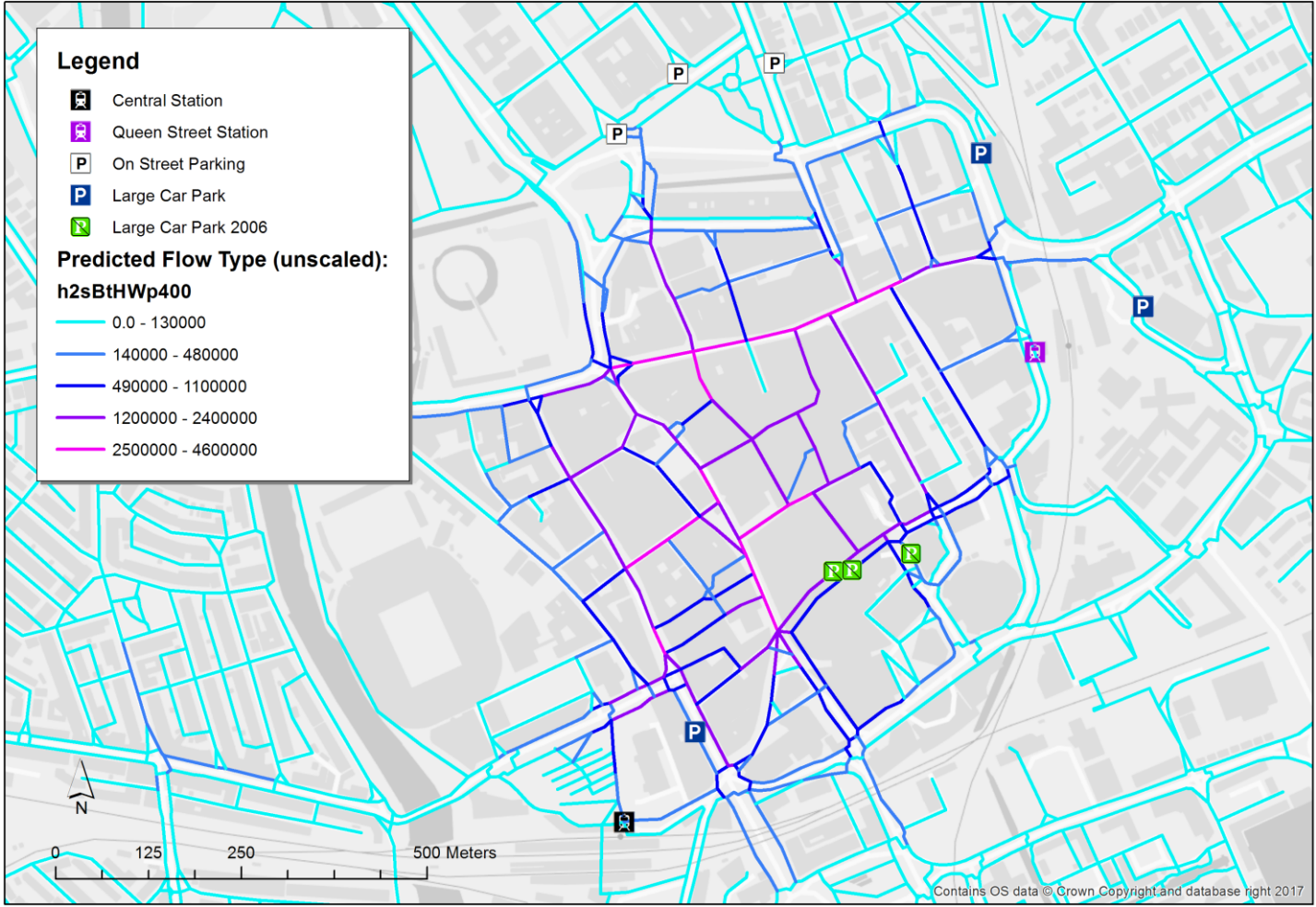
Major city centre redevelopment
2007-2010

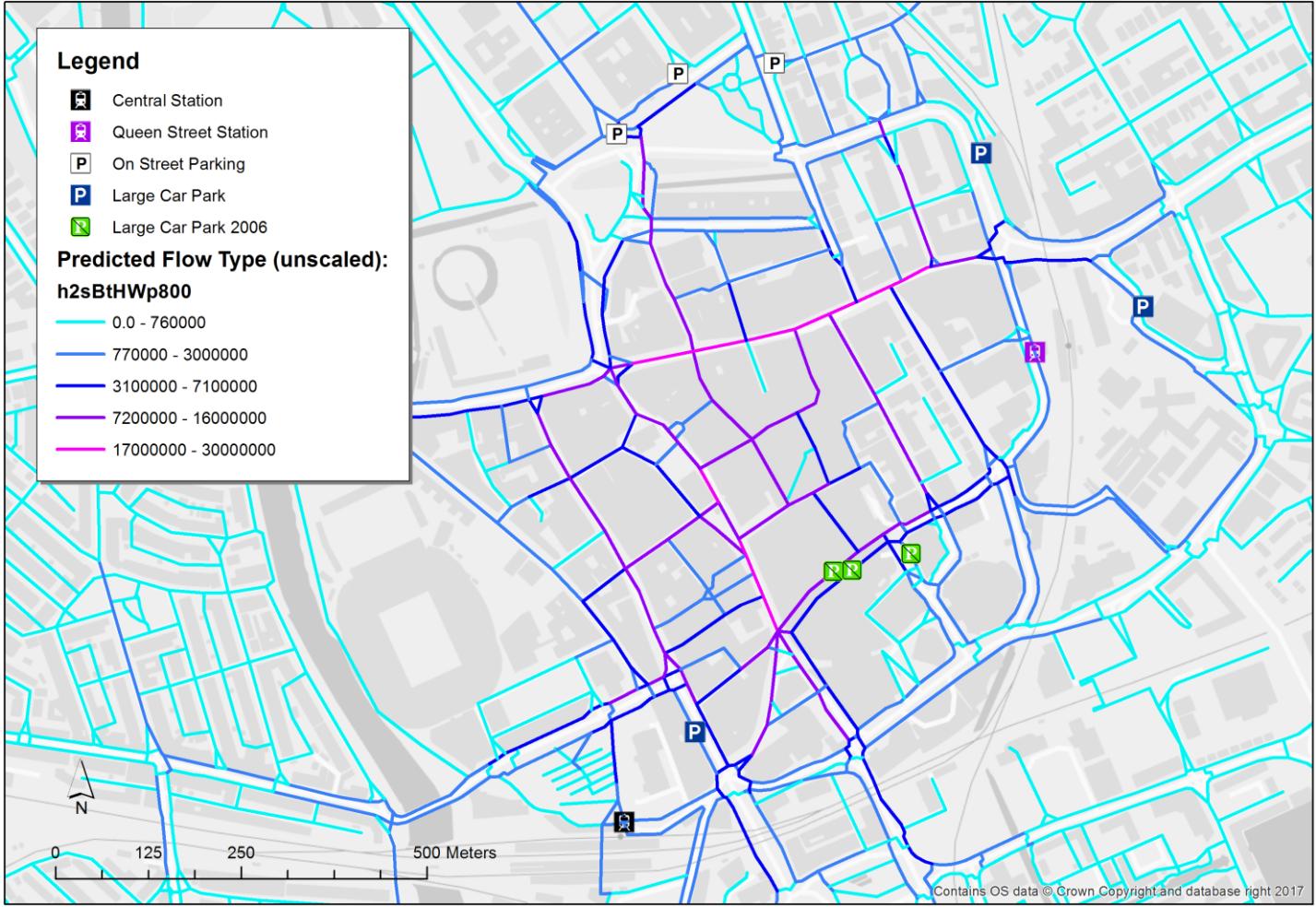
Data Innovation Institute seedcorn project
with
Ian Harvey
Scott Orford
Alain Chiaradia

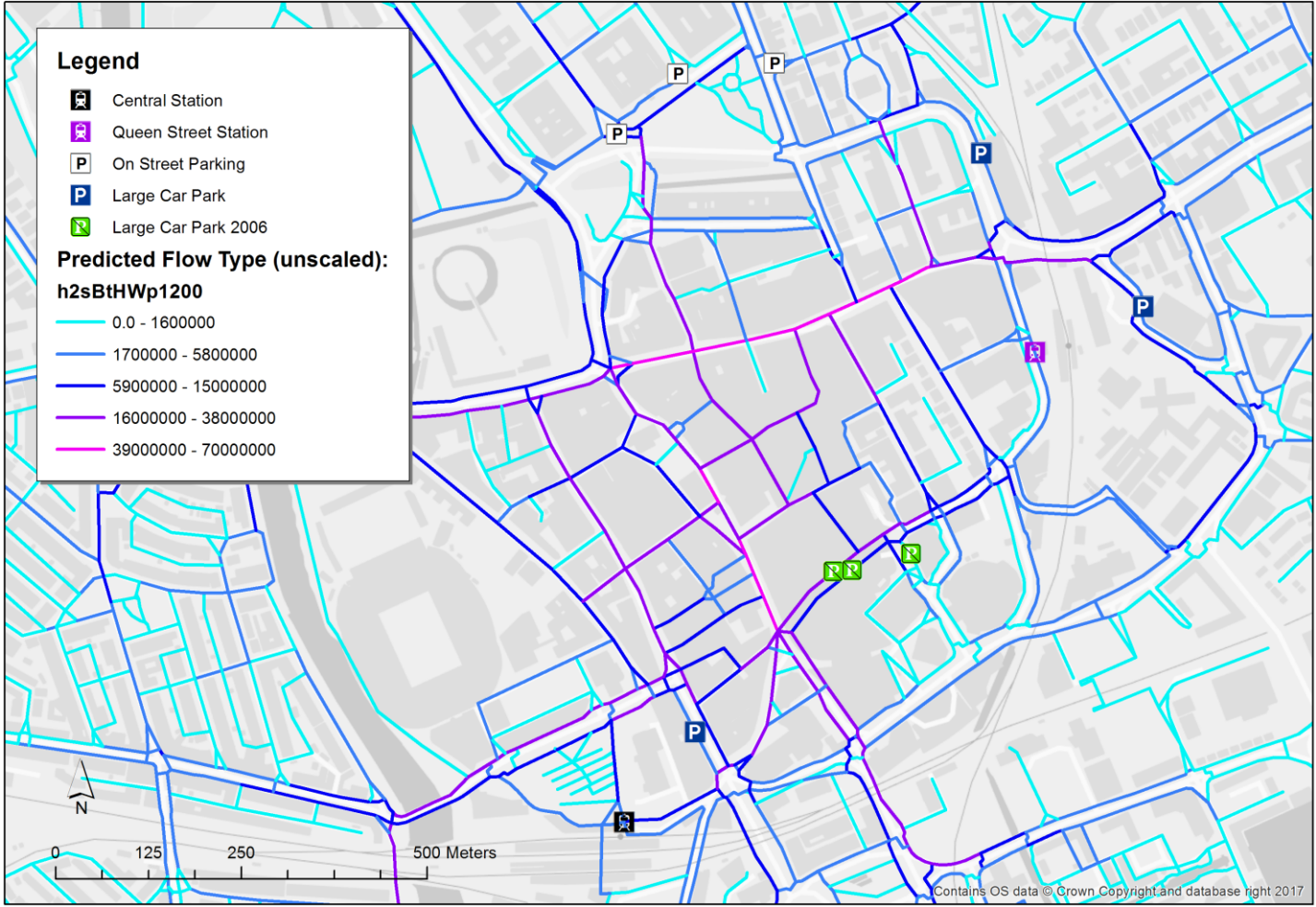


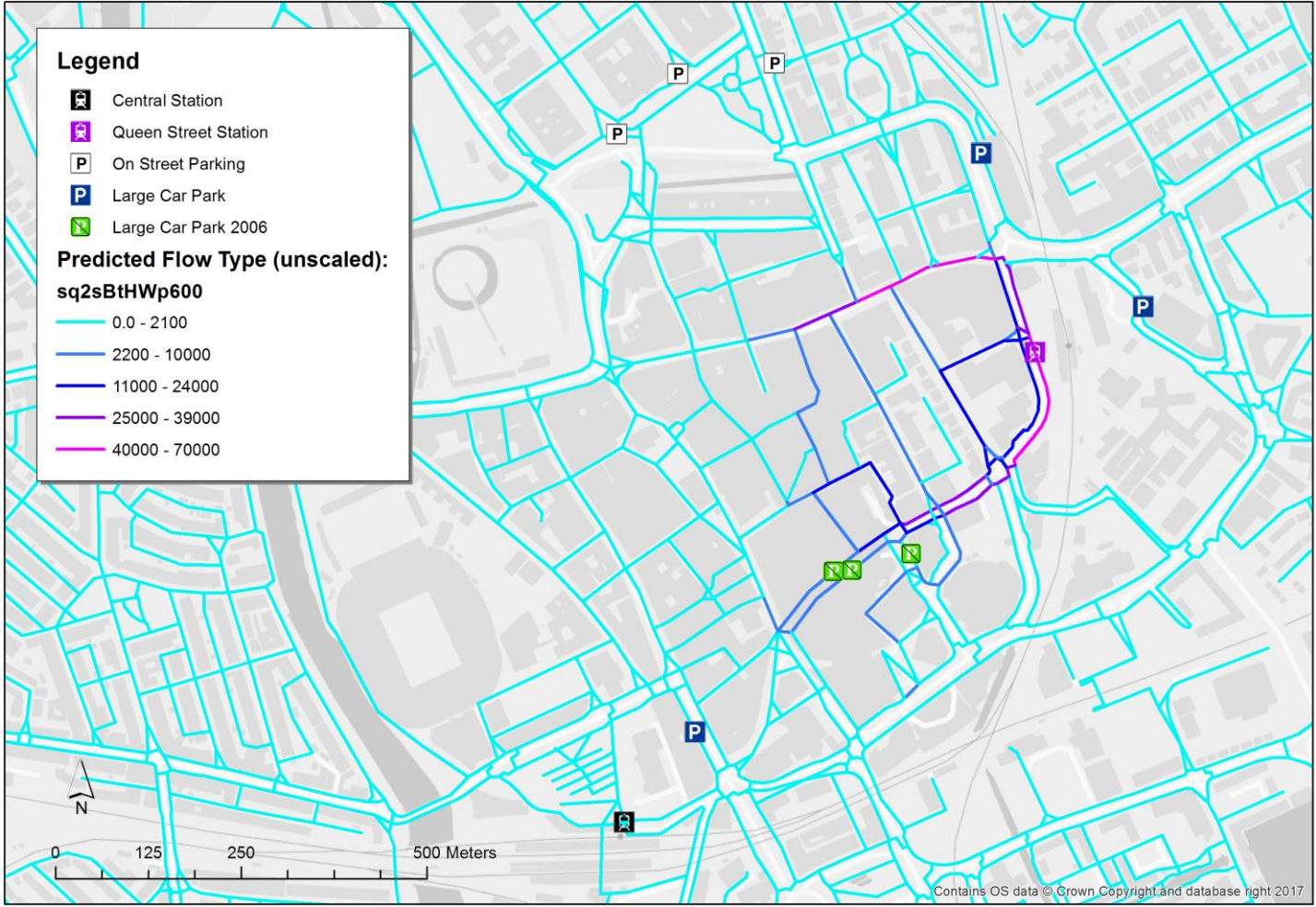


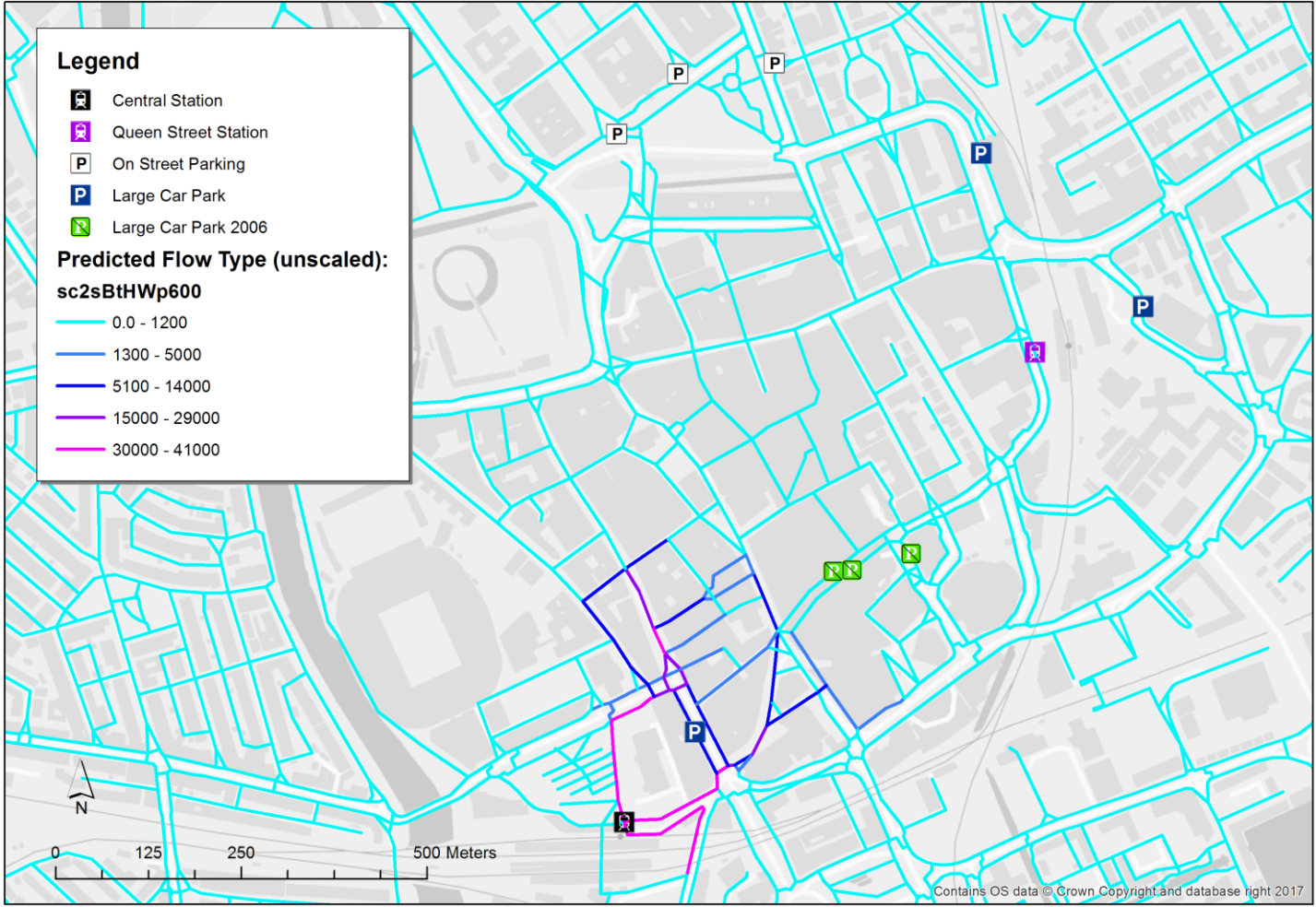


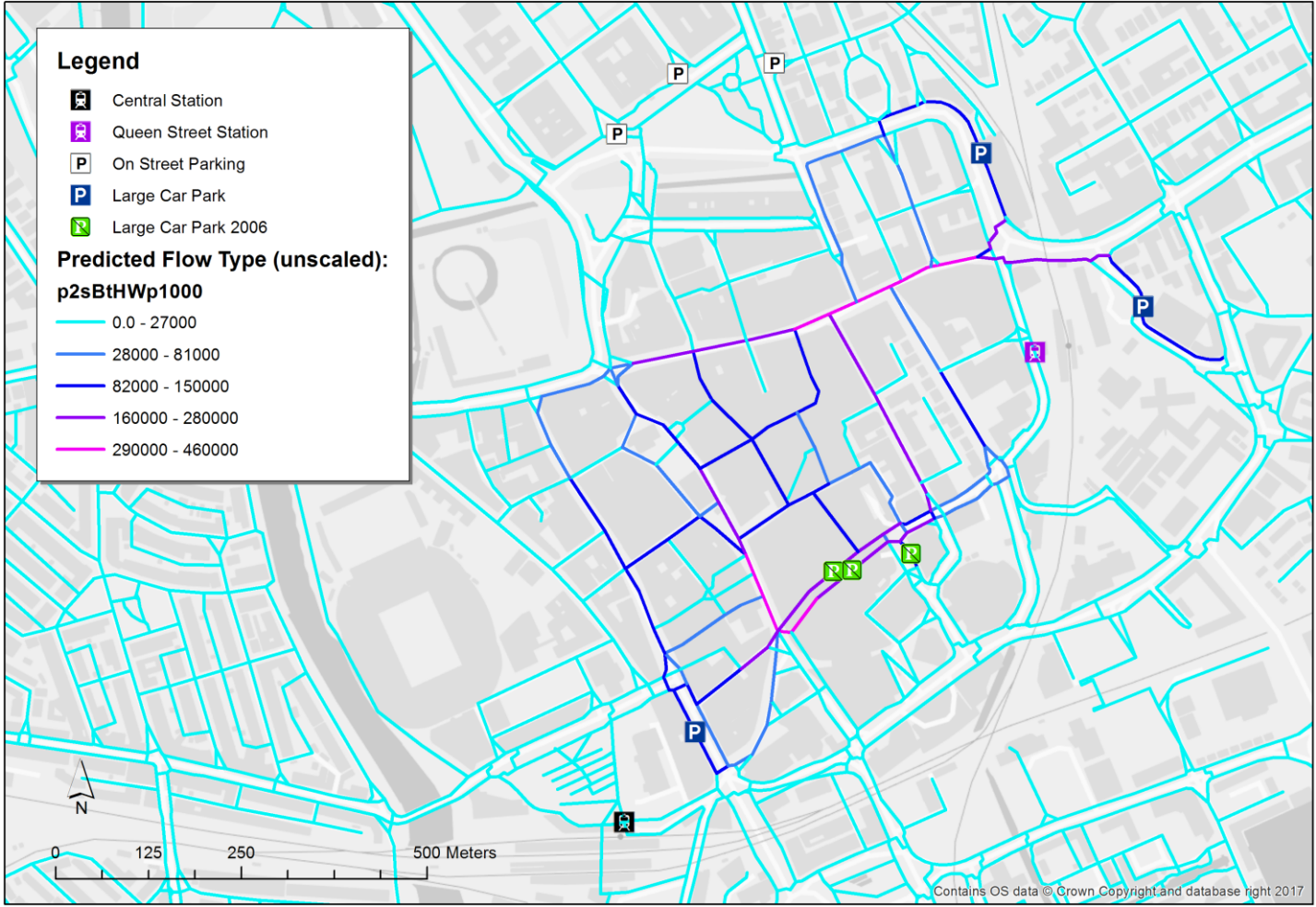


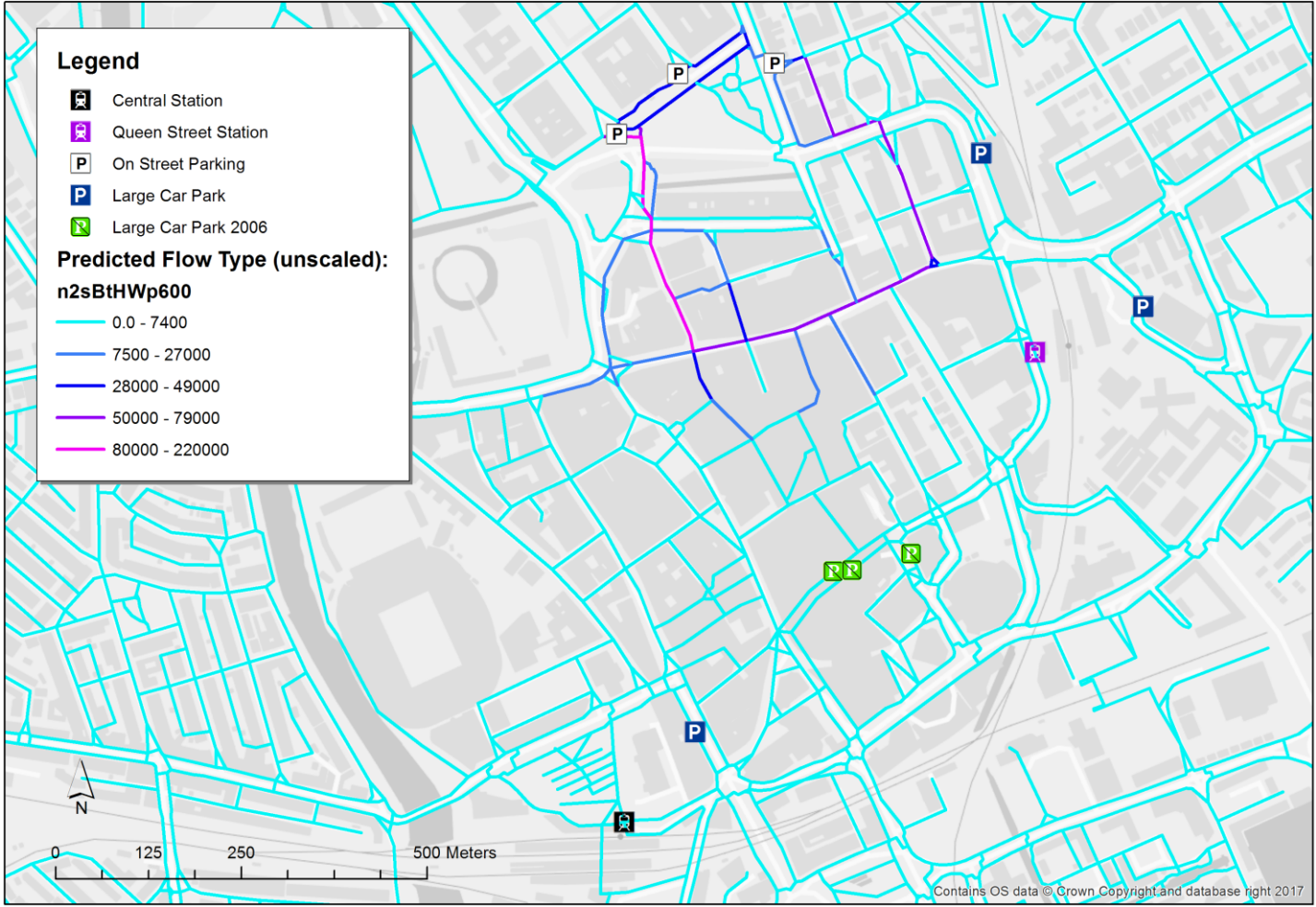


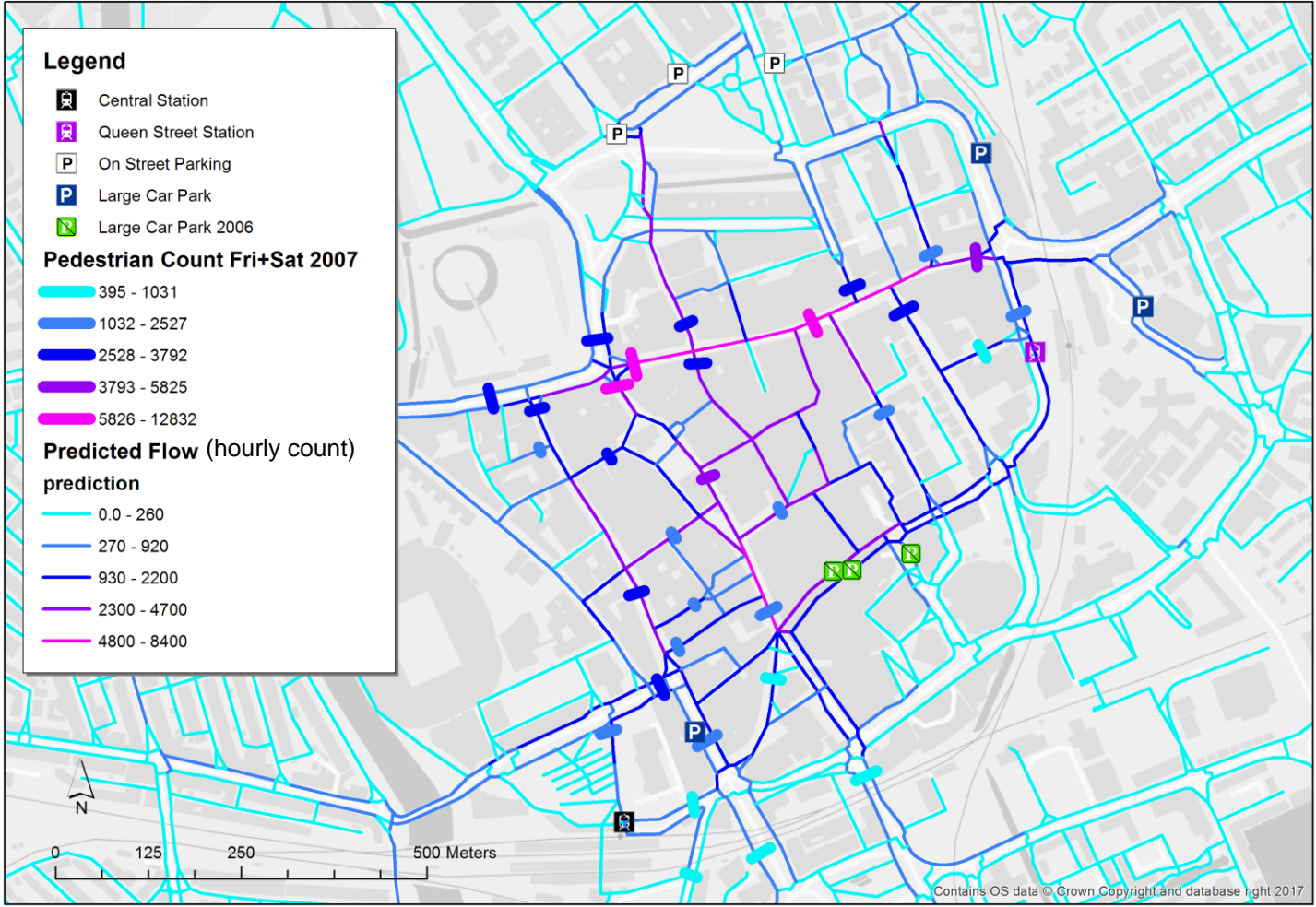






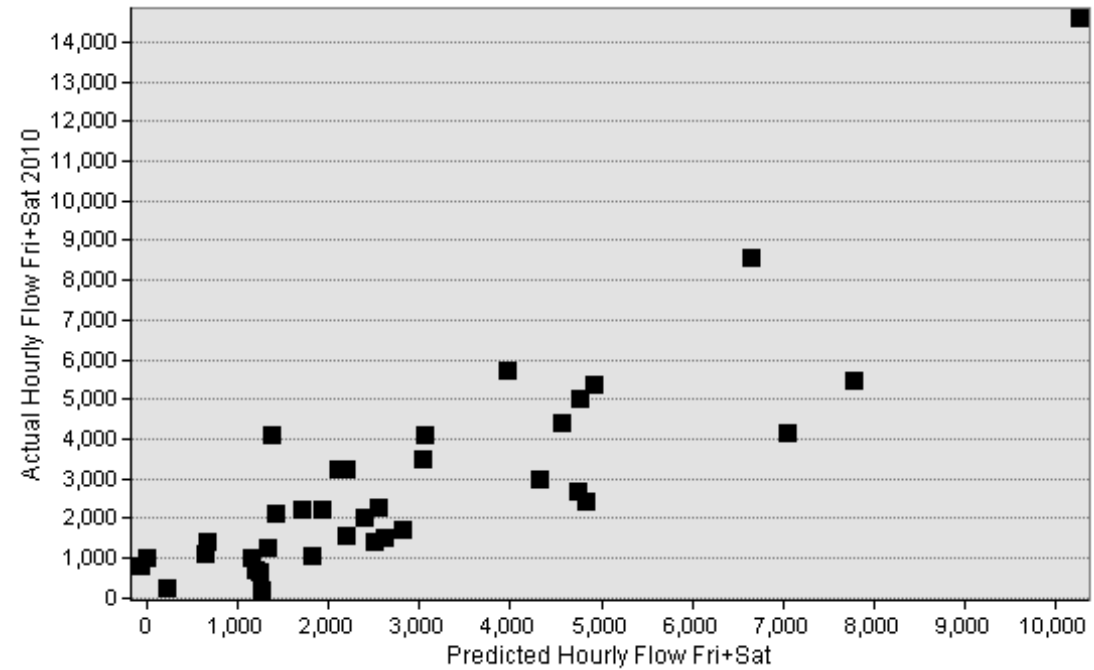






Predictive performance

To our knowledge the first time a pedestrian model has been tested in its ability to predict longitudinal change



Year	Null model r2	Incremental model r2	Direct model r2
2008	0.79	n/a	n/a
2009	0.85	n/a	n/a
2010	0.81	0.84	0.72
2011	0.63	0.73	0.45

Users: Arup, Wedderburn, Alan Baxter, Hong Kong, Shanghai, Transport for London

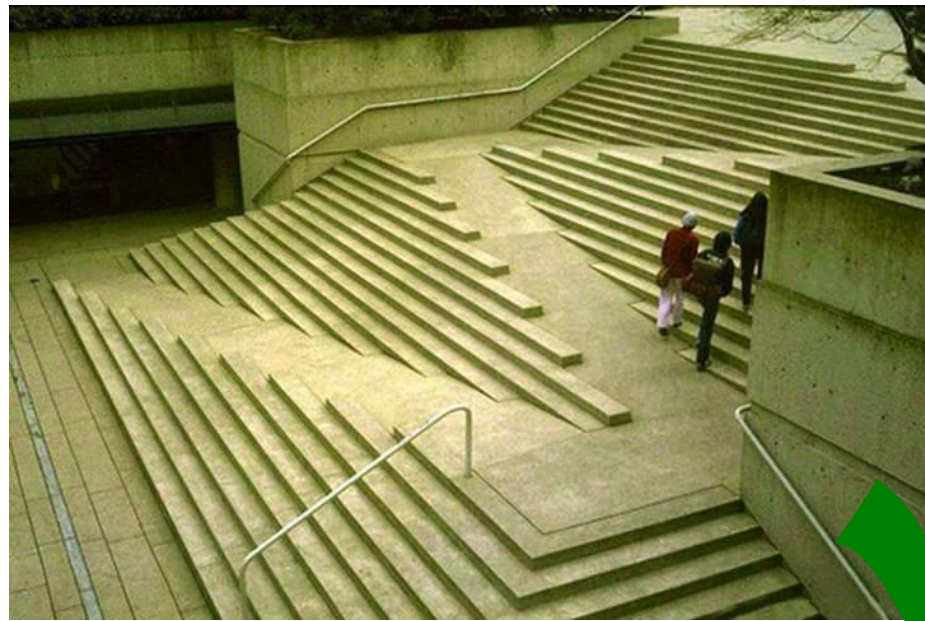
Cardiff City Region: Limited mobilities model

Richard Price MSc Dissertation

No test against data

Mapping severance for people unable to climb steps

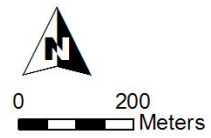
Enabled by audit of infrastructure under Wales Active Travel Act (2014)



Example: Abercynon

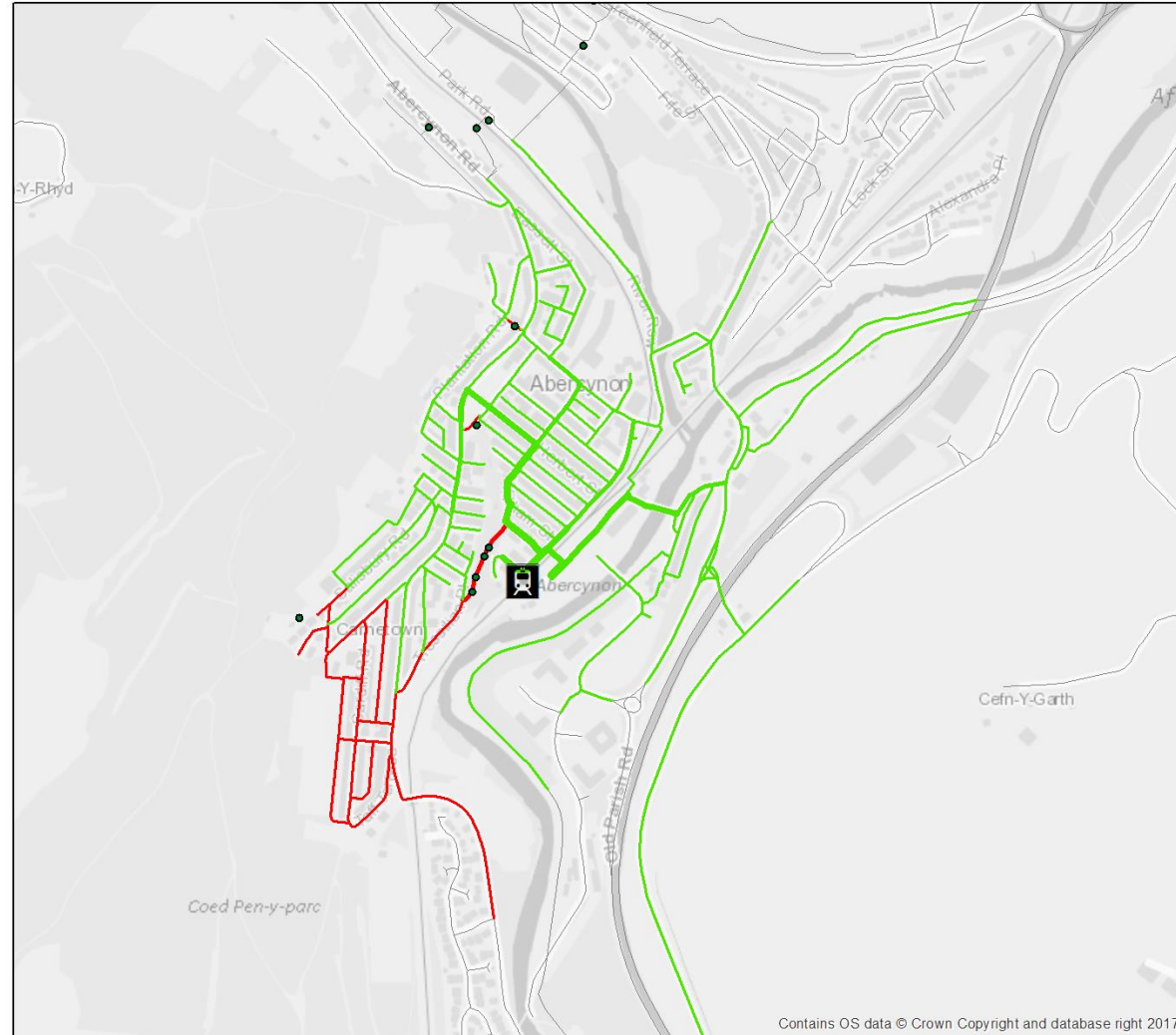
Stepped route provides essential shortcut to south, which cannot otherwise be reached within 800m

Step free route takes detour to north



Legend

- Steps
- Rail Stations
- 800m accessible to all
- 800m accessible via steps



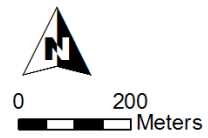
Pilot project – not for planning use

Example: Crymlyn

Stepped route provides essential shortcut to north, which cannot otherwise be reached within 800m

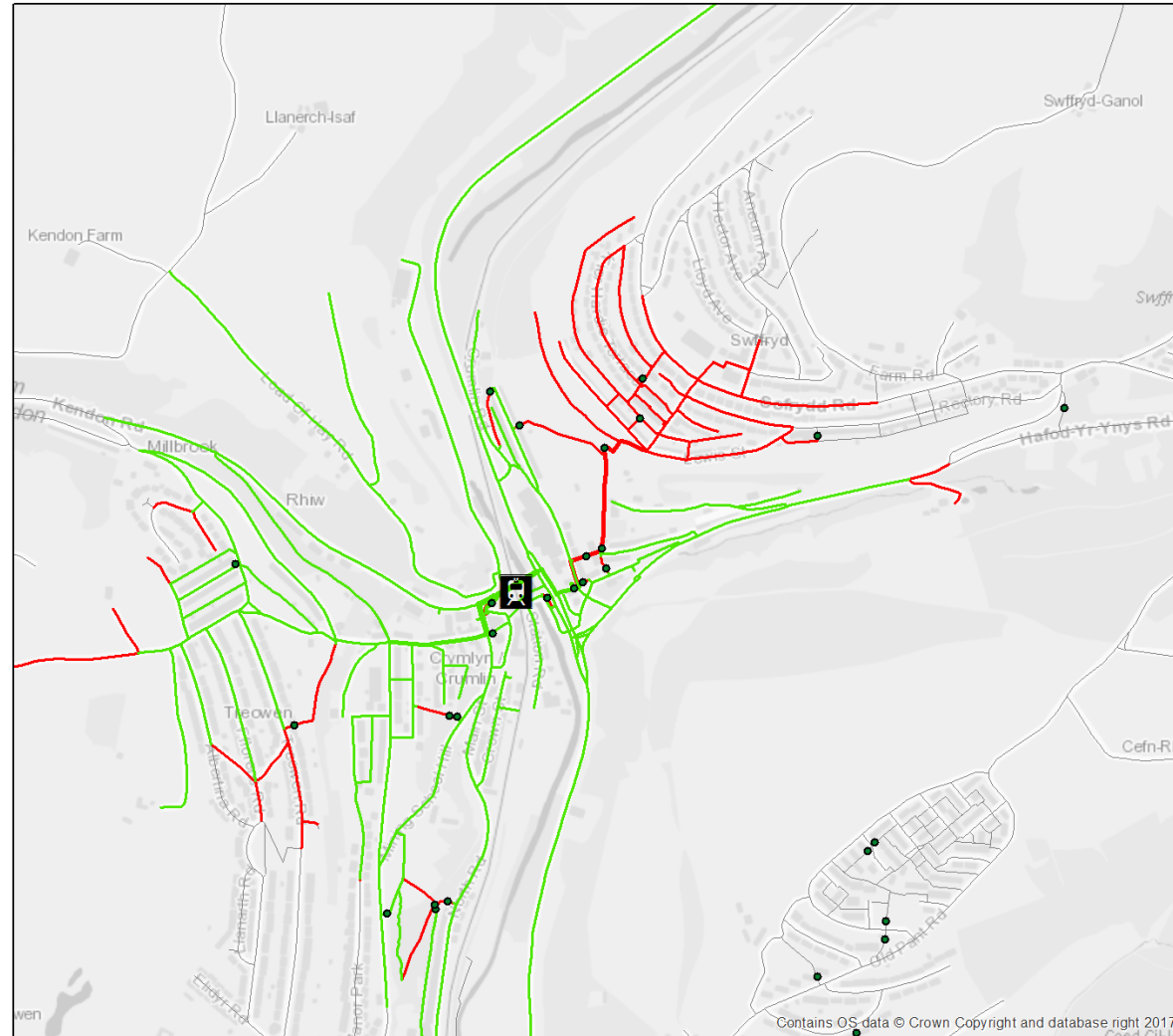
Step free route takes long detour to east

Possibly unavoidable due to topography of valley



Legend

- Steps
-  Rail Stations
- 800m accessible to all 
- 800m accessible via steps 

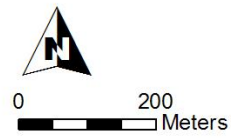


Pilot project – not for planning use

Example: New Tredegar

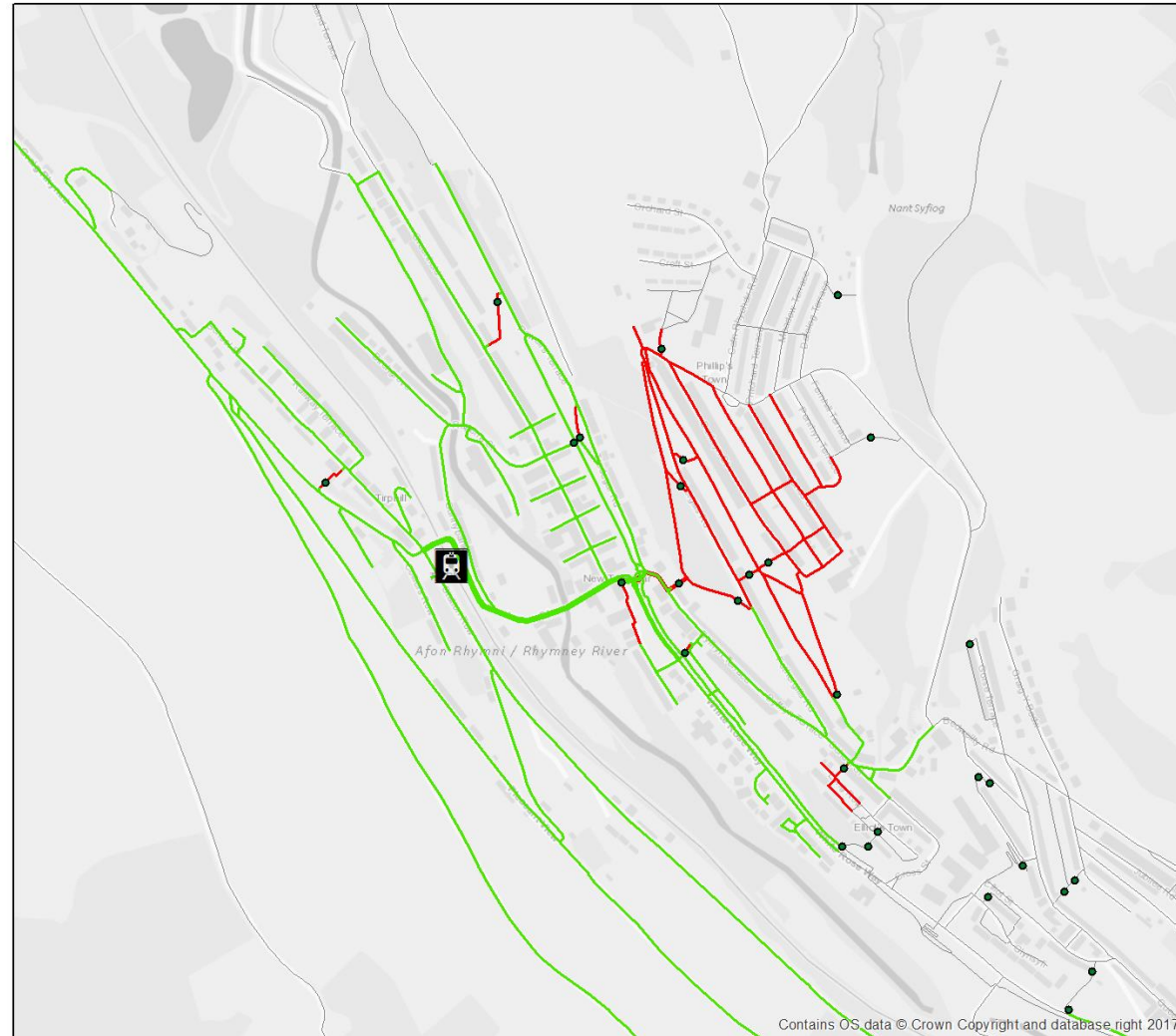
Stepped route provides essential shortcut to east, which cannot otherwise be reached within 800m

Step free route takes detour to south



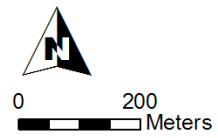
Legend

- Steps
-  Rail Stations
- 800m accessible to all 
- 800m accessible via steps 



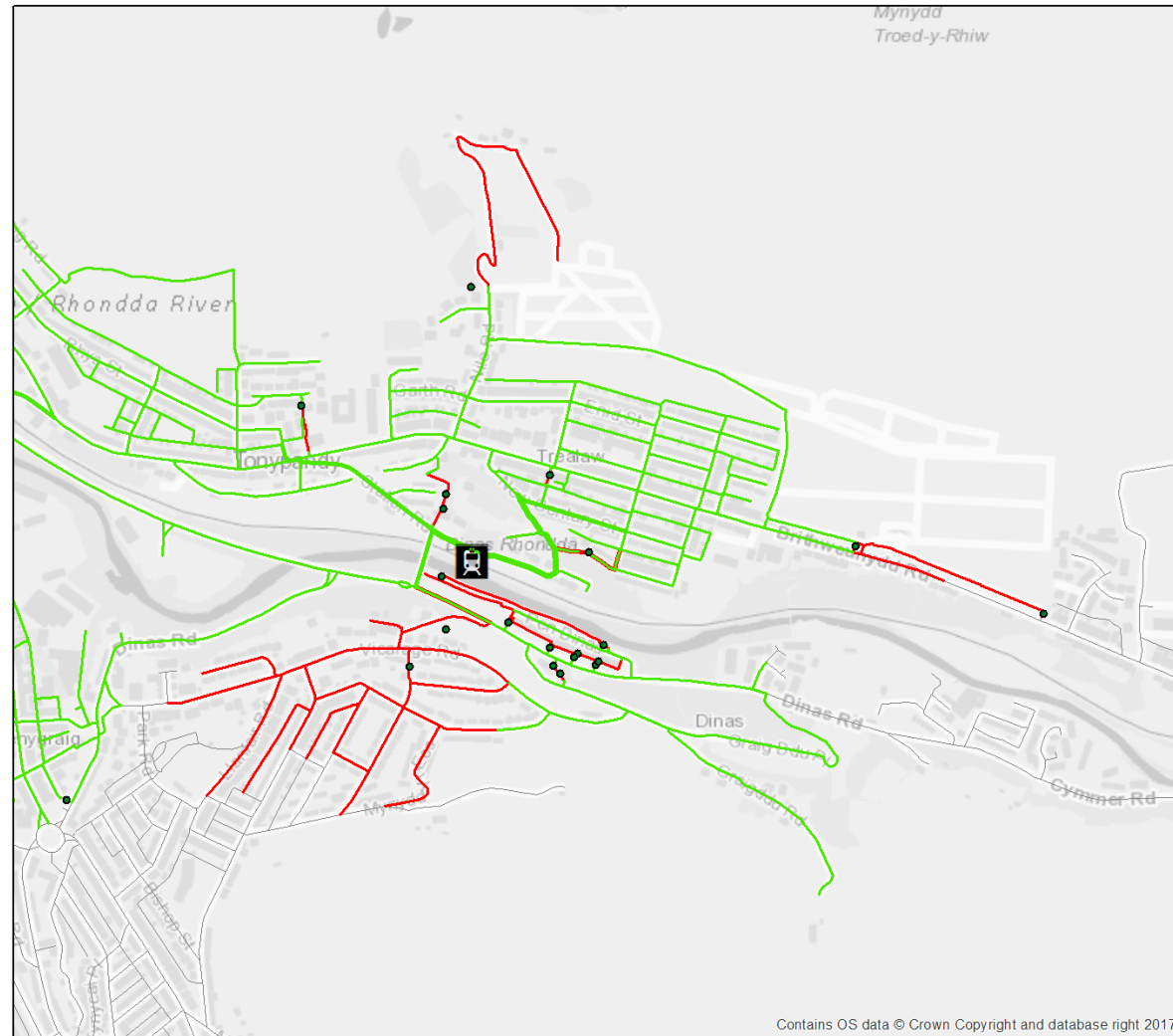
Example: Tonypandy

Stepped route provides essential shortcut to south, which cannot otherwise be reached within 800m



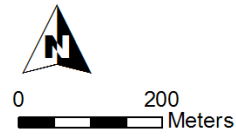
Legend

- Steps
- Rail Stations
- 800m accessible to all
- 800m accessible via steps




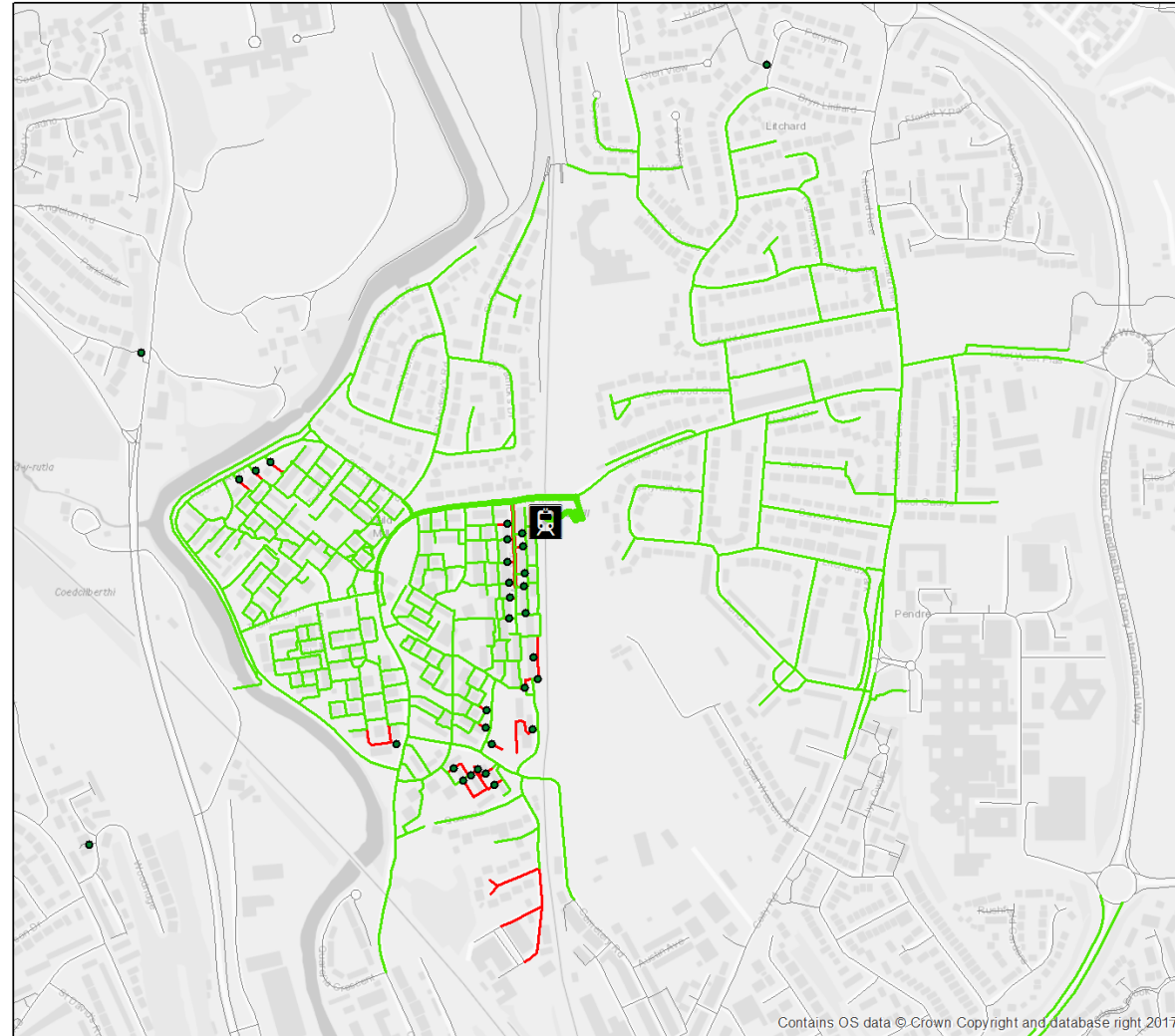
Example:
Wildmill (Bridgend)

High incidence of steps near station, but none are on essential route so impact is small



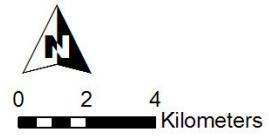
Legend

- Steps
-  Rail Stations
- 800m accessible to all 
- 800m accessible via steps 



Pilot project – not for planning use

Potential most inhibited by steps
(800m trip length)

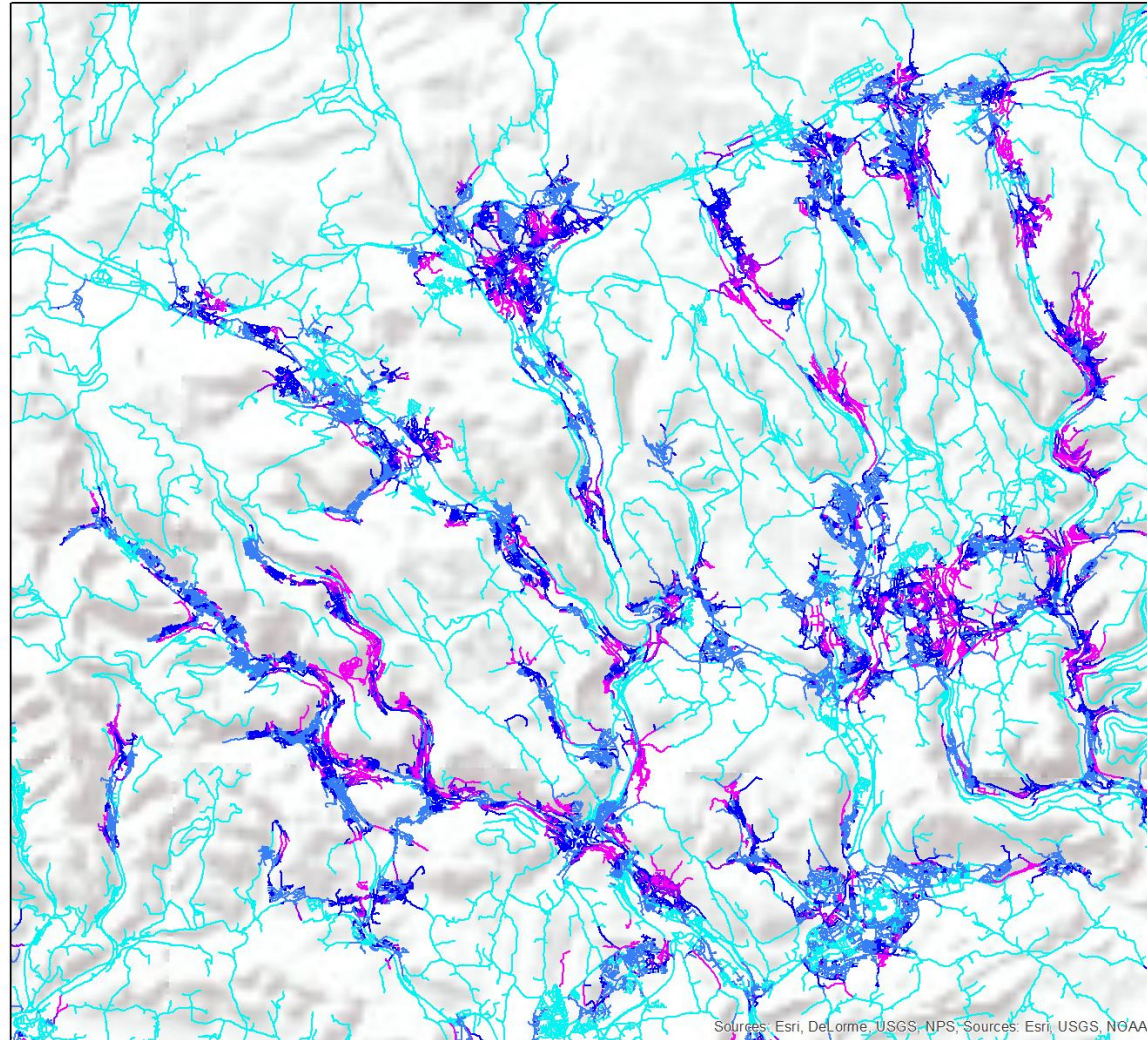


Legend

(No) steps accessibility ratio 800m

- 0.00 - 0.79
- 0.80 - 0.86
- 0.87 - 0.94
- 0.95 - 0.99
- 1.00

Worse
Better
Best



Sources: Esri, DeLorme, USGS, NPS, Sources: Esri, USGS, NOAA

Pilot project – not for planning use

Spatially explicit measures: Convex Hull

- Spatial locality has shape, and that shape has a convex hull
 - Area
 - Perimeter
 - Shape index
 - Bearing
 - Maximum radius



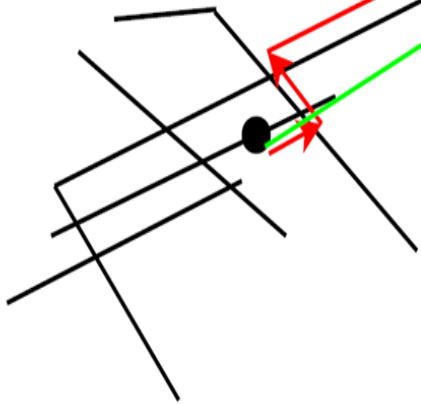
Convex Hull link to Community Cohesion

Convex Hull Maximum Radius 600m
A measure of network directness for pedestrians

Furthest point reachable within network radius from origin

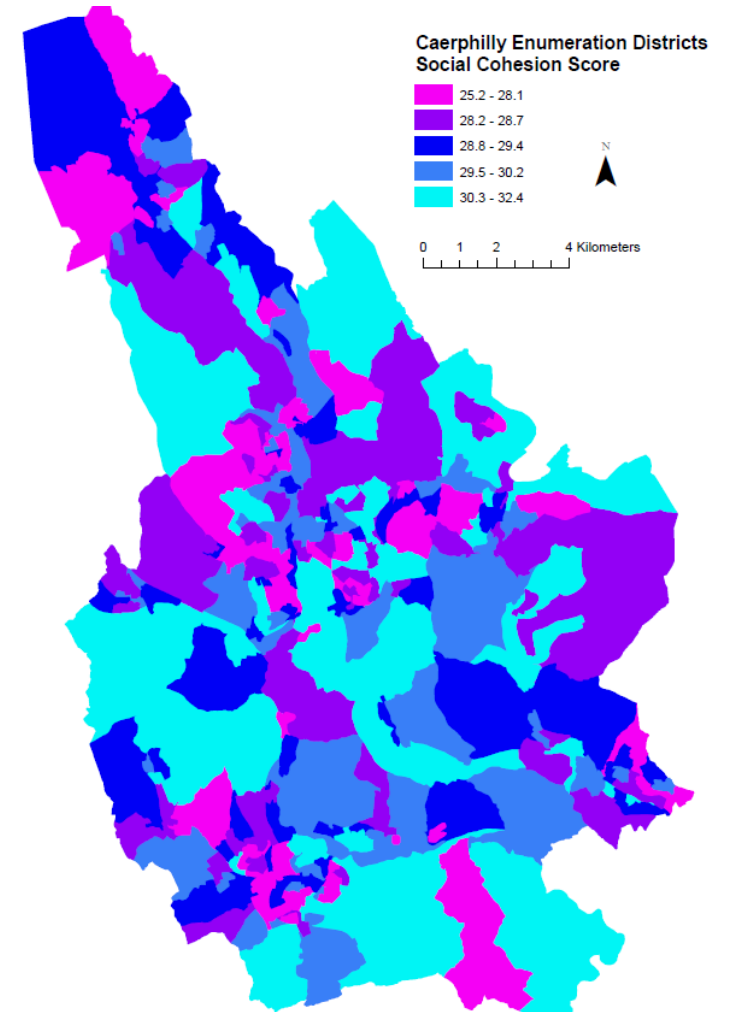
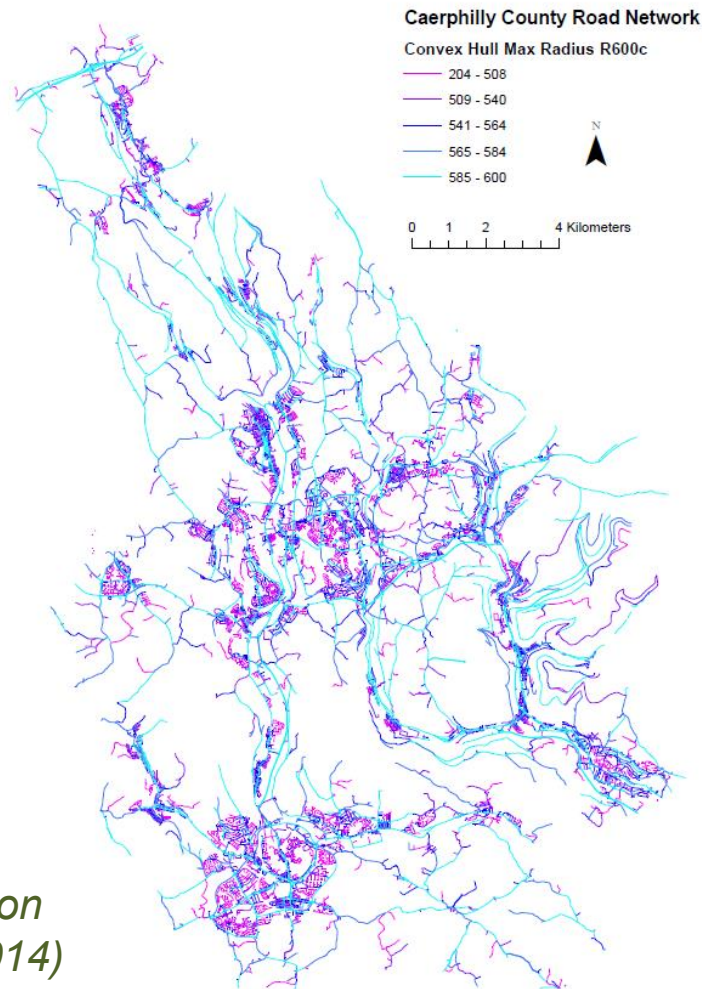
Network radius = 600m

HullR: Distance as crow flies $\leq 600m$



“the furthest you can get (as the crow flies) from your point of origin, by walking 600m (taking obstacles into account)”

Explained 10% of variance in community cohesion in 2 different studies (Cooper Fone Chiaradia 2014)



Network links to health

C. Sarkar, J. Gallacher, C. Webster, Morphometric analysis of the built environment in UK Biobank: Data analyses and specification manual (Jan 2014).

C. Sarkar, J. Gallacher, C. Webster, Urban built environment configuration and psychological distress in older men: Results from the Caerphilly

study, BMC Public Health 13 (1) (2013)

C. Sarkar, C. Webster, M. Pryor, D. Tang, S. Melbourne, X. Zhang, L. Jianzheng, Exploring associations between urban green, street design and walking: Results from the Greater London boroughs, Landscape and Urban Planning 143 (Supplement C) (2015) 112-125.

C. Sarkar, C. Webster, J. Gallacher, Residential greenness and prevalence of major depressive disorders: a cross-sectional, observational, associational study of 94,879 adult UK Biobank participants, The Lancet. Planetary Health 2 (4) (2018) 162-173.

C. Sarkar, C. Webster, J. Gallacher, Neighbourhood walkability and incidence of hypertension: Findings from the study of 429,334 UK Biobank participants, International Journal of Hygiene and Environmental Health 221 (3) (2018)

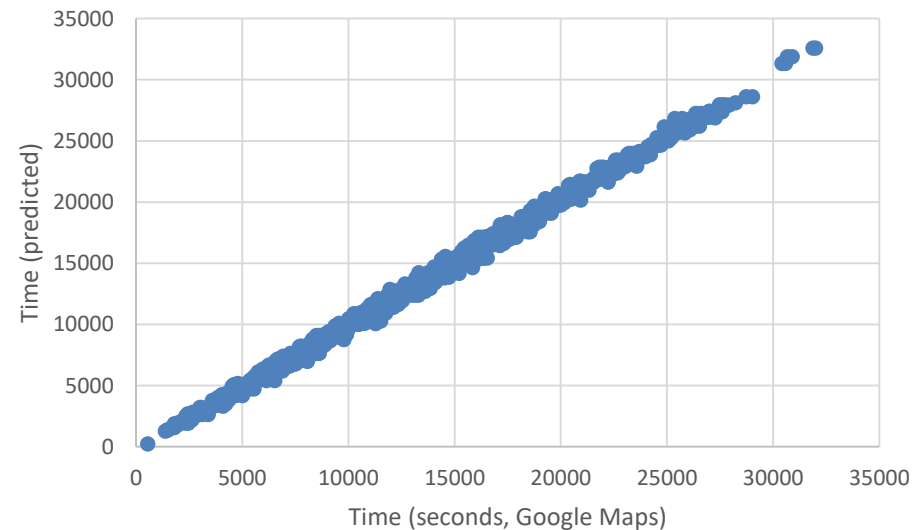


- UK Biobank: large scale epidemiology project
- sDNA quantifies built environment characteristics around 500,000 homes
- Findings on depression, hypertension, mediated by walking

Network Economic links: travel time

Modelling travel time from network alone

Feature	Estimated time (seconds)
1km network distance	32.0 (= 69.9 mph)
90 degree cumulative change of direction	7.61
Junction	3.75

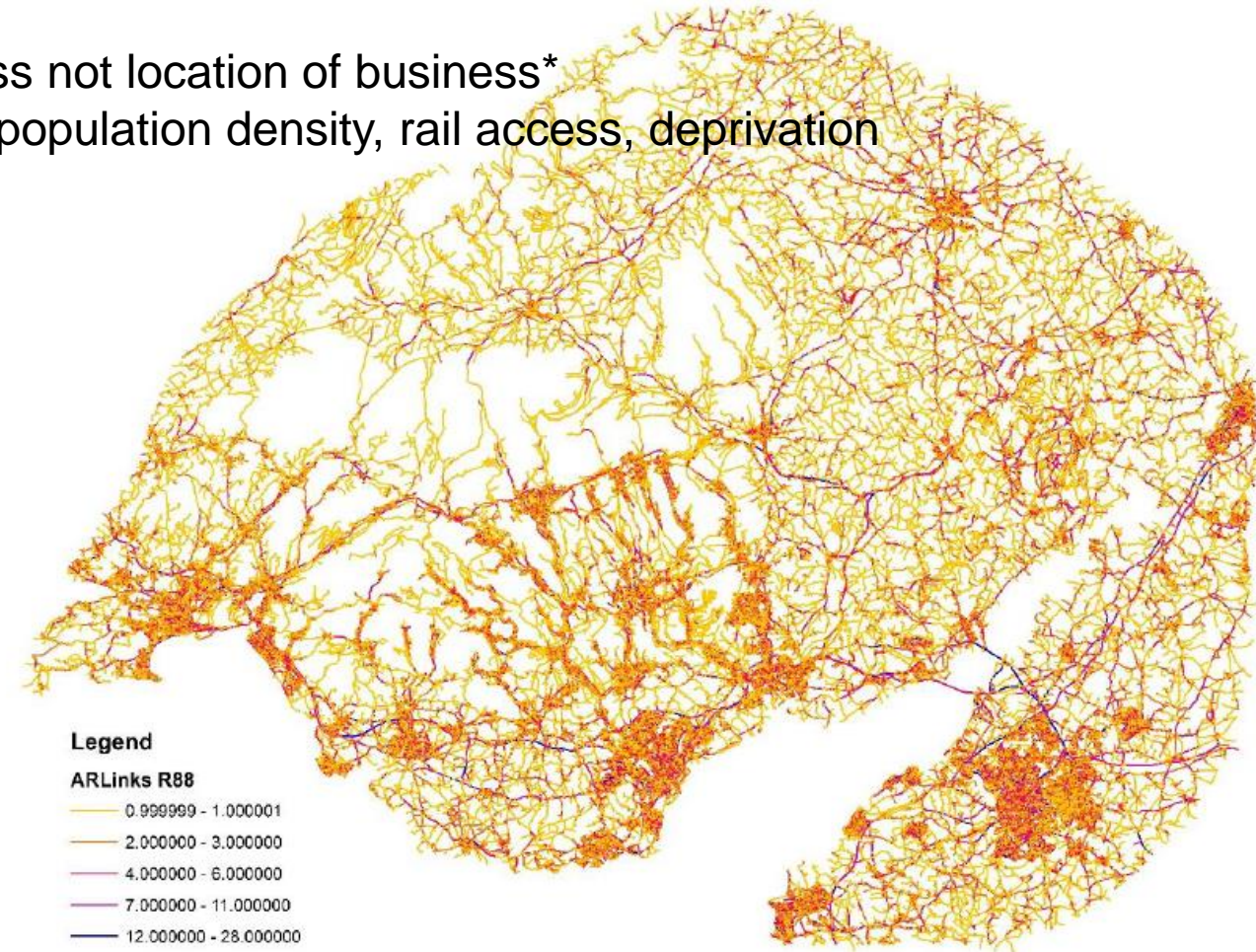
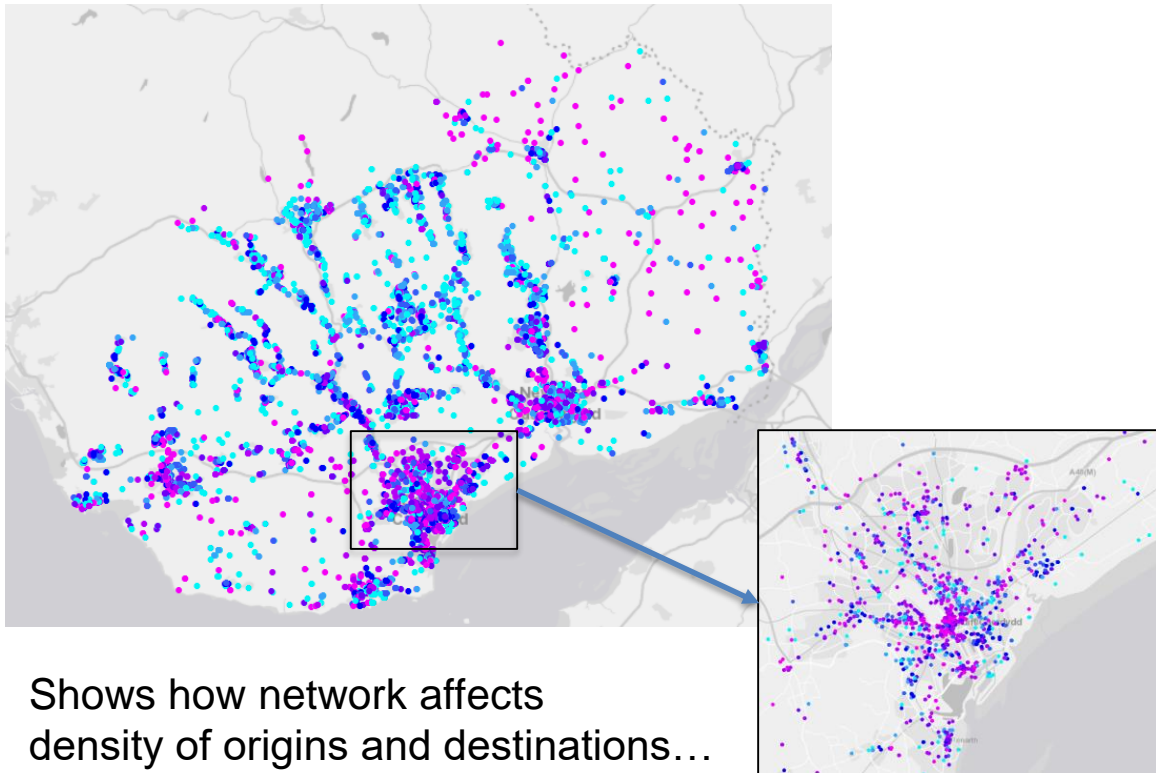


Network Economic links: Business Rates

Aamir Mohammed MSc Dissertation

Study was pitched at predicting rates for existing business not location of business*

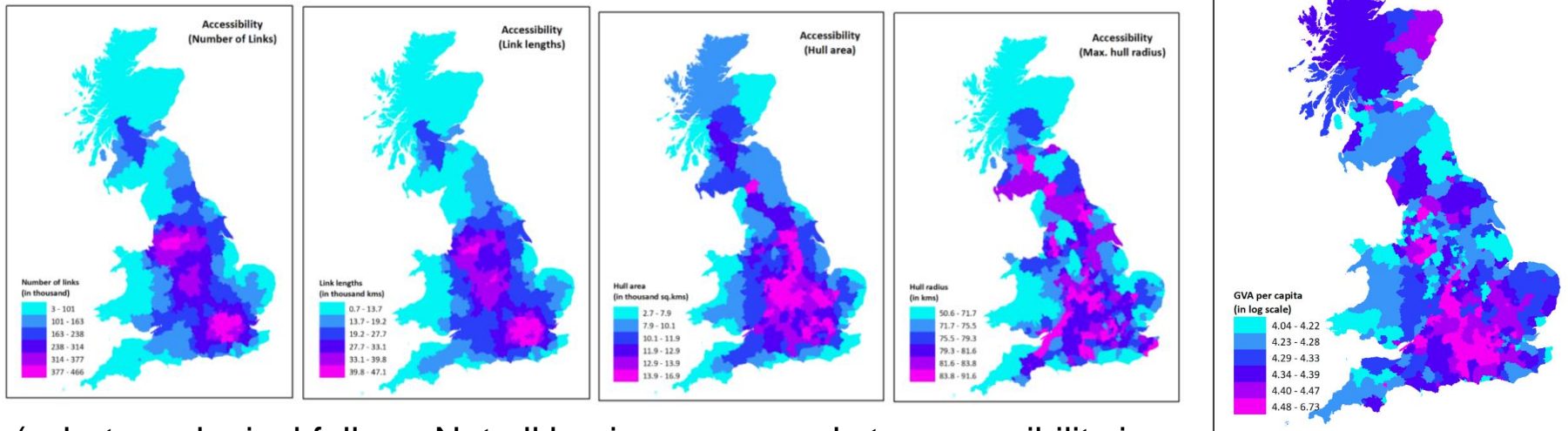
Highly significant association (esp R880), controlling for population density, rail access, deprivation



Network Economic links: GVA

Anwar Hossein MSc Dissertation

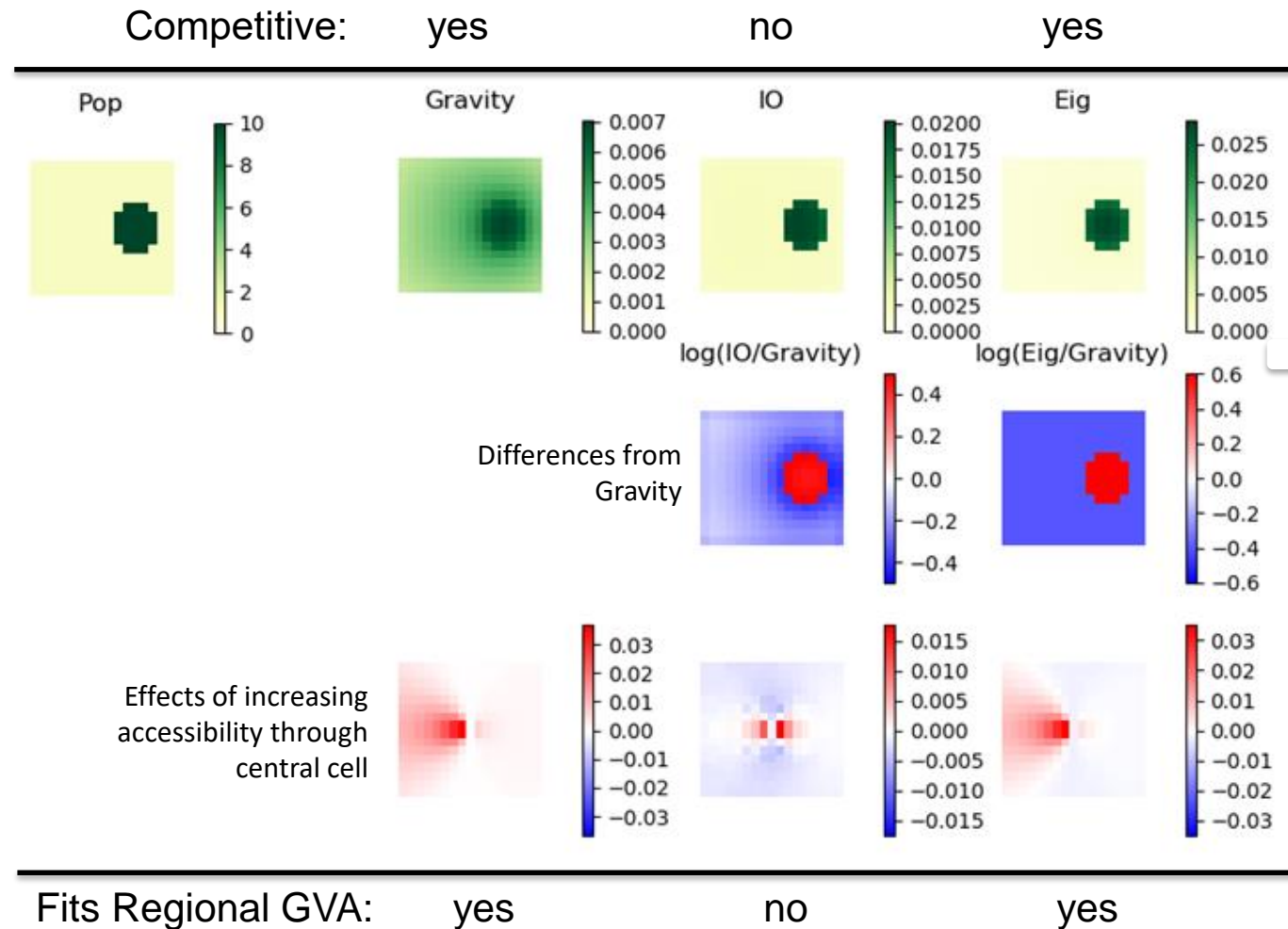
Significant network effects on GVA (especially Convex Hull Area – an efficiency measure), controlling for population density, employment, education.



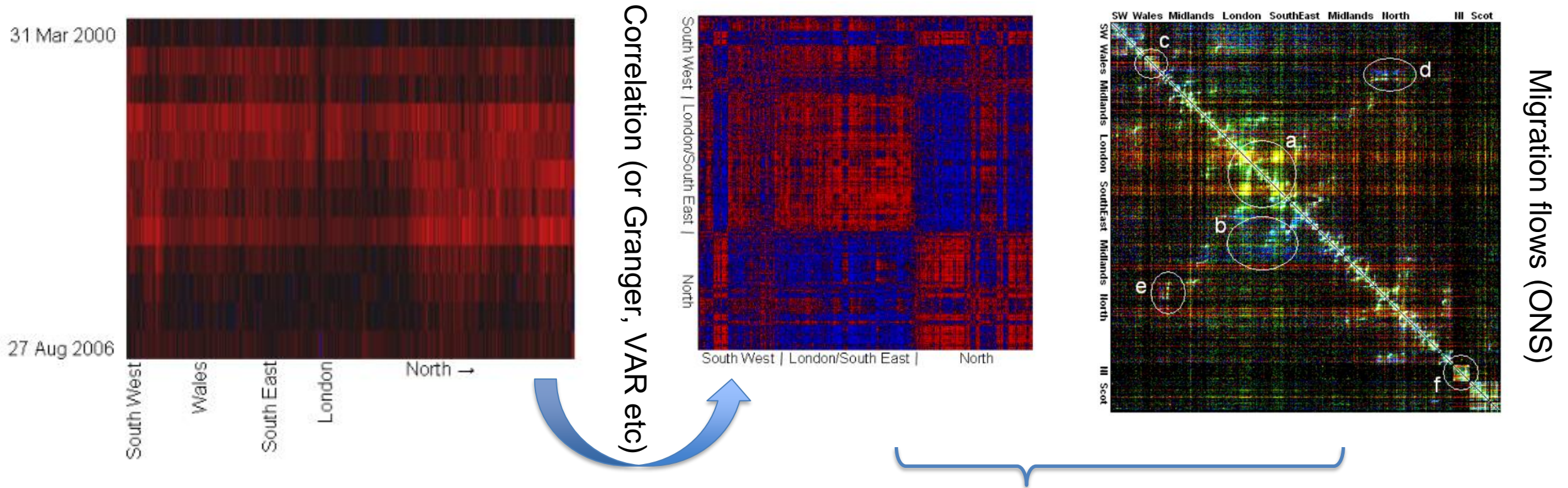
(...but, ecological fallacy. Not all business responds to accessibility in the same way; effect of accessibility on GVA appears to be both mediated and moderated by knowledge based industry (in cross sectional model. Longitudinal effects are unclear.)

Differing models of spatial competition

- Gravity model
 - dominant in economics, fits national GVA data
 - reducing distances always increases a gravity score, so not spatially competitive (unless used in model to divide limited resource)
- Intervening Opportunities
 - Reducing distances can reduce an IO score by diverting attention away
 - Does not fit national GVA data
- Eigenvalue centrality
 - reducing distances can reduce an eigenvalue score by diverting attention away
 - Does fit national GVA data
- Bayesian MCMC model comparison shows Gravity still better model however



Economics: spatial time series as network



Showed ripple effect in house prices caused more by similarity between areas than spatial interaction
Cooper Orford Webster (2011)

Regionalization

- Identification of Regional Areas for the National Development Framework. Welsh Government, 2017 (Webb, Harris, Cooper, Harvey, Healey)
- 54 variables spanning themes of Wellbeing for Future Generations Act, derived from & weighted by stakeholder consultation
- Network variables included
 - Quantity of accessible natural recreational space within short drive (any)
 - Quantity of accessible natural recreational space within short drive (high quality)
 - Travel time from key population centres
 - Communities derived from interaction data (Clauset, Newman & Moore 2004)
 - Migration
 - Commuting

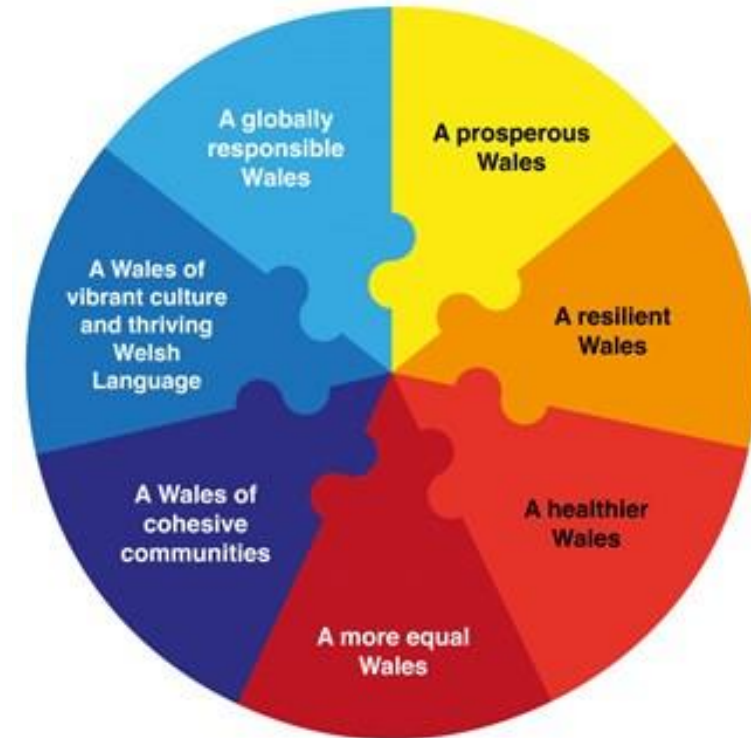


Figure 18: All Well-being Themes (Weighted) with Commuting Flows / 7 Regions

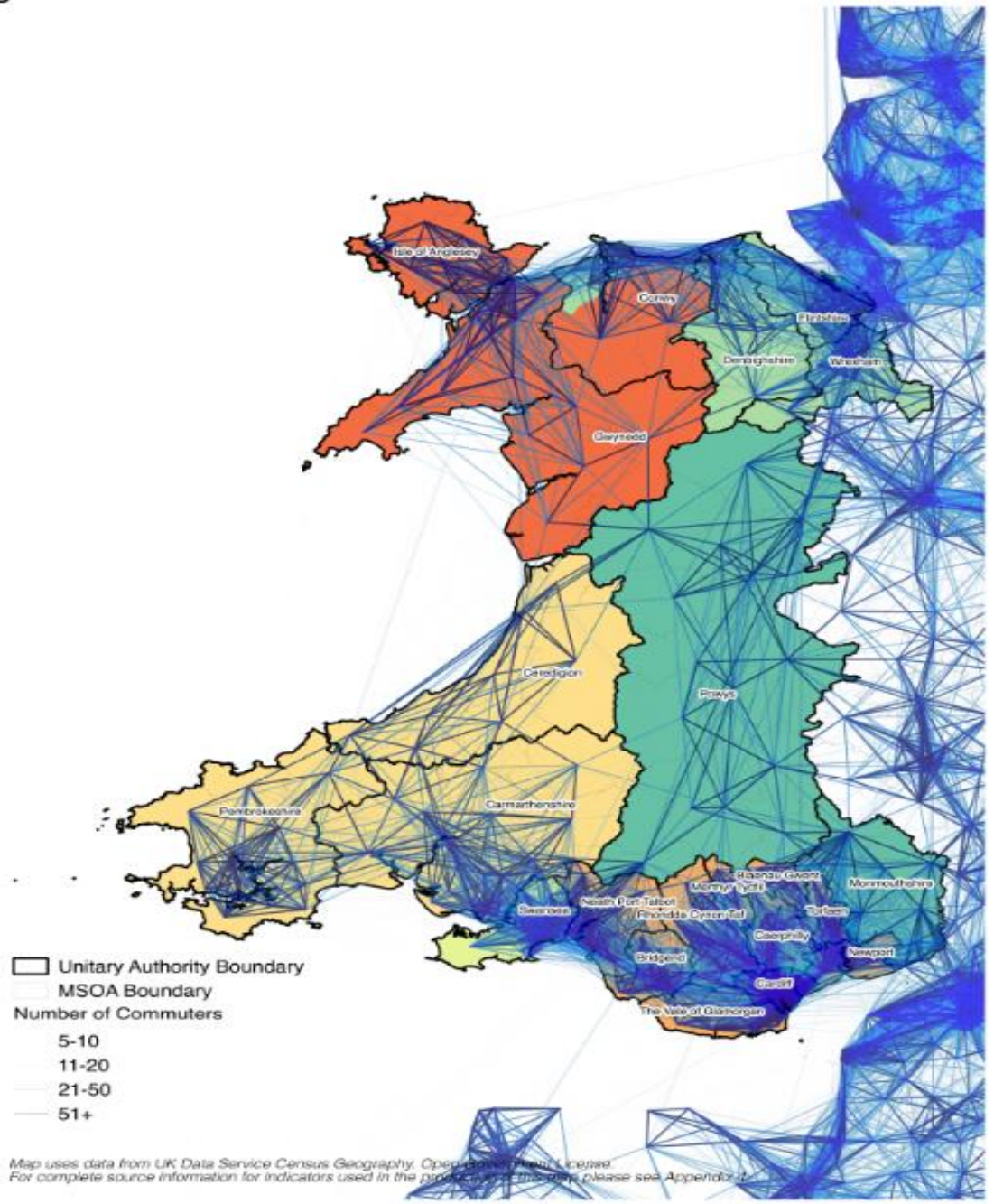


Figure 19: All Well-being Themes (Weighted) with Commuting Flows and Cross-boundary Areas / 7 Regions

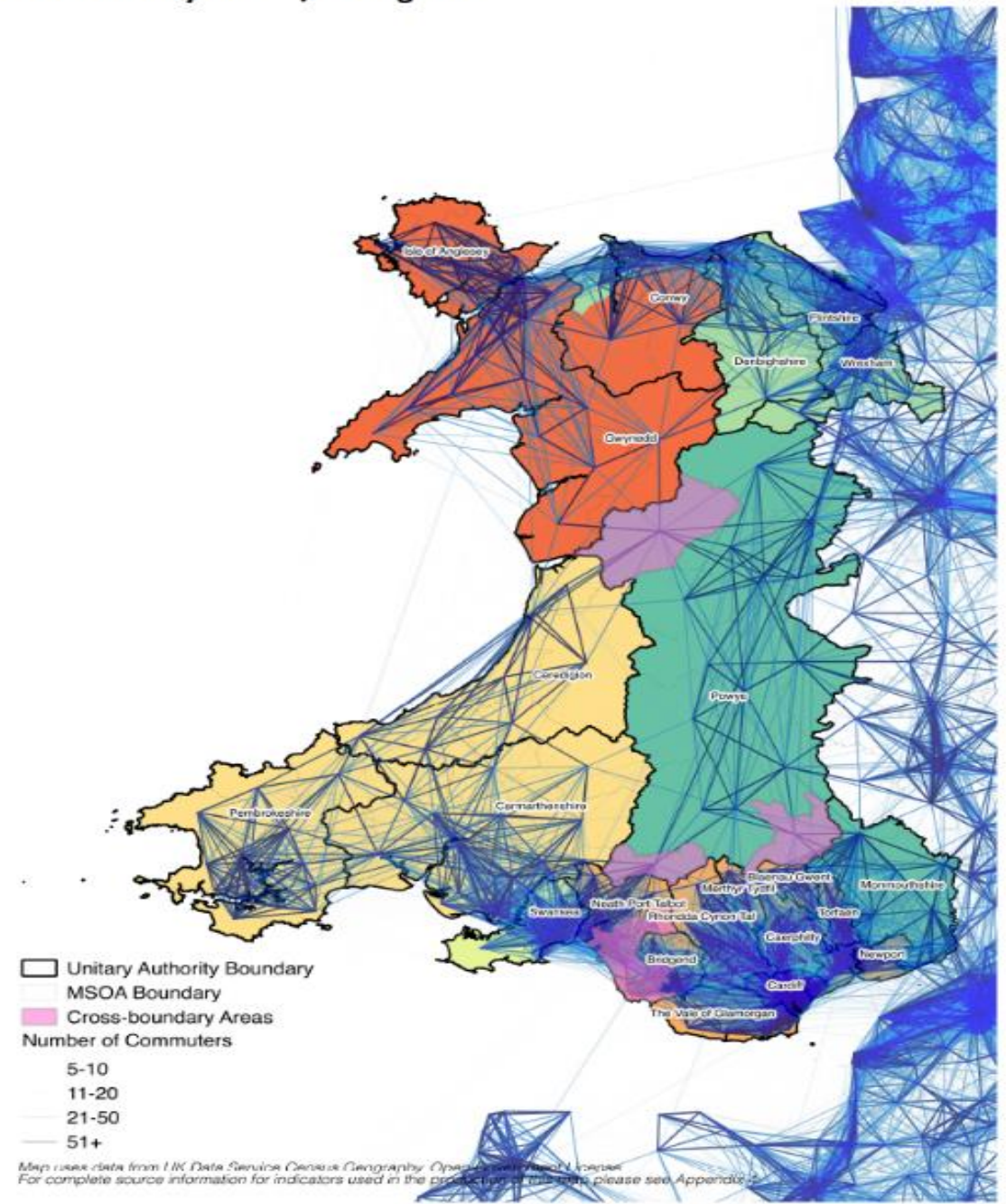


Figure 16: All Well-being Themes (Weighted) / 4 Regions

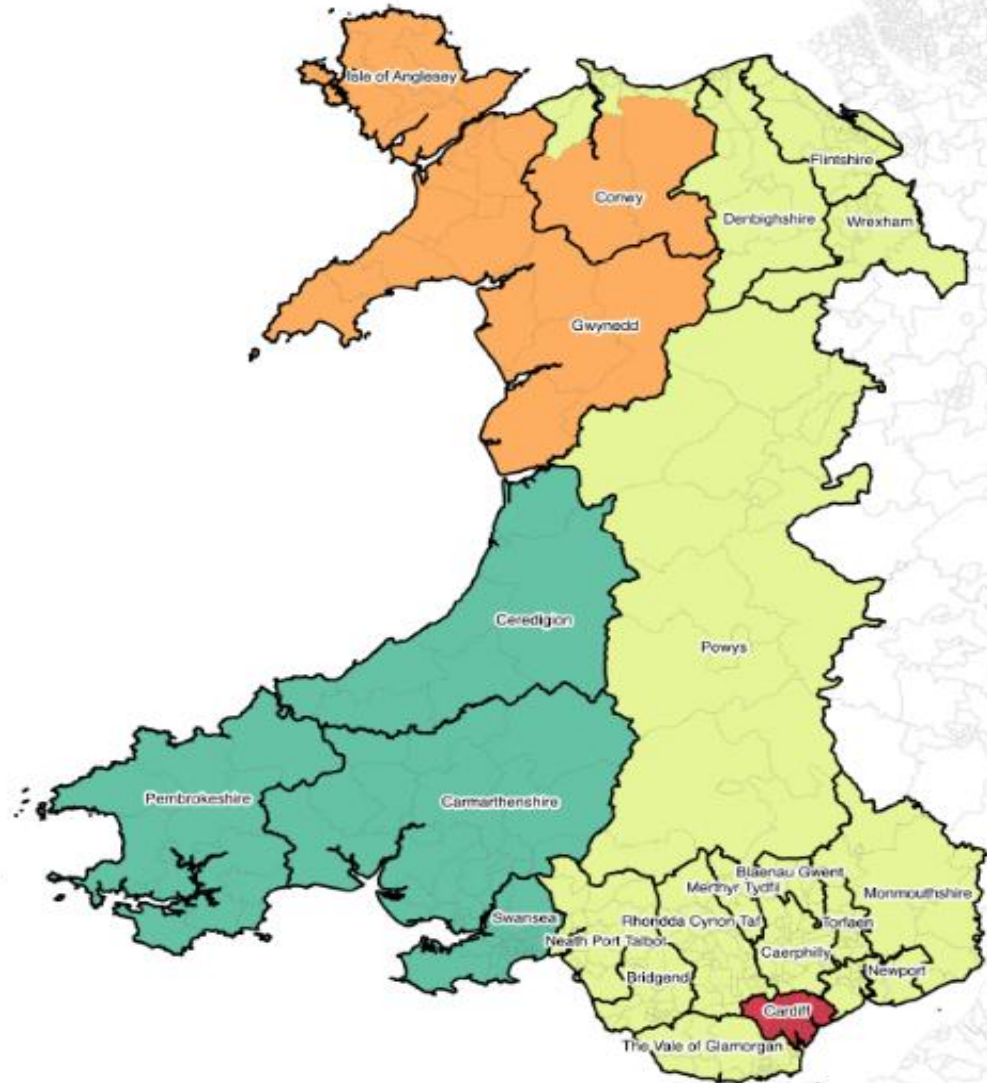
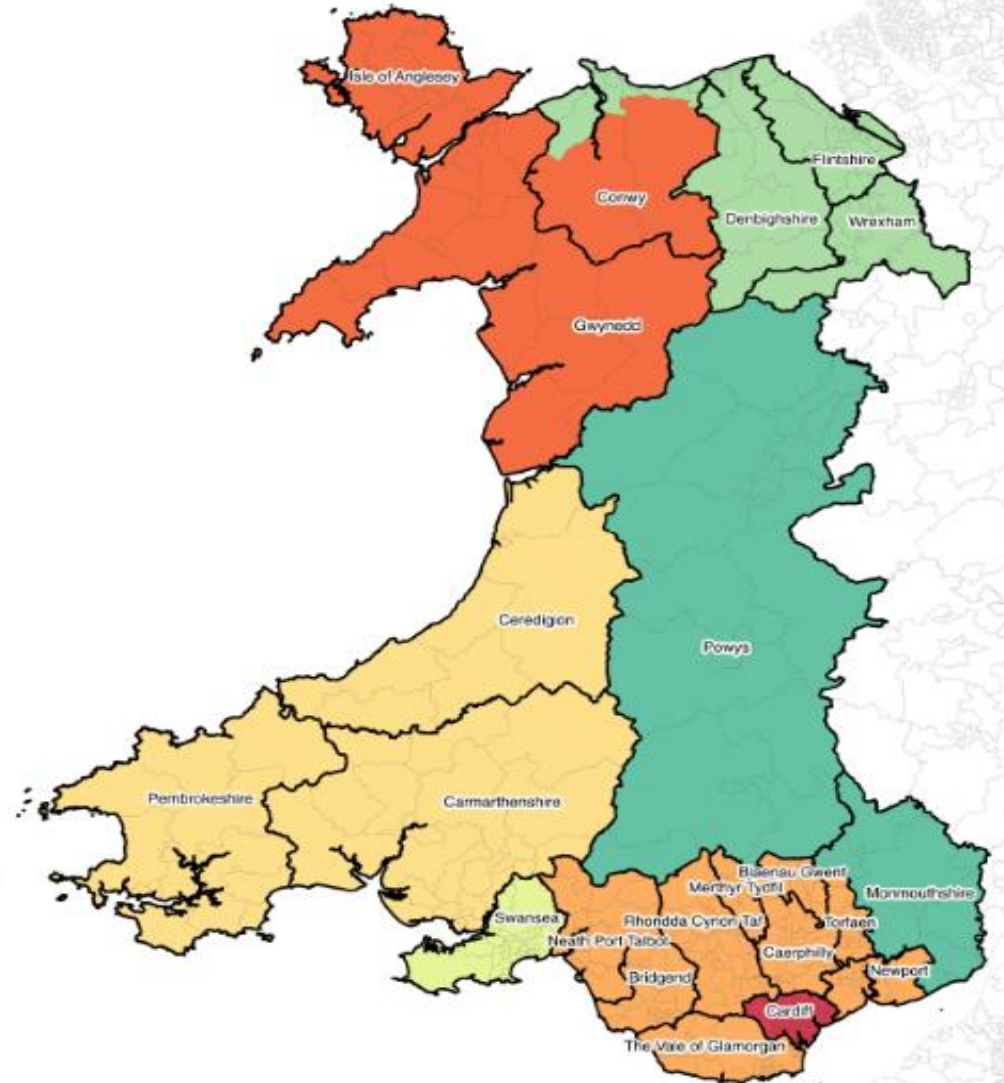
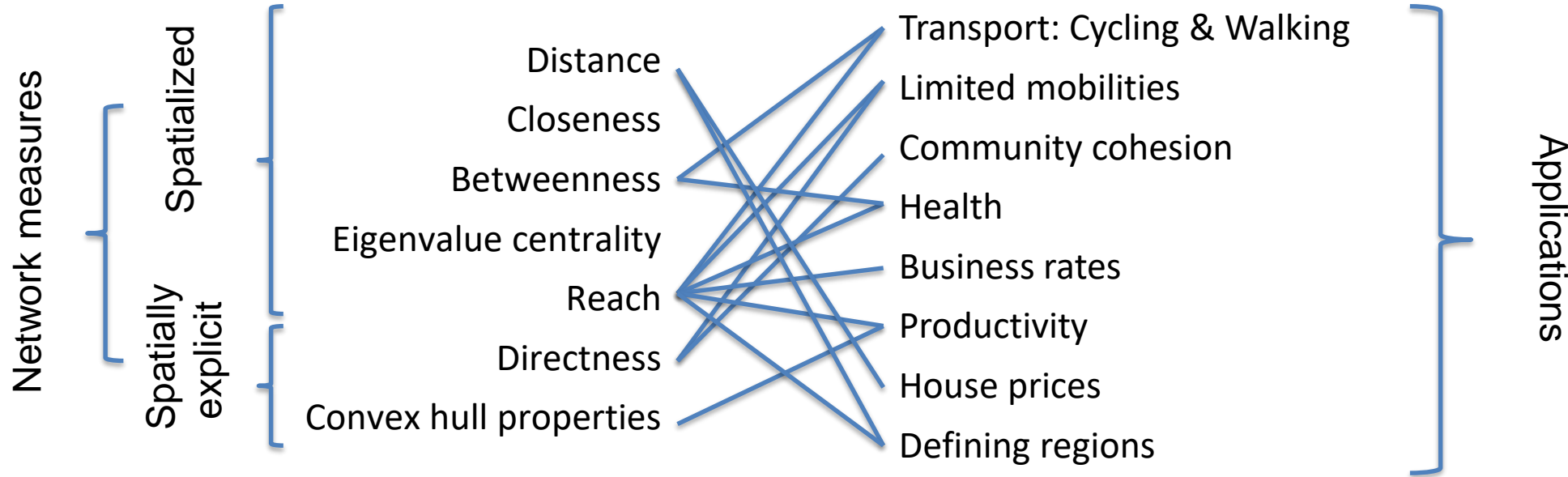


Figure 17: All Well-being Themes (Weighted) / 7 Regions



Summary



- Don't forget the Free software!
 - Plugin for ArcGIS, QGIS, Autocad

